CS131 Applicative worksheet
This isn't homework and is worth no credit. But it's good practice!

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Name:		
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	I encourage you to collaborate. Please record your collaborations below.	
	I encourage you to work these problems by hand, on the board. You'll learn the most, not to mention getting the best practice for exams.	
	Most solutions can be written in a single-line. Some solutions may take as many as four or five lines, but any more and you're off the scent.	
	Feel free to use Prelude definitions that <i>help</i> but don't make the question trivial.	
Collaborators:		

1 Instances

1.1 One of each, please

Write Functor and Applicative instances for the following datatype. Write the instantiated type of each instance function, even though Haskell doesn't want it.

data Pair a = Pair a a

1.2 One or the other

Write Functor and Applicative instances for the following datatype. Write the instantiated type of each instance function, even though Haskell doesn't want it.

data Choice a = ColumnA a | ColumnB a

Justify your choice for pure.

1.3 Reader

```
instance Functor ((->) r) where
  -- fmap :: (a -> b) -> (r -> a) -> (r -> b)
  fmap = (.)
```

Write an Applicative instance for (->) r. Write the instantiated type of each instance function, even though Haskell doesn't want it. (It's common to write such types as comments, like above.)

2 Abstracting out the essence

2.1 Not if you called them "stench blossoms"

Write a function that takes a first name and a last name and tries to join them into a full name. We'll do it first for Maybe and Either, then in general. For example, maybeName (Just "Dr.") (Just "Dave") should yield Just "Dr. Dave", but maybeName (Just "Madonna") Nothing should yield Nothing.

maybeName :: Maybe String -> Maybe String -> Maybe String

eitherName :: Either e String -> Either e String -> Either e String

nameA :: Applicative f => f String -> f String -> f String

2.2 Are phonebooks even a thing anymore?

import qualified Data.Map as Map
import Data.Map (Map)

Given a key, a value, and a map, Map.insert will add a new mapping. Write the following two functions using pattern matching which *try* to add new mappings, if all of the appropriate information is present.

maybeInsert :: Maybe k -> Maybe a -> Map k a -> Maybe (Map k a)

eitherInsert :: Either e k \rightarrow Either e a \rightarrow Map k a \rightarrow Either e (Map k a)

Write the following function. The A is for Applicative.

insertA :: Applicative $f \Rightarrow f k \Rightarrow f a \Rightarrow Map k a \Rightarrow f (Map k a)$

3 Generalizing

3.1	How art thou a	king //	But.	by fair	sequence	and	succession?
0.1	now are thou a	KIIIS / /	Due	by rain	sequence	and	succession.

Write a function sequence A :: Applicative f => [f a] -> f [a].

Go take a look at the Traversable type class in the Prelude.

3.2 One-upping

Look at Control.Applicative: there are functions liftA, liftA2, and liftA3. Look at the type of liftA... what other names does this function have?

Implement liftA2 and liftA3.

Write the type of ${\tt liftA4}$ and implement it.

3.3 To the left, to the left

Write (*>) :: Applicative f => f a -> f b -> f b (without using the built-in (*>) of the type class itself). Note that Nothing *> Just "little old me" == Nothing.

Write (<*) :: f a -> f b -> f a.

Why does Haskell include (<*) and (*>) in the Applicative type class?

3.4 I'm not listening

Write a function ignore :: Applicative $f \Rightarrow f$ a $\rightarrow f$ (). Throw away as little as possible.