

# SEARCH

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CS51A – Spring 2022

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## Admin

### Assignment 9

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## Search algorithm

Keep track of a list of states that we *could* visit, we'll call it "to\_visit"

General idea:

- ▣ take a state off the to\_visit list
- ▣ if it's the goal state
  - we're done!
- ▣ if it's not the goal state
  - Add all of the next states to the to\_visit list
- ▣ repeat

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## Search algorithms

add the start state to to\_visit

Repeat

- ▣ take a state off the to\_visit list
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Two variants: breadth first search (BFS) and depth first search (DFS) depending on whether we use a stack or a queue for to\_visit. Which is which?

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## Search algorithms

add the start state to `to_visit`

Repeat

- take a state off the `to_visit` list
- if it's the goal state
  - we're done!
- if it's not the goal state
  - Add all of the next states to the `to_visit` list

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Depth first search (DFS): `to_visit` is a stack  
 Breadth first search (BFS): `to_visit` is a queue

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## Implementing the state space

What the "world" (in this case a maze) looks like

- We'll define the world as a collection of *discrete* states
- States are connected if we can get from one state to another by taking a particular action
- This is called the "state space"

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## Implementing state space

What the "world" (in this case a maze) looks like

- We'll define the world as a collection of *discrete* states
- States are connected if we can get from one state to another by taking a particular action
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State:

- Is this the goal state? (`is_goal`)
- What states are connected to this state? (`next_states`)

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## Search variants implemented

add the start state to `to_visit`

Repeat

- take a state off the `to_visit` list
- if it's the goal state
  - we're done!
- if it's not the goal state
  - Add all of the successive states to the `to_visit` list

```
def dfs(start_state):
    s = Stack()
    return search(start_state, s)

def bfs(start_state):
    q = Queue()
    return search(start_state, q)

def search(start_state, to_visit):
    to_visit.add(start_state)

    while not to_visit.is_empty():
        current = to_visit.remove()

        if current.is_goal():
            return current
        else:
            for s in current.next_states():
                to_visit.add(s)

    return None
```

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What order would this variant visit the states?

```
def search(state):
    if state.is_goal():
        return state
    else:
        for s in state.next_states():
            result = search(s)
            if result != None:
                return result
        return None
```

1, 2, 5

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What order would this variant visit the states?

```
def search(state):
    if state.is_goal():
        return state
    else:
        for s in state.next_states():
            result = search(s)
            if result != None:
                return result
        return None
```

1, 2, 5, 3, 6, 9, 7, 8

What search algorithm is this?

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What order would this variant visit the states?

```
def search(state):
    if state.is_goal():
        return state
    else:
        for s in state.next_states():
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            if result != None:
                return result
        return None
```

1, 2, 5, 3, 6, 9, 7, 8

DFS!

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DFS with a stack

add the start state to to\_visit

Repeat

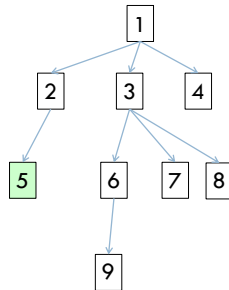
- take a state off the to\_visit list
- if it's the goal state
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- if it's not the goal state
  - Add all of the successive states to the to\_visit list

Depth first search (DFS): to\_visit is a stack  
Breadth first search (BFS): to\_visit is a queue

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## DFS with a stack

DFS: 1, 4, 3, 8, 7, 6, 9, 2, 5



Depth first search (DFS): to\_visit is a stack  
 Breadth first search (BFS): to\_visit is a queue

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## One last DFS variant

```

def search(state):
    if state.is_goal():
        return state
    else:
        for s in state.next_states():
            result = search(s)
            if result != None:
                return result
        return None

def dfs(state):
    if state.is_goal():
        return [state]
    else:
        result = []
        for s in state.next_states():
            result += dfs(s)
        return result
  
```

How is this different?

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## One last DFS variant

```

def search(state):
    if state.is_goal():
        return state
    else:
        for s in state.next_states():
            result = search(s)
            if result != None:
                return result
        return None

def dfs(state):
    if state.is_goal():
        return [state]
    else:
        result = []
        for s in state.next_states():
            result += dfs(s)
        return result
  
```

Returns ALL solutions found, not just one

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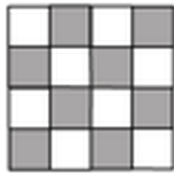
## Matrices!



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## N-queens problem

Place N queens on an N by N chess board such that none of the N queens are attacking any other queen.

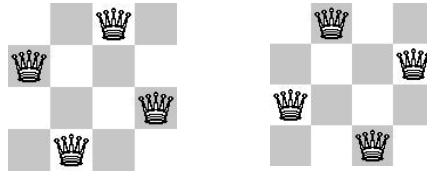


Solution(s)?

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## N-queens problem

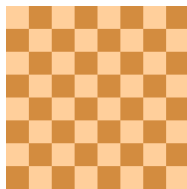
Place N queens on an N by N chess board such that none of the N queens are attacking any other queen.



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## N-queens problem

Place N queens on an N by N chess board such that none of the N queens are attacking any other queen.



Solution(s)?

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## N-queens problem

Place N queens on an N by N chess board such that none of the N queens are attacking any other queen.

How do we solve this with search:

What is a state?

What is the start state?

What is the goal?

How do we transition from one state to the next?

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## Search algorithm

add the **start state** to to\_visit

Repeat

- ▣ take a state off the to\_visit list
- ▣ if it's the **goal state** Is this a goal state?
  - we're done!
- ▣ if it's not the goal state What states can I get to from the current state?
  - Add all of the **next states to the** to\_visit list

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Any problem that we can define these three things  
can be plugged into the search algorithm!

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## N queens problem

[http://en.wikipedia.org/wiki/Eight\\_queens\\_puzzle](http://en.wikipedia.org/wiki/Eight_queens_puzzle)

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