

## Longest word code

## Relationship between distributions



## Relationship between distributions

$P(51$ Pass, EngPass $)=P($ EngPass $) * P(51$ Pass $\mid$ EngPass $)$

The probability of passing CS51 and English is:

1. Probability of passing English *
2. Probability of passing CS51 given that you passed English

Can think of it as describing the two events happening in two steps:
The likelihood of $X$ and $Y$ happening:

1. How likely it is that $Y$ happened?
2. Given that $Y$ happened, how likely is it that $X$ happened?

| Relationship between distributions |
| :--- |
| $P(51$ Pass, EngPass $)=P(51$ Pass $) * P($ EngPass $\mid 51$ Pass $)$ |
| The probability of passing CS51 and English is: |
| 1. Probability of passing CS51 * |
| 2. Probability of passing English given that you passed $\mathrm{CS51}$ |
| Can also view it with the other event happening first |





| One observation |
| :---: |
| $P($ positive $) * P($ datalpositive $)$ |
| $P($ negative $) * P($ data\|negative $)$ | MAX $\quad$ For picking the largest $P($ data $)$ doesn't matter!




| An aside: $P($ heads $)$ |
| :--- |
| What is the $P($ heads ) on a fair coin? |
| 0.5 |
| What if you didn't know that, but had a coin to |
| experiment with? |
| Flip it a bunch of times and count how many times it comes |
| up heads |
| P(heads) $=\frac{\text { number of times heads came up }}{\text { total number of coin tosses }}$ |

Try it out...

| $P($ feature $\mid$ label $)$ |
| :---: |
| $P($ heads $)=\frac{\text { number of times heads came up }}{\text { total number of coin tosses }}$ |
| Can we do the same thing here? What is the probability of a |
| feature given positive, i.e. the probability of a feature occurring in |
| in the positive label? |
| $P($ feature 1 positive $)=?$ |

## P(feature |label)

$P($ heads $)=\frac{\text { number of times heads came up }}{\text { total number of coin tosses }}$

Can we do the same thing here? What is the probability of a feature given positive, i.e. the probability of a feature occurring in in the positive label?

$$
P(\text { feature } \mid \text { positive })=\frac{\text { number of positive examples with that feature }}{\text { total number of positive examples }}
$$

## Training Naïve Bayes



| Nailve Bayes Text Classification |  |
| :--- | :--- |
| Positive |  |
| I loved it <br> I loved that movie <br> I hated that I loved it | Negative |
| Given examples of text in different categories, learn to predict the <br> category of new examples |  |
| Sentiment classification: given positive/negative examples of text <br> (sentences), learn to predict whether new text is positive/negative |  |


| Text classification training |  |
| :--- | :--- |
| Positive |  |
| I loved it <br> I loved that movie <br> I hated that I loved it | Negative <br> I hated it <br> I hated that movie <br> I loved that I hated it |
| We'll assume words iust occur once in any given sentence |  |


| Text classification training |  |
| :--- | :--- |
| Positive | Negative |
| I loved it <br> I loved that movie <br> I hated that loved it | I hated it <br> I hated that movie <br> I loved that hated it |
| We'll assume words iust occur once in any given sentence |  |


| Training the model |  |
| :---: | :---: |
| Positive <br> I loved it <br> I loved that movie <br> I hated that loved it <br> For each wor <br> p(word \| | Negative <br> I hated it <br> I hated that movie <br> I loved that hated it <br> 1, learn: |


| Training the model |  |
| :--- | :--- |
| Positive | Negative |
| I loved it | I hated it |
| I loved that movie |  |
| I hated that loved it | I hated that movie |
| I loved that hated it |  |


| Training the model |  |
| :---: | :---: |
| Positive | Negative |
| I loved it | I hated it |
| I loved that movie | I hated that movie |
| I hated that loved it | I loved that hated it |
| $\mathrm{P}(1 \mid$ positive) $=3 / 3=1.0$ |  |
| $P(\text { word } \mid \text { label })=\frac{\text { number of times word occured in "label" examples }}{\text { total number of examples with that label }}$ |  |


| Training the model |  |
| :---: | :---: |
| Positive | Negative |
| I loved it | I hated it |
| I loved that movie | I hated that movie |
| I hated that loved it | I loved that hated it |
| $\mathrm{P}(\mathrm{I} \mid$ positive) P(loved \| positive) |  |
| $P(\text { word } \mid \text { label })=\frac{\text { number of times word occured in "label" examples }}{\text { total number of examples with that label }}$ |  |


| Training the model |  |
| :---: | :---: |
| Positive | Negative |
| I loved it | I hated it |
| I loved that movie | I hated that movie |
| I hated that loved it | I loved that hated it |
| $\mathrm{P}(1 \mid$ positive) |  |
| P (loved \| positive) |  |
| $P(\text { word } \mid \text { label })=\frac{\text { number of times word occured in "label" examples }}{\text { total number of examples with that label }}$ |  |



| Training the model |  |  |
| :---: | :---: | :---: |
| Positive |  | Negative |
| I loved it |  | I hated it |
| I loved that movie |  | I hated that movie |
| I hated that loved it |  | I loved that hated it |
| P (1 \\| positive) | $=1.0$ | $\mathrm{P}(\mathrm{l} \mid$ negative $)=$ ? |
| P (loved \| positive) | $=2 / 3$ |  |
| P (hated \| positive) | $=1 / 3$ |  |
| $P(\text { word } \mid \text { label })=\frac{\text { number of times word occured in "label" examples }}{\text { total number of examples with that label }}$ |  |  |



| Training the model |  |  |  |
| :---: | :---: | :---: | :---: |
| Positive |  | Negative |  |
| I loved it |  | I hated it |  |
| I loved that movie |  | I hated that movie |  |
| I hated that loved it |  | I loved that hated it |  |
| $\mathrm{P}(1 \mid$ positive) | $=1.0$ | $\mathrm{P}(1 \mid$ negative) | $=1.0$ |
| P (loved \| positive) | $=2 / 3$ | P (movie \| negative) |  |
| P (hated \| positive) | $=1 / 3$ |  |  |
| $P(\text { word } \mid \text { label })=\frac{\text { number of times word occured in "label" examples }}{\text { total number of examples with that label }}$ |  |  |  |


| Training the model |  |  |  |
| :---: | :---: | :---: | :---: |
| Positive |  | Negative |  |
| I loved it |  | I hated it |  |
| I loved that movie |  | I hated that movis |  |
| I hated that loved it |  | I loved that hated it |  |
| $\mathrm{P}(\mathrm{I} \mid$ positive) P (loved \| positive) | $\begin{aligned} & =1.0 \\ & =2 / 3 \end{aligned}$ | $\mathrm{P}(1 \mid$ negative) P (movie \| negative) | $\begin{aligned} & =1.0 \\ & =1 / 3 \end{aligned}$ |
| P (hated \| positive) | $=1 / 3$ | ... |  |
| $P(\text { word } \mid \text { label })=\frac{\text { number of times word occured in "label" examples }}{\text { total number of examples with that label }}$ |  |  |  |



| Trained model |  |  |  |
| :---: | :---: | :---: | :---: |
| $\mathrm{P}(\mathrm{l} \mid$ positive) | $=1.0$ | $\mathrm{P}(1 \mid$ negative $)$ | $=1.0$ |
| P(loved \| positive) | $=2 / 3$ | p (hated \| negative) | $=1.0$ |
| $p$ (it \| positive) | $=2 / 3$ | p (that \| negative) | $=2 / 3$ |
| $p$ (that \| positive) | $=2 / 3$ | P (movie \| negative) | $=1 / 3$ |
| p (movie \| positive) | $=1 / 3$ | p (it \| negative) | $=2 / 3$ |
| P (hated \| positive) | $=1 / 3$ | $p$ (loved \| negative) | $=1 / 3$ |
| $\mathrm{P}(1 \mid$ positive $) * \mathrm{P}($ hated $\mid$ positive $) * \mathrm{P}($ movie $\mid$ positive $)=1.0 * 1 / 3 * 1 / 3=1 / 9$ |  |  |  |
| $\mathrm{P}(1 \mid$ negative) $* \mathrm{P}($ hated \| negative) $* \mathrm{P}($ movie \| negative) $=1.0 * 1.0 * 1 / 3=1 / 3$ |  |  |  |

## Trained model

| $\mathrm{P}(I \mid$ positive $)$ | $=1.0$ | $\mathrm{P}(\|\mid$ negative $)$ | $=1.0$ |
| :--- | :--- | :--- | :--- |
| P (loved \| positive) | $=2 / 3$ | p (hated $\mid$ negative $)$ | $=1.0$ |
| p (it $\mid$ positive) | $=2 / 3$ | p (that $\mid$ negative | $=2 / 3$ |
| p (that \| positive) | $=2 / 3$ | P (movie $\mid$ negative) | $=1 / 3$ |
| p (movie \| positive) | $=1 / 3$ | p (it \| negative) | $=2 / 3$ |
| P (hated \| positive) | $=1 / 3$ | p (loved $\mid$ negative) | $=1 / 3$ |

How would we classify: "I hated movie"?

| Trained model |  |  |  |
| :---: | :---: | :---: | :---: |
| $\mathrm{P}(1 \mid$ positive) | $=1.0$ | $P(1 \mid$ negative $)$ | $=1.0$ |
| P (loved \| positive) | $=2 / 3$ | p(hated \| negative) | $=1.0$ |
| p (it \| positive) | $=2 / 3$ | p (that \| negative) | $=2 / 3$ |
| p (that \| positive) | $=2 / 3$ | P (movie \| negative) | $=1 / 3$ |
| p(movie \| positive) | $=1 / 3$ | p (it \| negative) | $=2 / 3$ |
| P (hated \| positive) | $=1 / 3$ | p(loved \| negative) | $=1 / 3$ |
| How would we classify: "I hated the movie"? |  |  |  |


| Trained model |  |  |  |
| :---: | :---: | :---: | :---: |
| $\mathrm{P}(\mathrm{I} \mid$ positive) | $=1.0$ | $\mathrm{P}(1 \mid$ negative) | $=1.0$ |
| P(loved \| positive) | $=2 / 3$ | p(hated \| negative) | $=1.0$ |
| p (it \| positive) | $=2 / 3$ | p (that \| negative) | $=2 / 3$ |
| p (that \| positive) | $=2 / 3$ | P (movie \| negative) | $=1 / 3$ |
| p(movie \| positive) | $=1 / 3$ | p (it \| negative) | $=2 / 3$ |
| P(hated \| positive) | $=1 / 3$ | p(loved \| negative) | $=1 / 3$ |
| $\mathrm{P}(\mathrm{I} \mid$ positive) $* \mathrm{P}($ hated $\mid$ positive) $* \mathrm{P}($ (the $\mid$ positive $) * \mathrm{P}($ movie $\mid$ positive) $=$ |  |  |  |
| $\mathrm{P}(\mathrm{I} \mid$ negative) $* \mathrm{P}($ hated $\mid$ negative $) * \mathrm{P}($ the $\mid$ negative $) * \mathrm{P}($ movie $\mid$ negative $)=$ |  |  |  |


| Trained model |  |  |  |
| :---: | :---: | :---: | :---: |
| $\mathrm{P}(\mathrm{l} \mid$ positive) | $=1.0$ | $\mathrm{P}(1 \mid$ negative) | $=1.0$ |
| P (loved \| positive) | $=2 / 3$ | p (hated \| negative) | $=1.0$ |
| p (it \| positive) | $=2 / 3$ | p (that \| negative) | $=2 / 3$ |
| p (that \| positive) | $=2 / 3$ | P (movie \| negative) | $=1 / 3$ |
| p (movie \| positive) | $=1 / 3$ | $p$ (it \| negative) | $=2 / 3$ |
| P (hated \| positive) | $=1 / 3$ | p(loved \| negative) | $=1 / 3$ |
| $\begin{aligned} & \mathrm{P}(\mathrm{I} \mid \text { positive }) * \mathrm{P}(\text { hated } \mid \text { positive }) * \mathrm{P}(\text { the } \mid \text { positive }) * \mathrm{P}(\text { movie } \mid \text { positive })= \\ & \mathrm{P}(\mathrm{I} \mid \text { negative }) * \mathrm{P}(\text { hated } \mid \text { negative }) * \mathrm{P}(\text { the } \mid \text { negative }) * \mathrm{P}(\text { movie } \mid \text { negative })= \end{aligned}$ |  |  |  |
|  |  |  |  |
| What are these? |  |  |  |


| Trained model |  |  |  |
| :---: | :---: | :---: | :---: |
| $\mathrm{P}(\mathrm{I} \mid$ positive) | $=1.0$ | $\mathrm{P}(1 \mid$ negative) | $=1.0$ |
| P(loved \\| positive) | $=2 / 3$ | p (hated \| negative) | $=1.0$ |
| $p$ (it \| positive) | $=2 / 3$ | p (that \| negative) | $=2 / 3$ |
| $p$ (that \| positive) | $=2 / 3$ | P (movie \| negative) | $=1 / 3$ |
| p (movie \| positive) | $=1 / 3$ | p (it \| negative) | $=2 / 3$ |
| P (hated \| positive) | $=1 / 3$ | p(loved \| negative) | $=1 / 3$ |
| $\mathrm{P}(\mathrm{I} \mid$ positive) $* \mathrm{P}($ hated $\mid$ positive) $* \mathrm{P}($ the $\mid$ positive $) * \mathrm{P}($ movie \| positive) $=$ |  |  |  |
| $\mathrm{P}(\mathrm{l} \mid$ negative) * $\mathrm{P}($ hated $\mid$ negative $) * \mathrm{P}($ the $\mid$ negative $) * \mathrm{P}($ movie $\mid$ negative $)=$ |  |  |  |
| 0! Is this a problem? |  |  |  |


| Trained model |  |  |  |
| :---: | :---: | :---: | :---: |
| $\mathrm{P}(\mathrm{I} \mid$ positive) | $=1.0$ | $P(1 \mid$ negative $)$ | $=1.0$ |
| P(loved \| positive) | $=2 / 3$ | p (hated \| negative) | $=1.0$ |
| p (it \| positive) | $=2 / 3$ | p (that \| negative) | $=2 / 3$ |
| p (that \| positive) | $=2 / 3$ | P (movie \| negative) | $=1 / 3$ |
| $p$ (movie \| positive) | $=1 / 3$ | p (it \| negative) | $=2 / 3$ |
| P(hated \| positive) | $=1 / 3$ | p(loved \| negative) | $=1 / 3$ |
| $\mathrm{P}(\mathrm{I} \mid$ positive) $* \mathrm{P}($ hated \| positive) * $\mathrm{P}($ the \| positive) * $\mathrm{P}($ movie \| positive) $=$ |  |  |  |
| $\mathrm{P}(\mathrm{l} \mid$ negative) $* \mathrm{P}($ hated $\mid$ negative $) * \mathrm{P}($ the \| negative) $* \mathrm{P}($ movie \| negative) $=$ |  |  |  |
| Yes. They make the entire product go to 0! |  |  |  |


| Trained model |  |  |  |
| :---: | :---: | :---: | :---: |
| $\mathrm{P}(\mathrm{I} \mid$ positive) | $=1.0$ | $\mathrm{P}(1 \mid$ negative) | $=1.0$ |
| P(loved \| positive) | $=2 / 3$ | $p$ (hated \| negative) | $=1.0$ |
| p (it \| positive) | $=2 / 3$ | p (that \| negative) | $=2 / 3$ |
| p (that \| positive) | $=2 / 3$ | P (movie \| negative) | $=1 / 3$ |
| p (movie \| positive) | $=1 / 3$ | p (it \| negative) | $=2 / 3$ |
| P (hated \| positive) | $=1 / 3$ | p(loved \| negative) | $=1 / 3$ |
| $\mathrm{P}(\mathrm{I} \mid$ positive) $* \mathrm{P}($ hated \| positive) $* \mathrm{P}($ (he $\mid$ positive $) * \mathrm{P}($ movie \| positive) $=$ |  |  |  |
| $\mathrm{P}(\mathrm{I} \mid$ negative $) * \mathrm{P}($ hated $\mid$ negative $) * \mathrm{P}($ (he $\mid$ negative $) * \mathrm{P}($ movie $\mid$ negative $)=$ |  |  |  |
| Our solution: assume any unseen word has a small, fixed probability, e.g. in this example $1 / 10$ |  |  |  |


| Trained model |  |  |  |
| :---: | :---: | :---: | :---: |
| $\mathrm{P}(\mathrm{l} \mid$ positive) | $=1.0$ | $P(1 \mid$ negative $)$ | $=1.0$ |
| P(loved \| positive) | $=2 / 3$ | p (hated \| negative) | $=1.0$ |
| p (it \| positive) | $=2 / 3$ | p (that \| negative) | $=2 / 3$ |
| p (that \| positive) | $=2 / 3$ | P (movie \| negative) | $=1 / 3$ |
| p(movie \| positive) | $=1 / 3$ | p (it \| negative) | $=2 / 3$ |
| P (hated \| positive) | $=1 / 3$ | p(loved \| negative) | $=1 / 3$ |
| $\mathrm{P}(\mathrm{l} \mid$ positive) $* \mathrm{P}$ (hated \| positive) $* \mathrm{P}($ (the \| positive) $* \mathrm{P}$ (movie \| positive) $=1 / 90$ |  |  |  |
| $\mathrm{P}(1 \mid$ negative) * P(hated \| negative) * P(the | negative) * P(movie | negative) $=1 / 30$ |  |  |  |
| Our solution: assume any unseen word has a small, fixed probability, e.g. in this example $1 / 10$ |  |  |  |

## Full disclaimer

l've fudged a few things on the Naïve Bayes model for simplicity

Our approach is very close, but it takes a few liberties that aren't technically correct, but it will work just fine ©

If you're curious, l'd be happy to talk to you offline

