

Lecture 21: Priority Queues & Heapsort

CS 62

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Priority Queues

A collection of entries that are inserted in such a way as to allow them to be dequeued in decreasing priority.

Entries can be either a pair of (key, value) or just values.
structure5 assumes the 2nd.

Lowest value has highest priority.

Examples: OS scheduler, ER, airport, etc.

Priority Queue ADT

```
public interface PriorityQueue<E extends Comparable<E>>{  
    public E remove(); //removes the element with smallest value  
    public E getFirst(); //fetches lowest valued item from queue  
    public void add(E value); //adds a value to the PQ  
    public boolean isEmpty();  
    public int size();  
    public void clear();  
}
```

Priority Queue implementations

1. As regular queue (array or linked list based) where either keep in order or search for lowest to remove:
 - One of add or remove will be $O(n)$
2. Heap representation (in arraylist) is more efficient:
 - $O(\log n)$ for both add and remove.
 - Insert into heap:
 - Place in next free position
 - "Percolate" it up.
 - Remove:
 - remove root
 - move last element in array up to root.
 - "Push" it down.
 - Peek element with highest priority in $O(1)$

VectorHeap

Class in structure5

Most heap operations, including insert and remove, execute in logarithmic time, but the minimum element can be returned in constant time.

PriorityQueue in standard Java

Treesort

- Build Binary search tree from the elements to be sorted (will cover later)
 - Adding one element is $O(\log n)$
 - Adding n elements is $O(n \log n)$
 - If tree is unbalanced, adding one element is $O(n)$, therefore worst case complexity $O(n^2)$
- Traverse the tree (in-order traversal) so that elements come out in sorted order
 - $O(n)$
- $O(n \log n)$ in best & average case and $O(n^2)$ in worst case
- Heapsort is always better!

HeapSort

- Make vector into a heap (depending on definition of priority max or min heap):
 - n insert operations = $O(n \log n)$
- Remove elements in order (the root since it contains smallest) and insert it into a sorted array. Keep updating heap
 - n remove operations = $O(n \log n)$
 - Total: $O(n \log n)$
- If clever can make into heap in $O(n)$ (1/2 vertices are leaves)
 - ... but still $O(n \log n)$ total.
 - $O(1)$ extra space (for swaps)
 - Not stable
- <https://visualgo.net/en/heap>

Comparing Sorts

- Quicksort:
 - fastest on average $O(n \log n)$, but worst case is $O(n^2)$
 - Takes $O(\log n)$ extra space
- Heapsort:
 - $O(n \log n)$ in average & worst case. No extra space.
 - A bit slower on average than quicksort and mergesort.
- Mergesort:
 - $O(n \log n)$ in average and worst case.
 - $O(n)$ extra space.
 - On-disk mergesort performs well on external files where not all fit in memory