

Admin

Lab tomorrow

- □ Midterm recap (save questions for then)
- Course feedback discussion
- □ Start next assignment (2 week assignment)

Quiz on Thursday

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	Hashtables
	<pre>public interface Set<e> { public void put(E key); public boolean containsKey(E key); public E remove(E key); public boolean isEmpty(); public int size(); }</e></pre>
	Using an array is still a good idea
	Key idea: need to translate from the key into an index in the array
	Array will will will will will a will 5 will 7 will will will will will will wi
5	





































What makes a good hash function?

- $\hfill\square$ Approximates the assumption of simple uniform hashing
- Deterministic h(x) should always return the same value
- Low cost if it is expensive to calculate the hash value (e.g. log n) then we don't gain anything by using a table

Challenge: we don't generally know the distribution of the keys

Frequently data tend to be clustered (e.g. similar strings, run-times, SSNs). A good hash function should spread these out across the table

Division method				
h(k) = k mo	od m			
_	m	k	h(k)	
	11	25		
	11	1		
	11	17		
	13	133		
	13	7		
	13	25		

Division method			
h(k) = k mod m			
	m	k	h(k)
	11	25	3
	11	1	1
	11	17	6
	13	133	3
	13	7	7
	13	25	12

Division method Don't use a power of two. Why?							
	m k	bin(k)	h(k)				
	8 25	11001	1				
	8 1	00001	1				
	8 17	10001	1				
if $h(k) = k \mod 2^p$, the hash function is just the lower p bits of the value							

Division method
Good rule of thumb for <i>m</i> is a prime number not too close to a power of 2
Pros: quick to calculate easy to understand
Cons:

• keys close to each other will end up close in the hashtable

Division method

m k 8 25

8 1

8 17

Don't use a power of two. Why?

bin(k)

11001

00001

10001

h(k)

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h(k)

Mul	Multiplication method					
m	k	A	kA	h(k)		
8	15	0.618	9.27	floor(0.27*8) = 2		
8	23	0.618	14.214	floor(0.214*8) = 1		
8	100	0.618	61.8	floor(0.8*8) = 6		
$h(k) = \lfloor m(kA - \lfloor kA \rfloor) \rfloor$						

Multiplication method

Why a power of 2?

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Book has other heuristics

 $h(k) = \lfloor m(kA - \lfloor kA \rfloor) \rfloor$

 $A = (\sqrt{5} - 1)/2 = 0.6180339887$

Common choice is for m as a power of 2 and

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The hash function takes an additional parameter i which is the

slots to examine when a put or containsKey

number of collisions that have already occurred

The probe sequence **must** be a permutation of every hashtable entry. Why?

{ h(k,0), h(k,1), h(k,2), ..., h(k, m-1) } is a permutation of { 0, 1, 2, 3, ..., m-1 }















Open addressing: put public void put(E key) { [int i = 0; int next = probeSequence(key, i); while(i < table.length && table[next] != null){ i++; next = probeSequence(key, i); } table[next] = key; count++; }



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Open addressing: containsKey

// only 3 ways to exit the while loop
// the two of which below mean we didn't find it
return !(i == table.length || table[next] == null);

public boolean containsKey(E key){
 int i = 0;
 int next = probeSequence(key, i);

}

we got to a null entry

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while(i < table.length &&
 table[next] != null &&
 !table[next].equals(key)){
 i++;
 next = probeSequence(key, i);</pre>

return false if we searched the whole table or













Quadratic probing

 $h(k,i) = (h(k) + c_1i + c_2i^2) \mod m$

Rather than a linear sequence, we probe based on a quadratic function

Problems:

- must pick constants and *m* so that we have a proper probe sequence
- if h(x) = h(y), then h(x,i) = h(y,i) for all i
- secondary clustering

Double hashing

Probe sequence is determined by a second hash function

 $h(k,i) = (h_1(k) + i(h_2(k))) \mod m$

Problem:

• h2(k) must visit all possible positions in the table

Running time of put and containsKey for open addressing Depends on the hash function/probe sequence Worst case?

 $O(n)-probe sequence visits every full entry first before finding an empty % \label{eq:One}$

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How big should a hashtable be?

A good rule of thumb is the hashtable should be around half full

What happens when the hashtable gets full?

Copy: Create a new table and copy the values over

- results in one expensive put
- simple to implement

Amortized copy: When a certain ratio is hit, grow the table, but copy the entries over a few at a time with every insert

- no single put is expensive and can guarantee per put performance
- more complicated to implement

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To the code...

abstract classes!

Making your classes hashable:

- hashCode
- equals

HashSet:

HashMap:

https://docs.oracle.com/javase/8/docs/api/java/util/HashSet.html

https://docs.oracle.com/javase/8/docs/api/java/util/HashMap.html