## 

CS158 – Fall 2019

### Admin

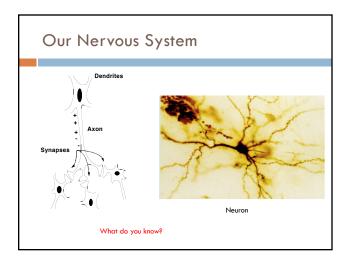
Assignment 7A solutions available on sakai in resources

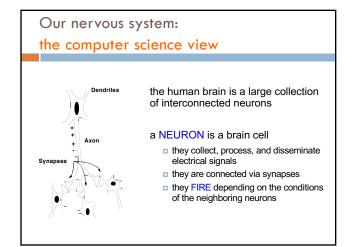
Assignment 7B

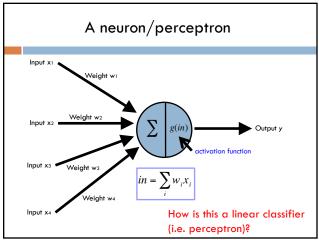
Assignment grading

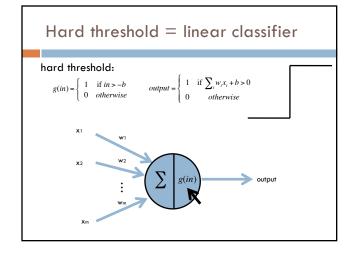
## Perceptron learning algorithm repeat until convergence (or for some # of iterations): for each training example $(f_1, f_2, ..., f_m$ label): $prediction = b + \sum_{i=1}^{n} w_i f_i$ if prediction \* label $\leq 0$ : // they don't agree for each w<sub>i</sub>: $w_i = w_i + f_i$ \*label b = b + label

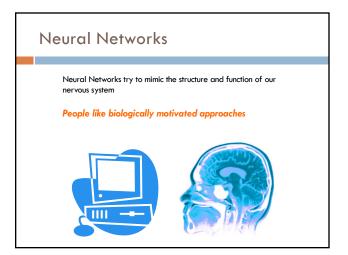
Why is it called the "perceptron" learning algorithm if what it learns is a line? Why not "line learning" algorithm?

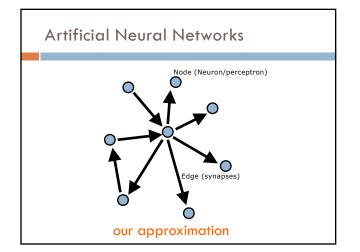


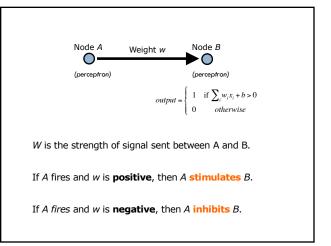


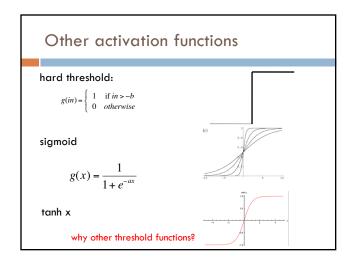


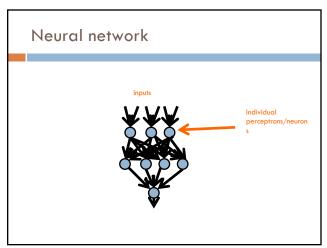


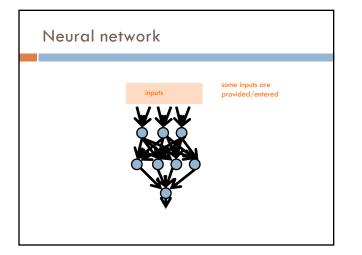


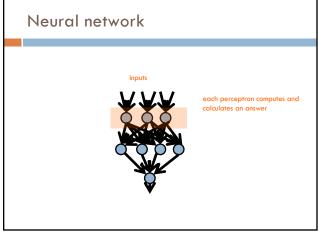


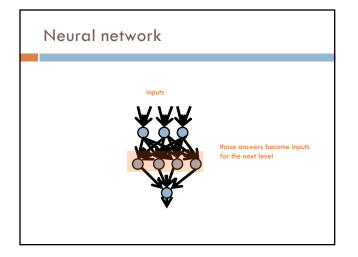


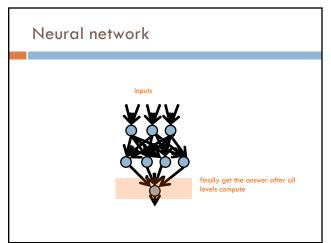


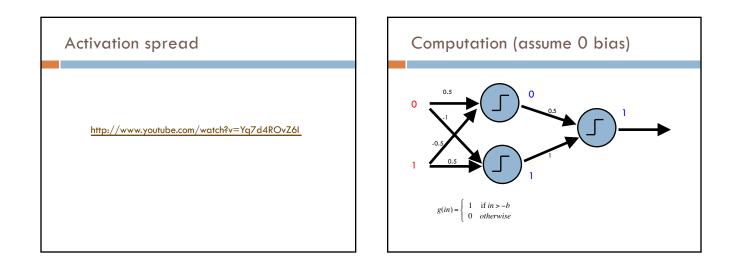


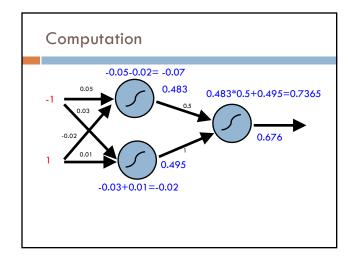


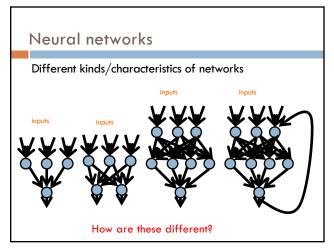


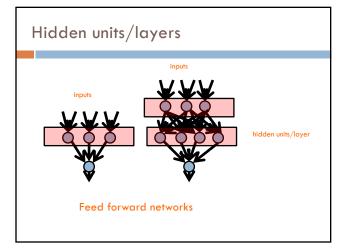


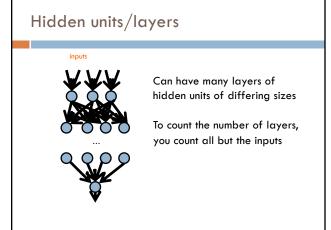


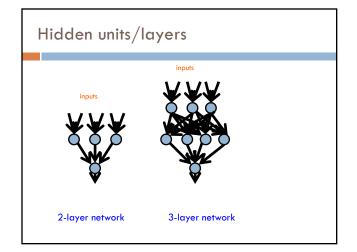


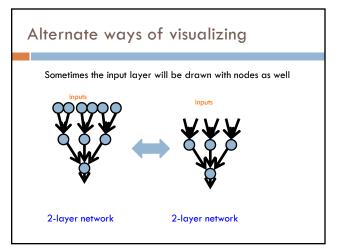


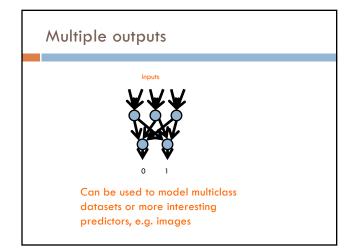


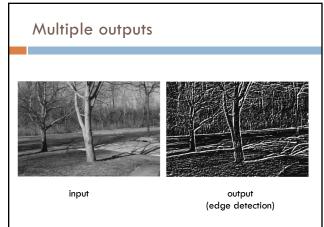


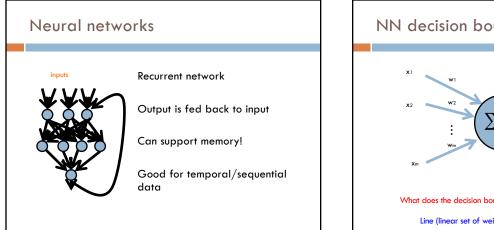


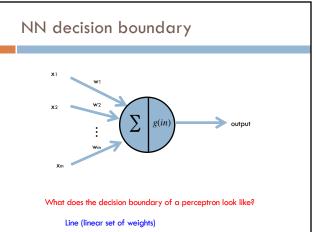


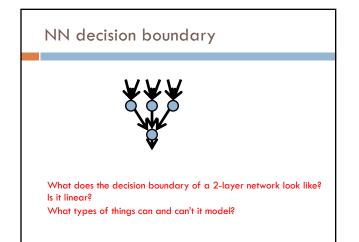


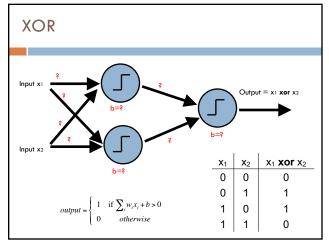


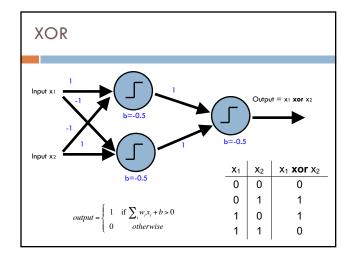


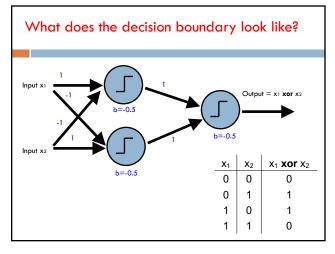


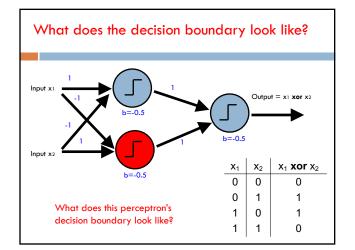


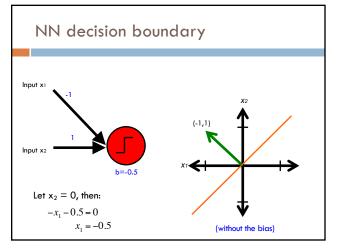


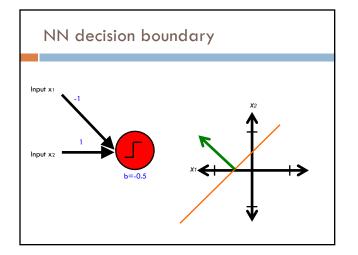


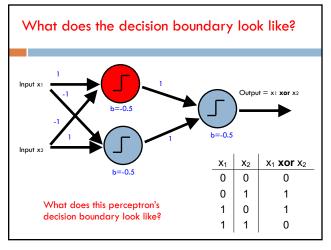


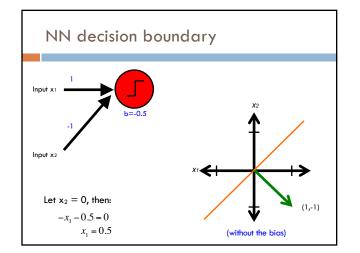


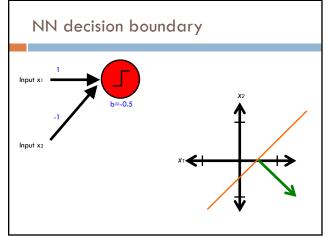


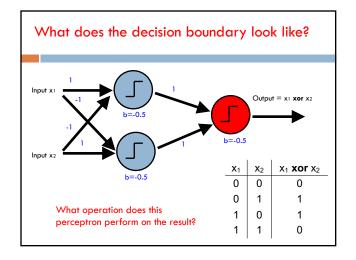


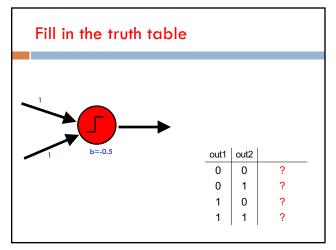


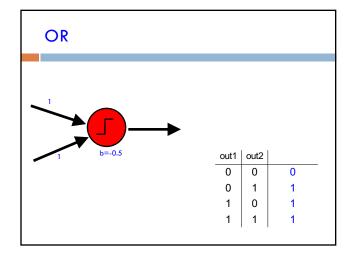


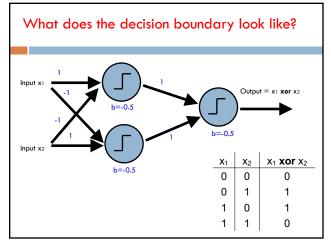


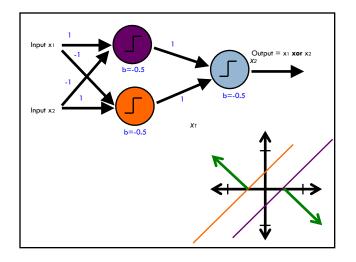


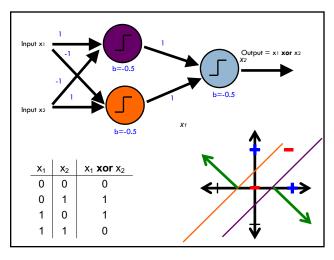


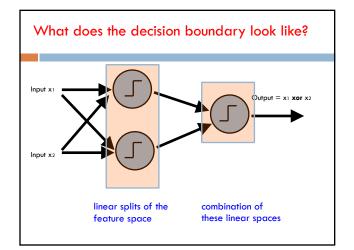


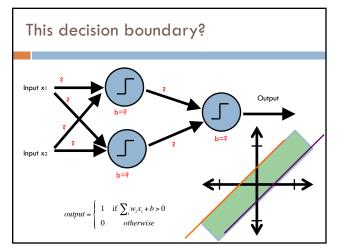


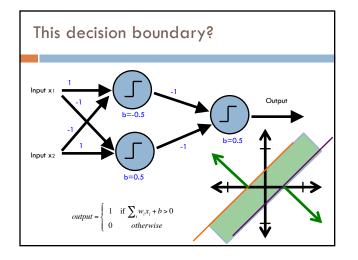


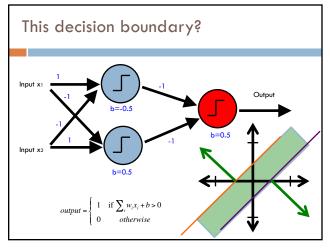


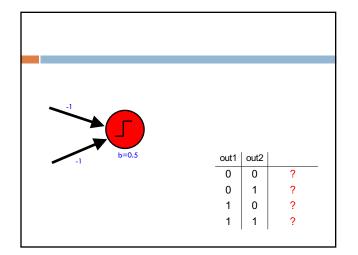


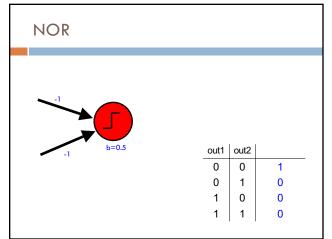


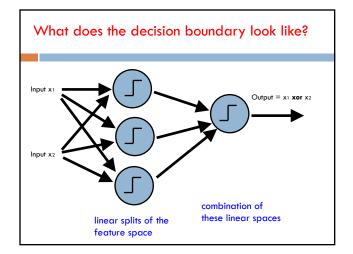


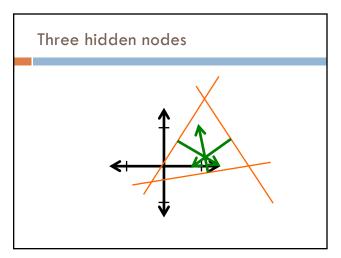










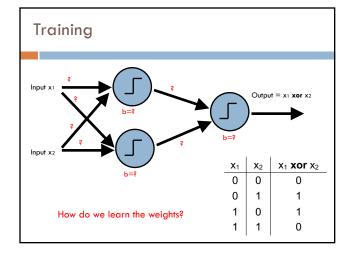


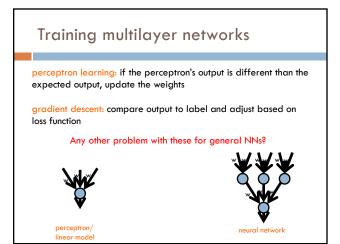
### NN decision boundaries

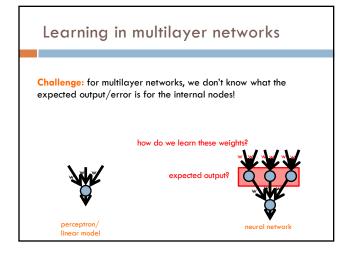
**Theorem 9** (Two-Layer Networks are Universal Function Approximators). Let F be a continuous function on a bounded subset of D-dimensional space. Then there exists a two-layer neural network  $\hat{F}$  with a finite number of hidden units that approximate F arbitrarily well. Namely, for all x in the domain of F,  $|F(x) - \hat{F}(x)| < \epsilon$ .

'Or, in colloquial terms "two-layer networks can approximate any function."

# NN decision boundaries For DT, as the tree gets larger, the model gets more complex The same is true for neural networks: more hidden nodes = more complexity Adding more layers adds even more complexity (and much more quickly) Good rule of thumb: number of 2-layer hidden nodes ≤ number of dimensions



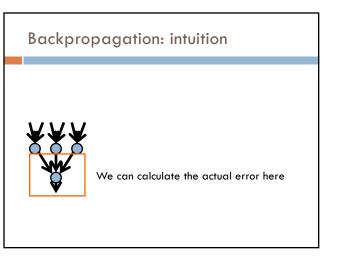


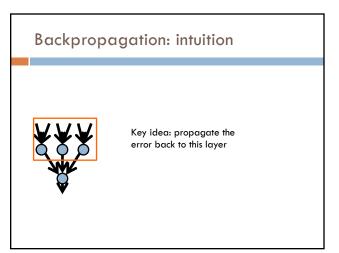


### Backpropagation: intuition

Gradient descent method for learning weights by optimizing a loss function

- 1. calculate output of all nodes
- 2. calculate the weights for the output layer based on the error
- 3. "backpropagate" errors through hidden layers



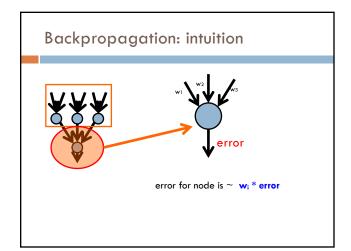


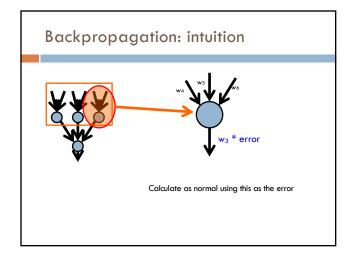
### Backpropagation: intuition

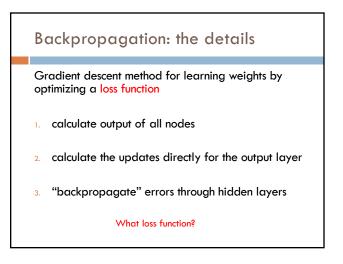
"backpropagate" the error:

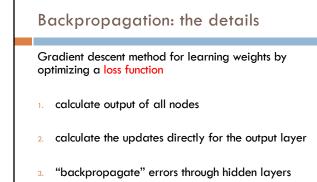
Assume all of these nodes were responsible for some of the error

How can we figure out how much they were responsible for?









 $loss = \sum_{x} \frac{1}{2} (y - \hat{y})^2$  squared error