

SORTING BASICS

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CS 62 – Spring 2021

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### Admin

Erin's office hours today 7-8pm (going forward)

My office hours today 3:30-4pm

Compression assignment hints/observations

2

### Sorting

What sorting algorithms have you seen before?

If I gave you a deck of cards and asked you to sort it, how would you do it?

3

### Sorting algorithms

Adaptive heapsort	Comb sort	Pancake sort
Bitonic sorter	Flashsort	<b>Quicksort</b>
Block sort	Gnome sort	Radix sort
Bubble sort	<b>Heapsort</b>	<b>Selection sort</b>
Bucket sort	<b>Insertion sort</b>	Shell sort
Cascade mergesort	Library sort	Spaghetti sort
Cocktail sort	<b>Mergesort</b>	<b>Treesort</b>

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## Selection sort

Divide the data into two parts: sorted and unsorted

Repeat:

5

## Selection sort

Divide the array into two parts: a sorted part on the left and an unsorted part on the right

Repeat:

- Find the smallest element in the unsorted part
- Swap it with the leftmost element of the unsorted array
- The sorted array is now one element larger

6

## Selection sort

3 44 38 5 47 1 36 26

sorted unsorted

Divide the array into two parts: a sorted part on the left and an unsorted part on the right

Repeat:

- Find the smallest element in the unsorted part
- Swap it with the leftmost element of the unsorted array
- The sorted array is now one element larger

7

## Selection sort

3 44 38 5 47 1 36 26

sorted unsorted

Smallest?

Divide the array into two parts: a sorted part on the left and an unsorted part on the right

Repeat:

- Find the smallest element in the unsorted part
- Swap it with the leftmost element of the unsorted array
- The sorted array is now one element larger

8

### Selection sort

sorted    **unsorted**

---

Divide the array into two parts: a sorted part on the left and an unsorted part on the right

Repeat:

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9

### Selection sort

sorted    **unsorted**

---

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Repeat:

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10

### Selection sort

sorted    **unsorted**                      **Smallest?**

---

Divide the array into two parts: a sorted part on the left and an unsorted part on the right

Repeat:

- Find the smallest element in the unsorted part
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- The sorted array is now one element larger

11

### Selection sort

sorted    **unsorted**                      **Smallest?**

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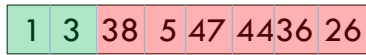
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12

## Selection sort



sorted unsorted

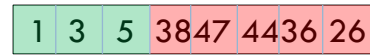
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13

## Selection sort



sorted unsorted

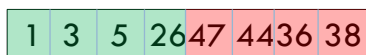
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14

## Selection sort



sorted unsorted

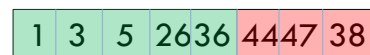
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15

## Selection sort



sorted unsorted

Divide the array into two parts: a sorted part on the left and an unsorted part on the right

Repeat:

- Find the smallest element in the unsorted part
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- The sorted array is now one element larger

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## Running time to find the smallest element

Best case?

Worst case?

Average case?

Divide the array into two parts: a sorted part on the left and an unsorted part on the right

Repeat:

- Find the smallest element in the unsorted part
- Swap it with the leftmost element of the unsorted array
- The sorted array is now one element larger

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## Running time to find the smallest element

All cases: `size_of_unsorted_array` – we have to search through the entire unsorted array to find it

Divide the array into two parts: a sorted part on the left and an unsorted part on the right

Repeat:

- Find the smallest element in the unsorted part
- Swap it with the leftmost element of the unsorted array
- The sorted array is now one element larger

18

## Overall runtime

3	44	38	5	47	1	36	26
---	----	----	---	----	---	----	----

sorted unsorted

`size_of_unsorted_array`

How big is this for the first iteration?

19

## Overall runtime

3	44	38	5	47	1	36	26
---	----	----	---	----	---	----	----


sorted unsorted

`size_of_unsorted_array`

How big is this for the first iteration? `n`

20

Overall runtime



1	44	38	5	47	3	36	26
---	----	----	---	----	---	----	----


sorted    **unsorted**

size\_of\_unsorted\_array

How big is this for the second iteration?

21

Overall runtime



1	44	38	5	47	3	36	26
---	----	----	---	----	---	----	----


sorted    **unsorted**

size\_of\_unsorted\_array

How big is this for the second iteration?  $n-1$

22

Overall runtime



1	3	5	38	47	44	36	26
---	---	---	----	----	----	----	----


sorted    **unsorted**

size\_of\_unsorted\_array

How big is this for the second iteration?

23

Overall runtime



1	3	5	38	47	44	36	26
---	---	---	----	----	----	----	----

sorted    **unsorted**

size\_of\_unsorted\_array

How big is this for the second iteration?  $n-2$

24

### Overall runtime

1 3 5 38 47 44 36 26

sorted          unsorted

size\_of\_unsorted\_array

How big is this for the last iteration?

25

### Overall runtime

1 3 5 26 36 38 44 47

sorted          unsorted

size\_of\_unsorted\_array

How big is this for the last iteration?    1

26

### Overall runtime

$$runtime = 1 + 2 + 3 + n - 2 + n - 1 + n = \sum_{i=1}^n i$$

Divide the array into two parts: a sorted part on the left and an unsorted part on the right

Repeat:

- Find the smallest element in the unsorted part
- Swap it with the leftmost element of the unsorted array
- The sorted array is now one element larger

27

### Overall runtime

$$runtime = \sum_{i=1}^n i \quad ?$$

Divide the array into two parts: a sorted part on the left and an unsorted part on the right

Repeat:

- Find the smallest element in the unsorted part
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28

## Overall runtime

$$runtime = \sum_{i=1}^n i = \frac{n(n+1)}{2}$$

Divide the array into two parts: a sorted part on the left and an unsorted part on the right

Repeat:

- Find the smallest element in the unsorted part
- Swap it with the leftmost element of the unsorted array
- The sorted array is now one element larger

29

## Overall runtime

$$runtime = \sum_{i=1}^n i = \frac{n(n+1)}{2} \quad O(?)$$

Divide the array into two parts: a sorted part on the left and an unsorted part on the right

Repeat:

- Find the smallest element in the unsorted part
- Swap it with the leftmost element of the unsorted array
- The sorted array is now one element larger

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## Selection sort: overall runtime

$$runtime = \sum_{i=1}^n i = \frac{n(n+1)}{2} \quad O(n^2)$$

Divide the array into two parts: a sorted part on the left and an unsorted part on the right

Repeat:

- Find the smallest element in the unsorted part
- Swap it with the leftmost element of the unsorted array
- The sorted array is now one element larger

31

## Insertion sort

3	44	38	5	47	1	36	26
---	----	----	---	----	---	----	----

Divide the array into two parts:

left part: left elements in sorted order

right part: right elements in unsorted order

Repeat:

- Look at the next element in the unsorted part
- Find the correct location in the sorted part (by sliding each item right one at a time)
- The sorted array is now one element larger

32



### Insertion sort

sorted unsorted

---

Divide the array into two parts:  
 left part: left elements in sorted order  
 right part: right elements in unsorted order

Repeat:

- Look at the next element in the unsorted part
- Find the correct location in the sorted part (by sliding each item right one at a time)
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33

### Insertion sort

sorted unsorted

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Divide the array into two parts:  
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34

### Insertion sort

sorted unsorted

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Divide the array into two parts:  
 left part: left elements in sorted order  
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Repeat:

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35

### Insertion sort

sorted unsorted

---

Divide the array into two parts:  
 left part: left elements in sorted order  
 right part: right elements in unsorted order

Repeat:

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36

### Insertion sort

sorted                      unsorted                      Is 5 in the correct spot?

---

Divide the array into two parts:  
 left part: left elements in sorted order  
 right part: right elements in unsorted order

Repeat:

- Look at the next element in the unsorted part
- Find the correct location in the sorted part (by sliding each item right one at a time)
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37

### Insertion sort

sorted                      unsorted

---

Divide the array into two parts:  
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38

### Insertion sort

sorted                      unsorted                      Is 5 in the correct spot?

---

Divide the array into two parts:  
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39

### Insertion sort

sorted                      unsorted

---

Divide the array into two parts:  
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40

### Insertion sort

sorted                      unsorted                      Is 5 in the correct spot?

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Divide the array into two parts:  
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41

### Insertion sort

sorted                      unsorted

---

Divide the array into two parts:  
 left part: left elements in sorted order  
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Repeat:

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42

### Insertion sort

sorted                      unsorted

---

Divide the array into two parts:  
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Repeat:

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- Find the correct location in the sorted part (by sliding each item right one at a time)
- The sorted array is now one element larger

43

### Insertion sort

sorted                      unsorted                      Was that fast or slow?

---

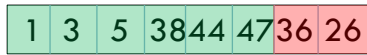
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44

## Insertion sort



sorted                      unsorted

Divide the array into two parts:  
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Repeat:

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- Find the correct location in the sorted part (by sliding each item right one at a time)
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45

## Insertion sort



sorted                      unsorted

Was that fast or slow?

Divide the array into two parts:  
left part: left elements in sorted order  
right part: right elements in unsorted order

Repeat:

- Look at the next element in the unsorted part
- Find the correct location in the sorted part (by sliding each item right one at a time)
- The sorted array is now one element larger

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## Running time to find the correct spot

Best case?

Worst case?

Average case?

Divide the array into two parts:  
left part: left elements in sorted order  
right part: right elements in unsorted order

Repeat:

- Look at the next element in the unsorted part
- Find the correct location in the sorted part (by sliding each item right one at a time)
- The sorted array is now one element larger

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## Running time to find the correct spot

Best case:  $O(1)$ , it's larger than any element to the left

Worst case:  $\text{size\_sorted\_part}$ , it's smaller than any element to the left

Average case:  $\text{size\_sorted\_part}/2$

Divide the array into two parts:  
left part: left elements in sorted order  
right part: right elements in unsorted order

Repeat:

- Look at the next element in the unsorted part
- Find the correct location in the sorted part (by sliding each item right one at a time)
- The sorted array is now one element larger

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## Insertion sort: overall runtime

Best case? When does this happen?

Worst case? When does this happen?

Average case?

Divide the array into two parts:

left part: left elements in sorted order

right part: right elements in unsorted order

Repeat:

- Look at the next element in the unsorted part
- Find the correct location in the sorted part (by sliding each item right one at a time)
- The sorted array is now one element larger

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## Overall runtime

Best case:  $O(n)$ , the array is already sorted

Worst case:  $O(n^2)$ , the array is reverse sorted (same sum as before)

Average case:  $O(n^2)$ ,  $n$  iterations and still have to move  $n/2$  entries on average

Divide the array into two parts:

left part: left elements in sorted order

right part: right elements in unsorted order

Repeat:

- Look at the next element in the unsorted part
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50