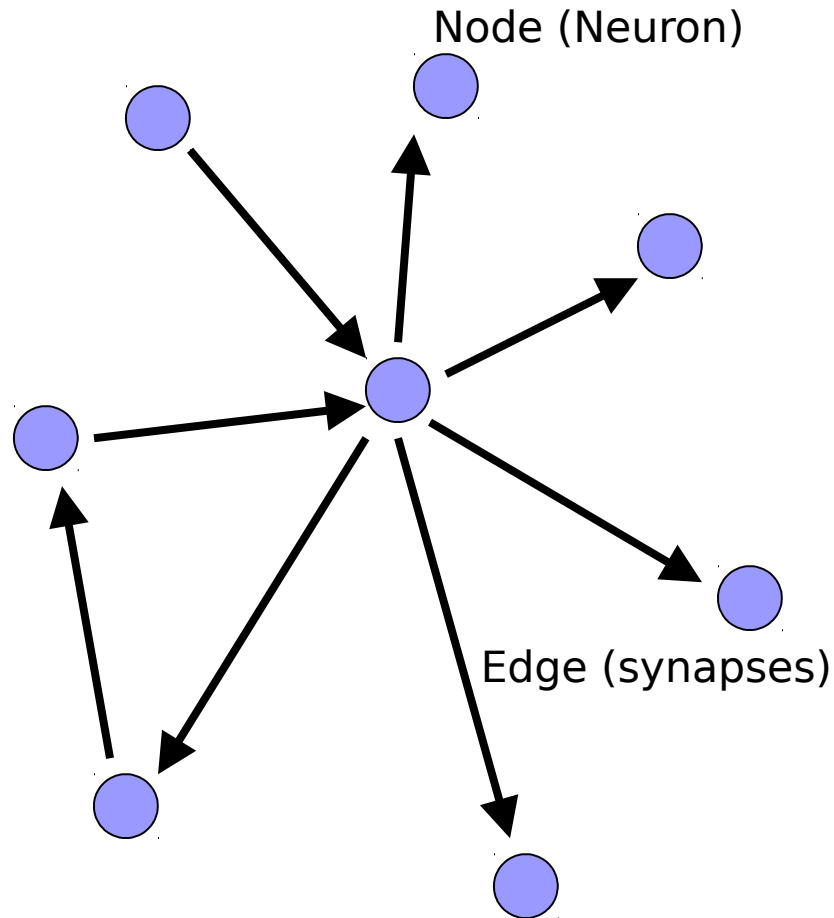


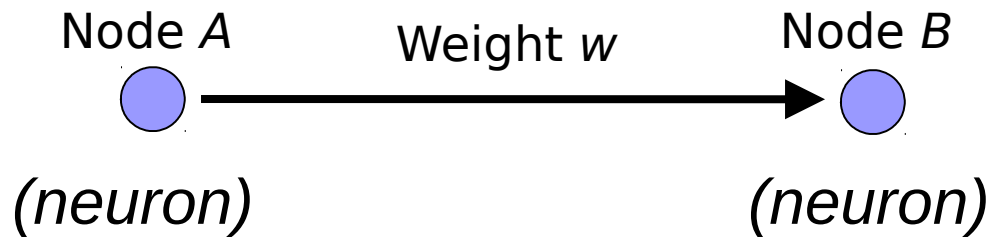
A decorative graphic on the left side of the slide consists of several overlapping squares in various shades of blue and purple, arranged in a roughly diagonal pattern. At the top of the slide, there is a horizontal bar with a gradient from light blue to white.

Perceptron Learning

David Kauchak/
Joseph C. Osborn
CSCI 051a
Fall 2019

Artificial Neural Networks



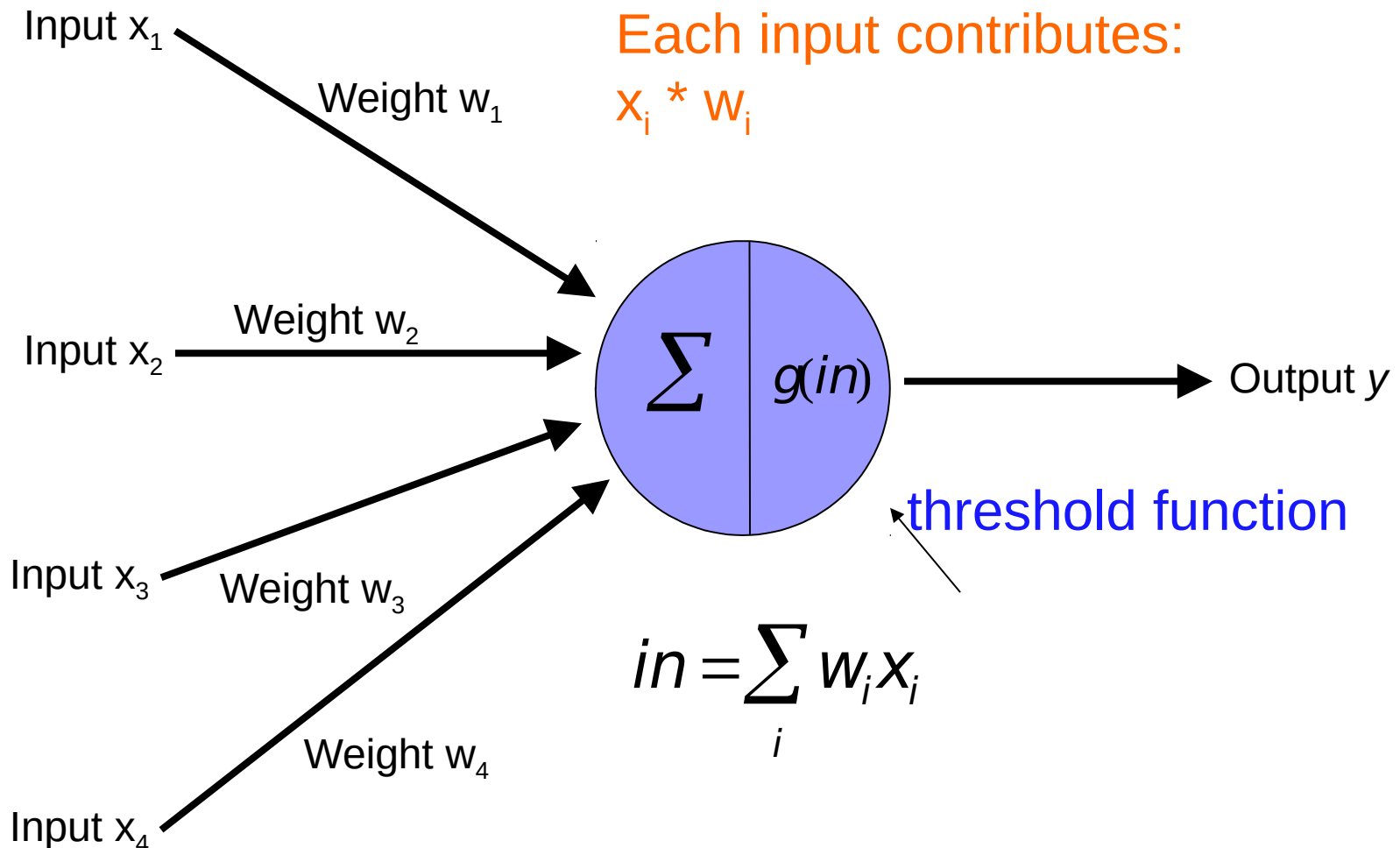


W is the strength of signal sent between A and B.

If A fires and w is **positive**, then A **stimulates** B.

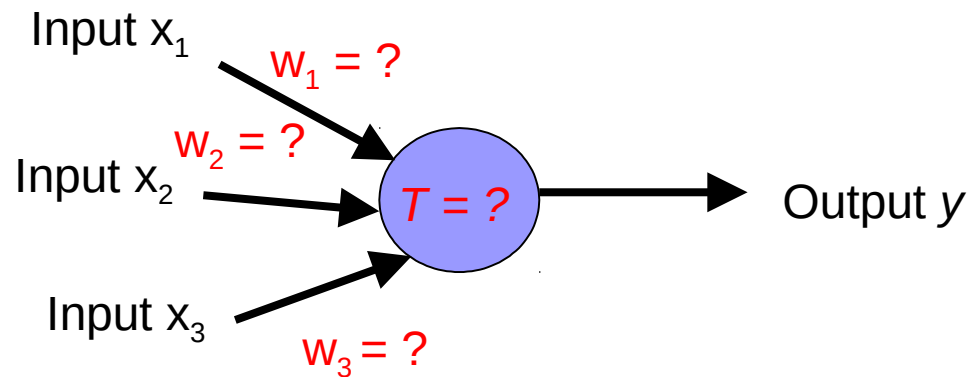
If A *fires* and w is **negative**, then A **inhibits** B.

A Single Neuron/Perceptron



Training neural networks

x_1	x_2	x_3	x_1 and x_2
0	0	0	1
0	1	0	0
1	0	0	1
1	1	0	0
0	0	1	1
0	1	1	1
1	0	1	1
1	1	1	0



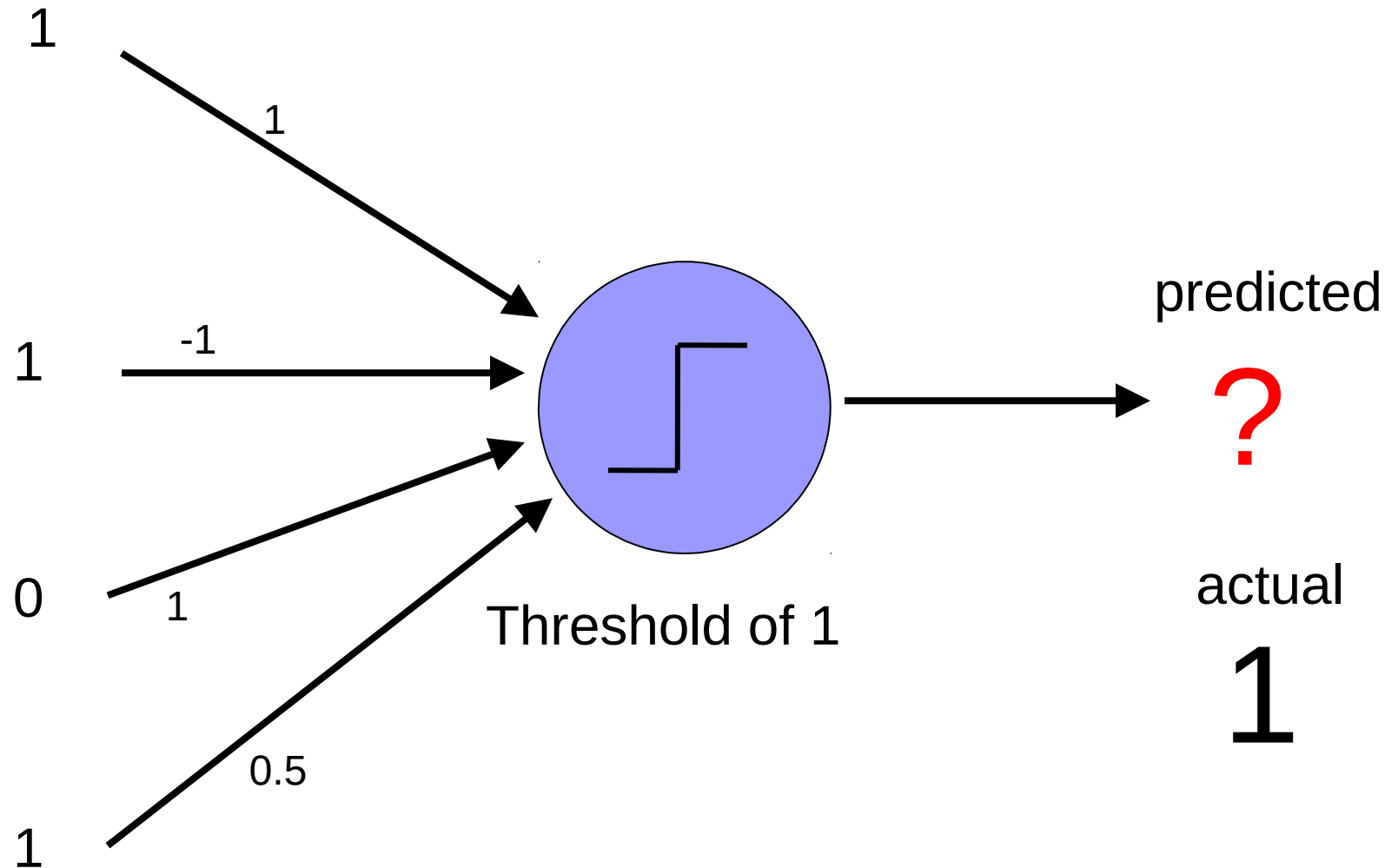
1. start with some initial weights and thresholds
2. show examples repeatedly to NN
3. update weights/thresholds by comparing NN output to actual output

Perceptron learning algorithm

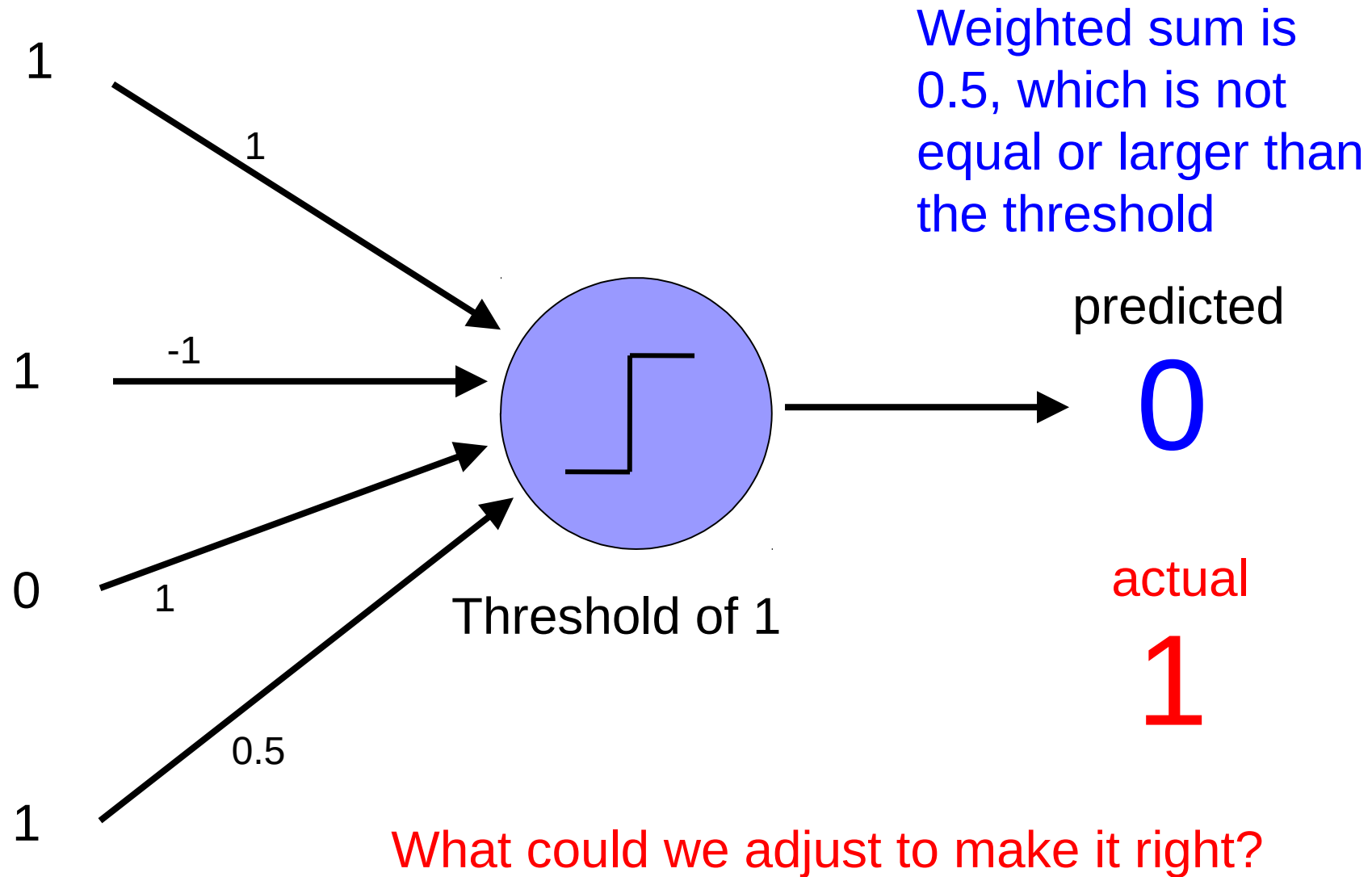
repeat until you get all examples right:

- for each “training” example:
 - calculate current prediction on example
 - if *wrong*:
 - update weights and threshold towards getting this example correct

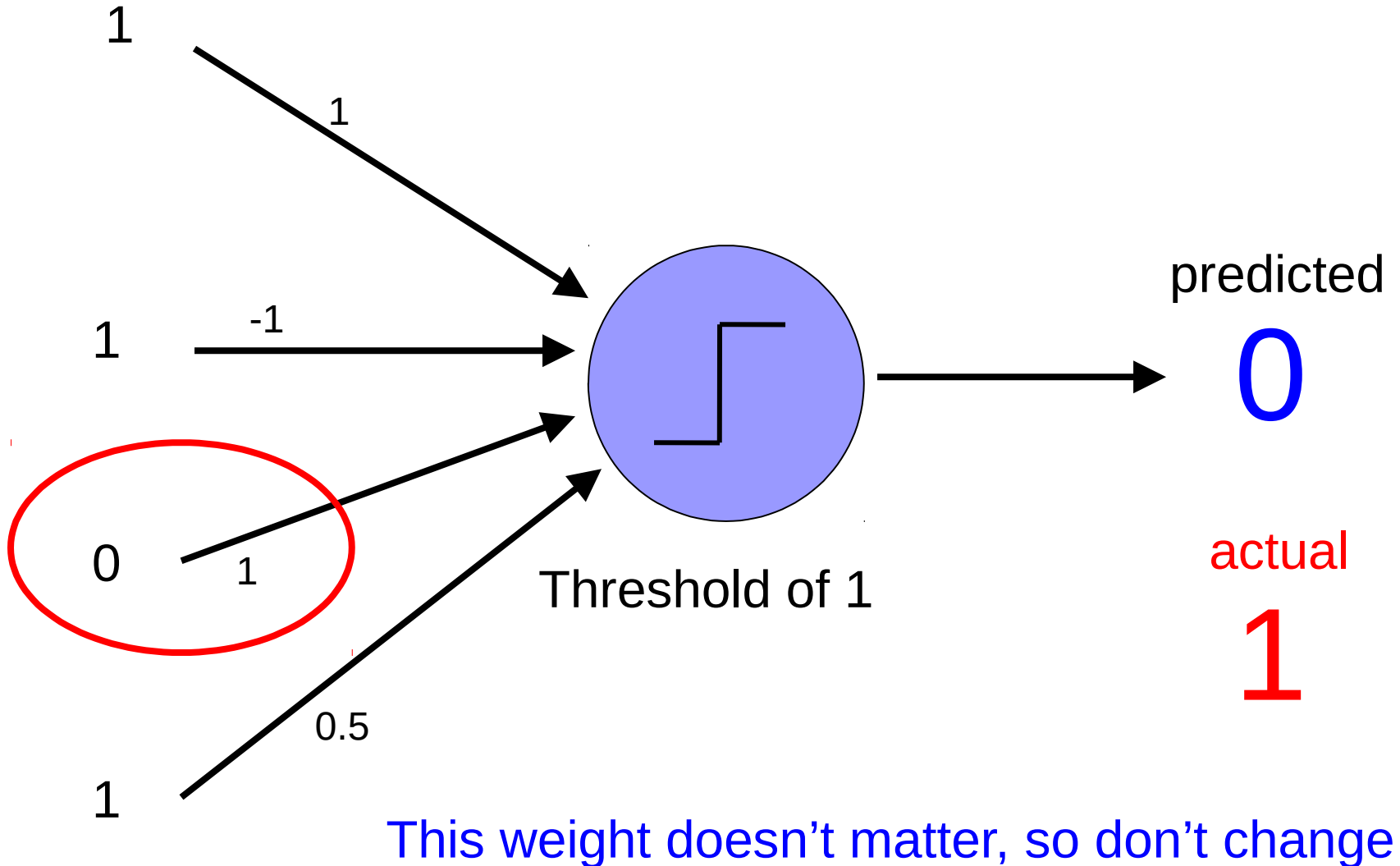
Perceptron learning



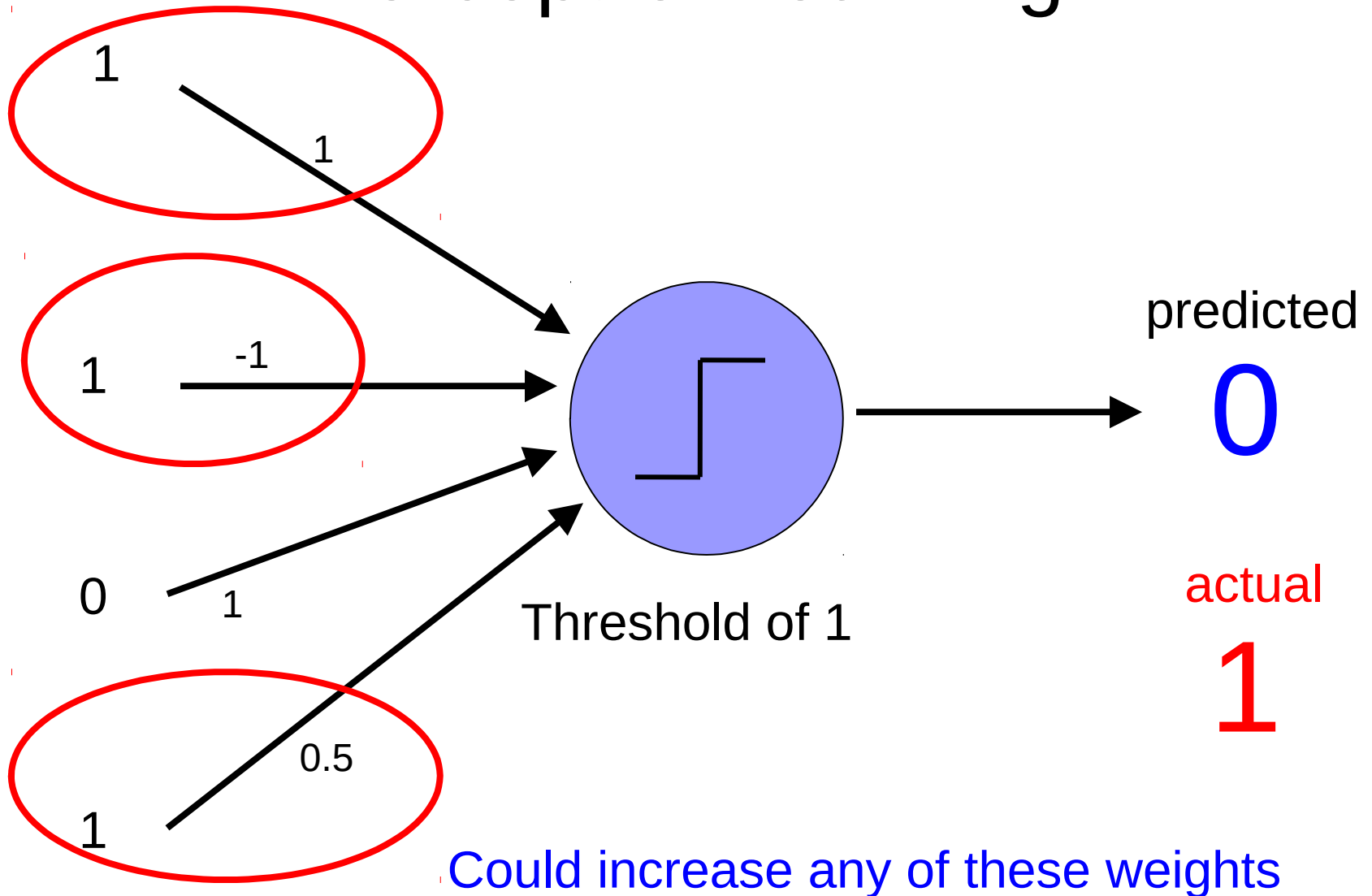
Perceptron learning



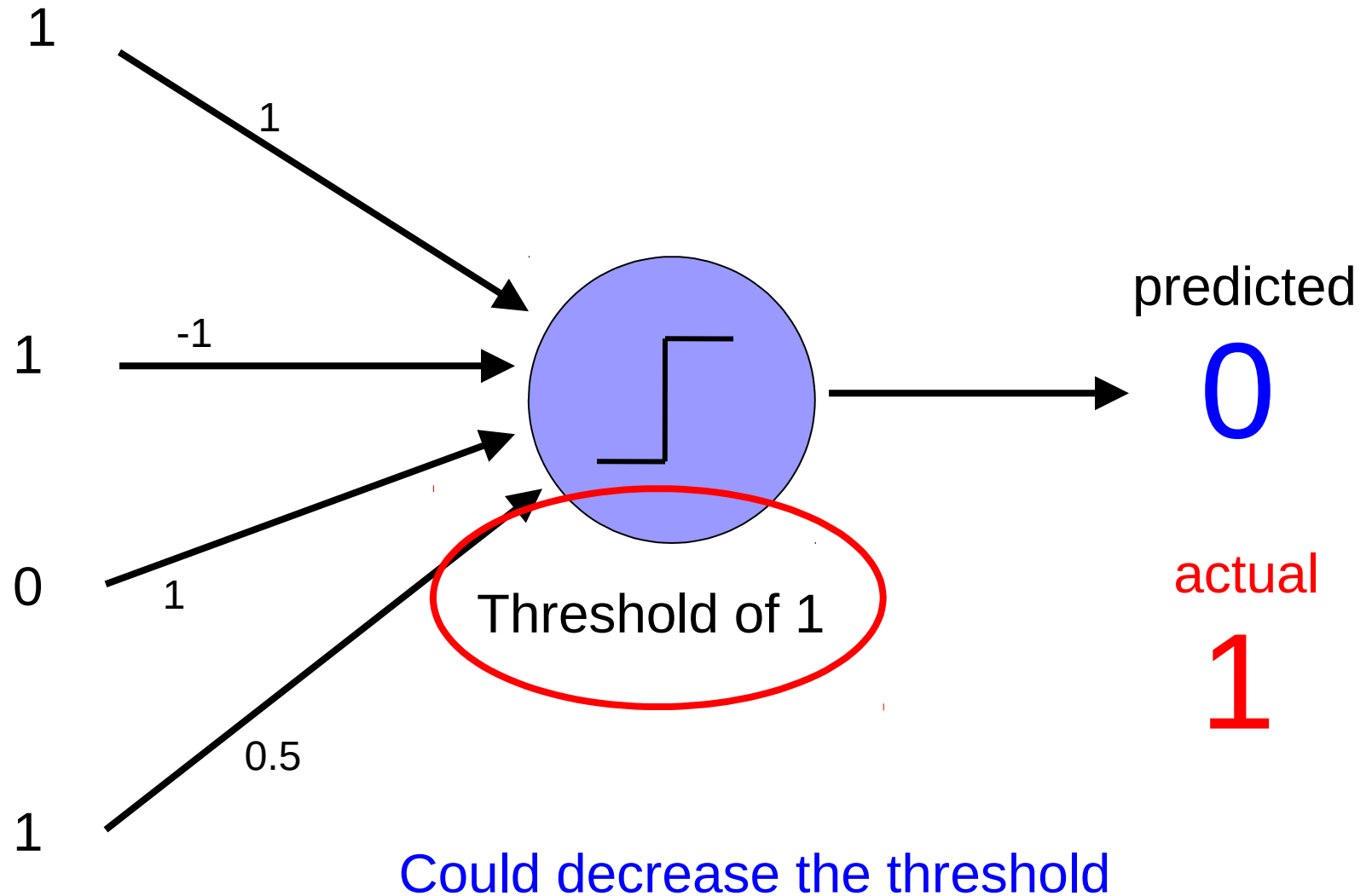
Perceptron learning



Perceptron learning

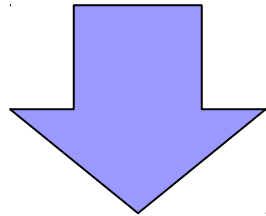


Perceptron learning



Perceptron update rule

- if *wrong*:
 - update weights and threshold towards getting this example correct

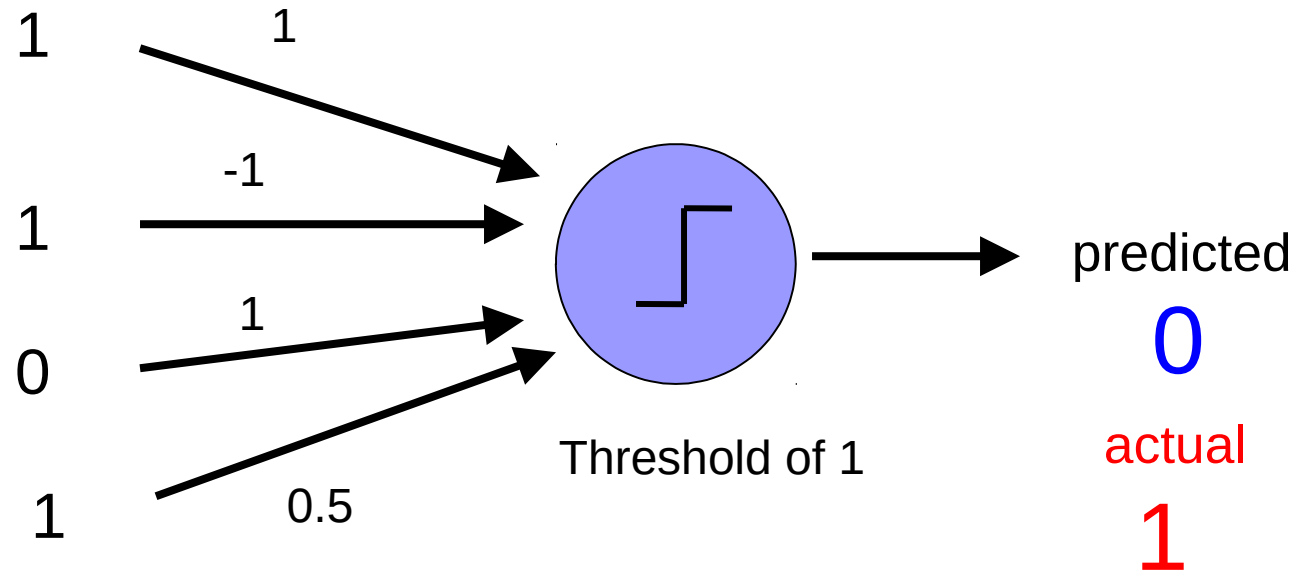


- if *wrong*:

$$w_i = w_i + \Delta w_i$$

$$\Delta w_i = \lambda * (\text{actual} - \text{predicted}) * x_i$$

Perceptron learning

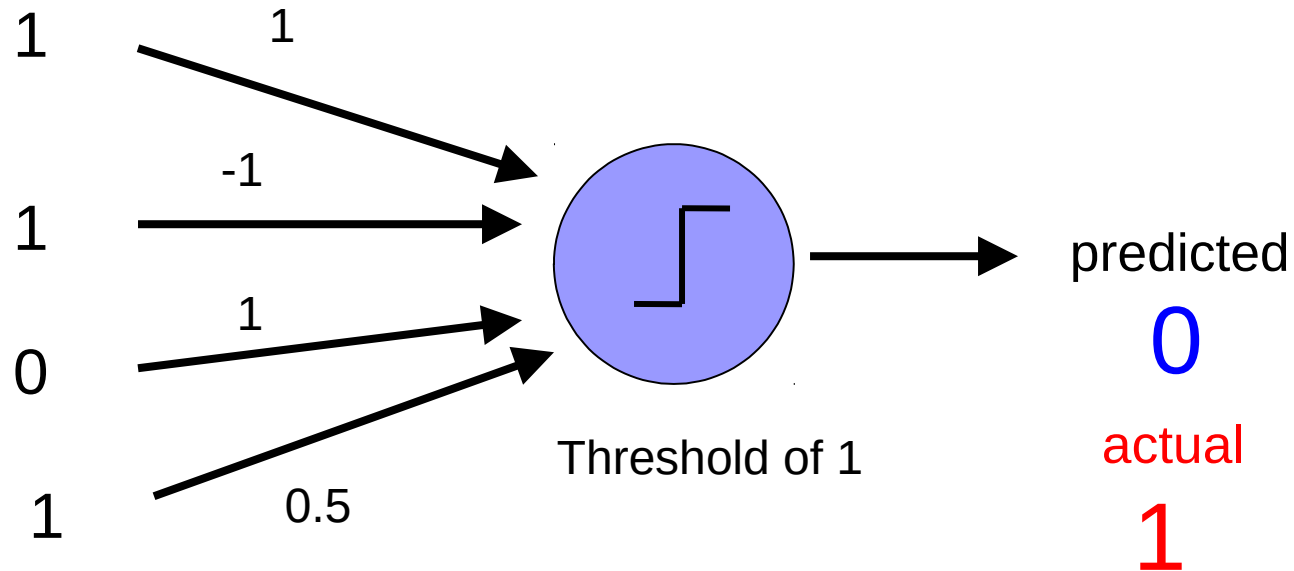


$$w_i = w_i + \Delta w_i$$

$$\Delta w_i = \lambda * (\text{actual} - \text{predicted}) * x_i$$

What does this do in this case?

Perceptron learning

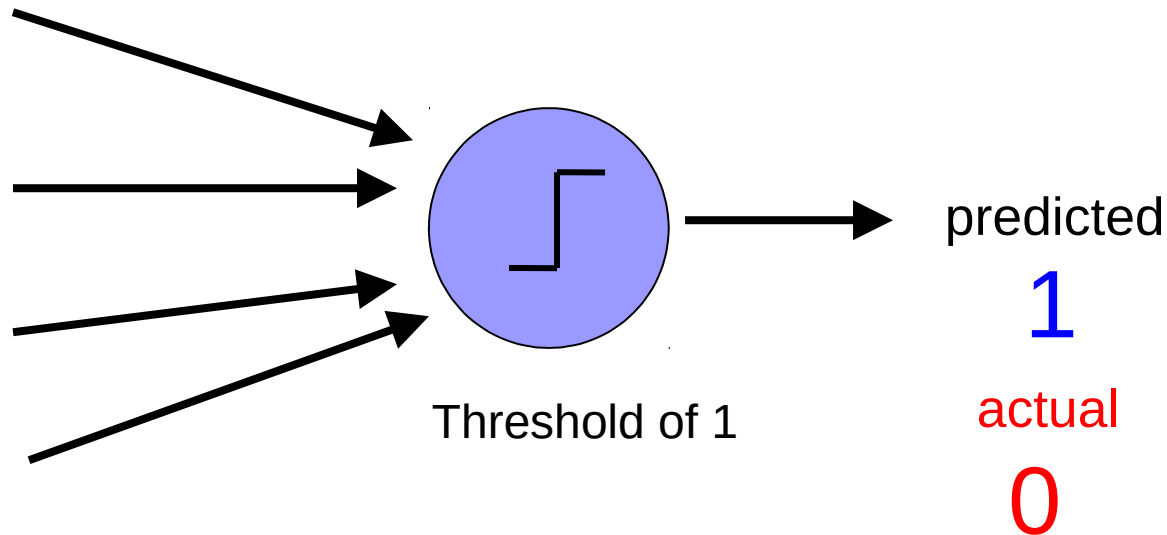


$$w_i = w_i + \Delta w_i$$

$$\Delta w_i = \lambda * (\text{actual} - \text{predicted}) * x_i$$

causes us to increase the weights!

Perceptron learning

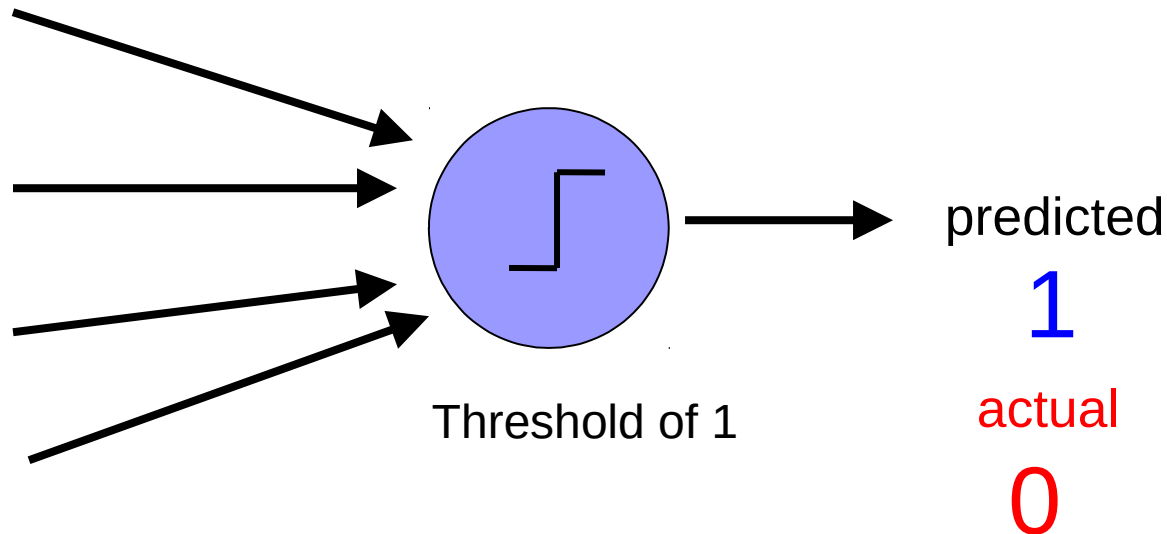


$$w_i = w_i + \Delta w_i$$

$$\Delta w_i = \lambda * \underbrace{(\text{actual} - \text{predicted})}_{\text{error}} * x_i$$

What if predicted = 1 and actual = 0?

Perceptron learning

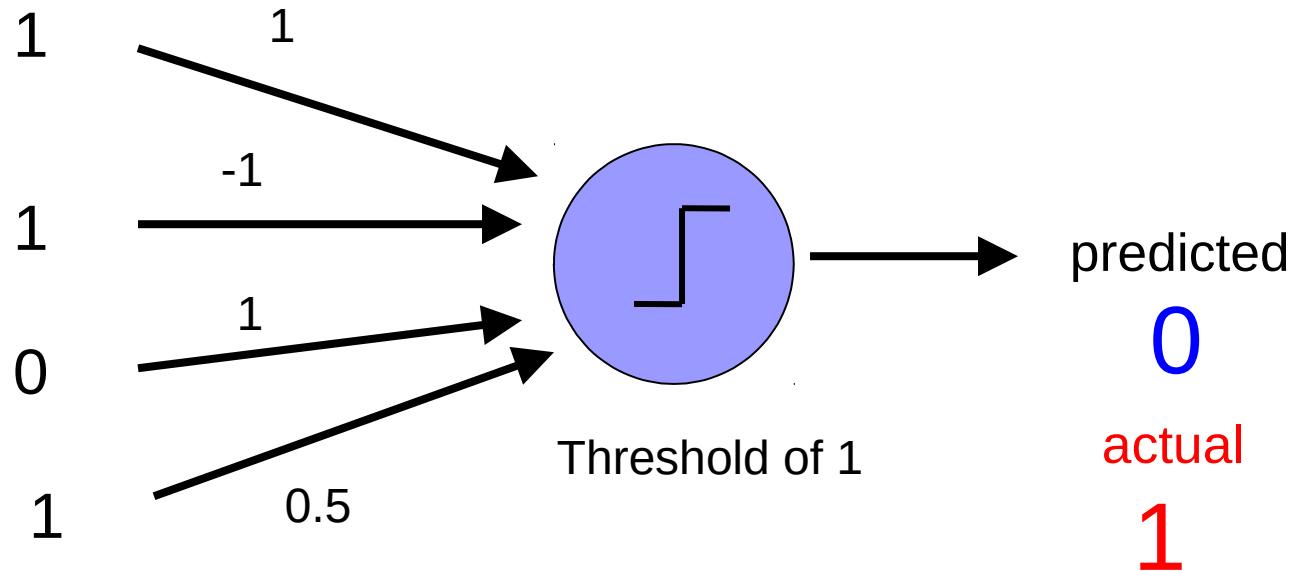


$$w_i = w_i + \Delta w_i$$

$$\Delta w_i = \lambda * \underbrace{(\text{actual} - \text{predicted})}_{-1} * x_i$$

We're over the threshold, so want to decrease weights:
actual - predicted = -1

Perceptron learning

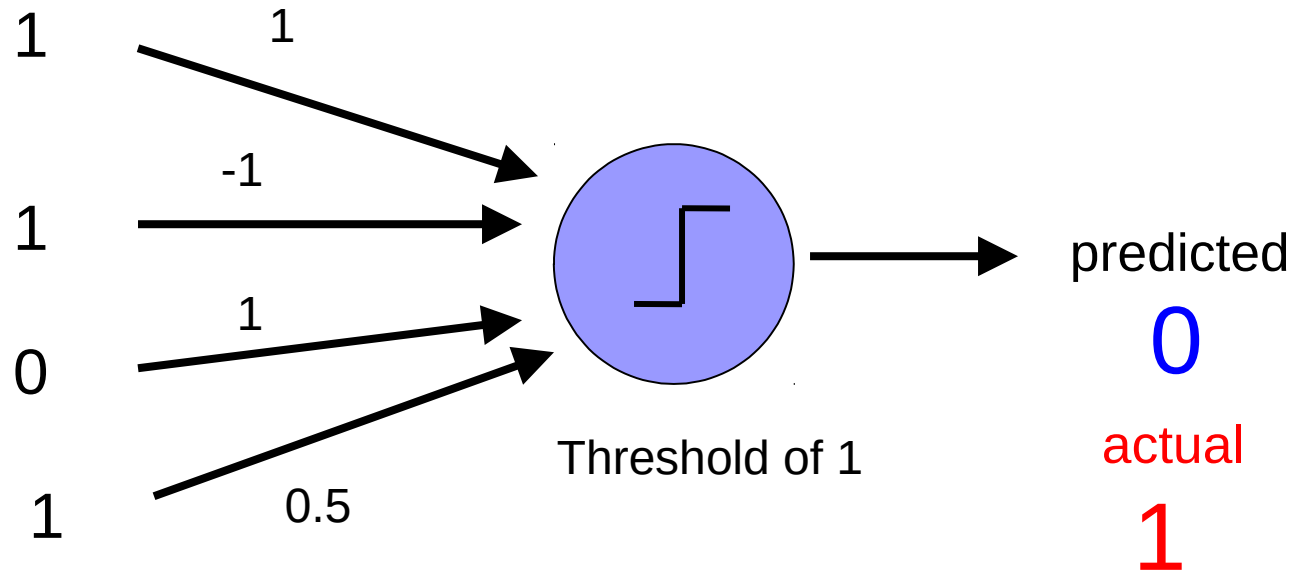


$$w_i = w_i + \Delta w_i$$

$$\Delta w_i = \lambda * (\text{actual} - \text{predicted}) * x_i$$

What does this do?

Perceptron learning

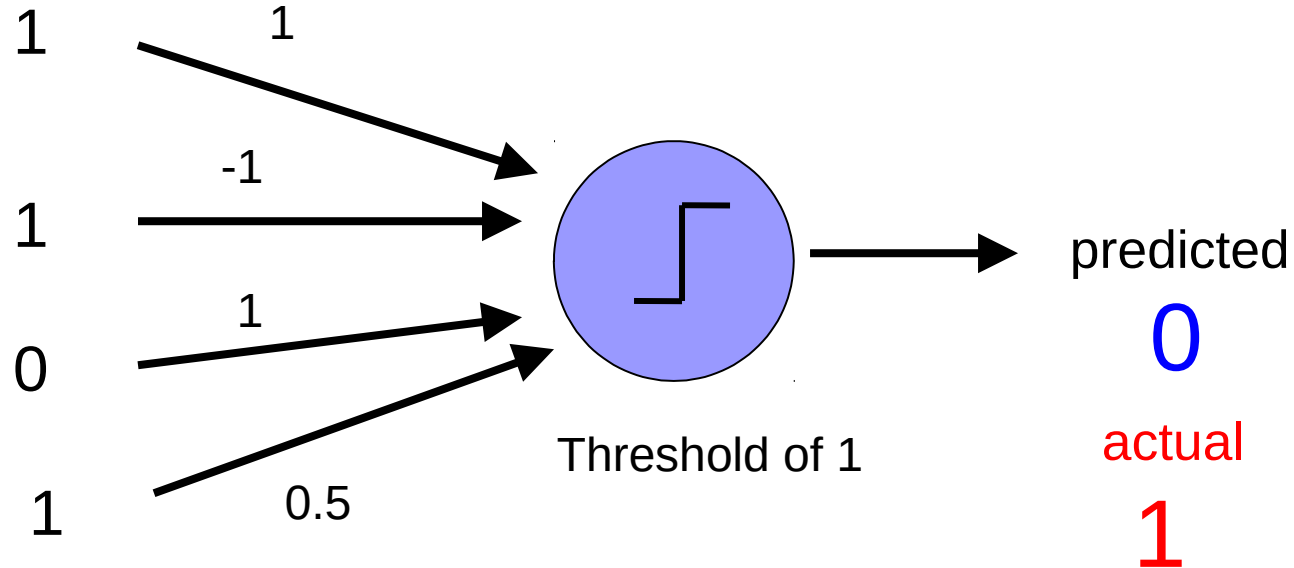


$$w_i = w_i + \Delta w_i$$

$$\Delta w_i = \lambda * (\text{actual} - \text{predicted}) * x_i$$

Only adjust those weights that actually contributed!

Perceptron learning

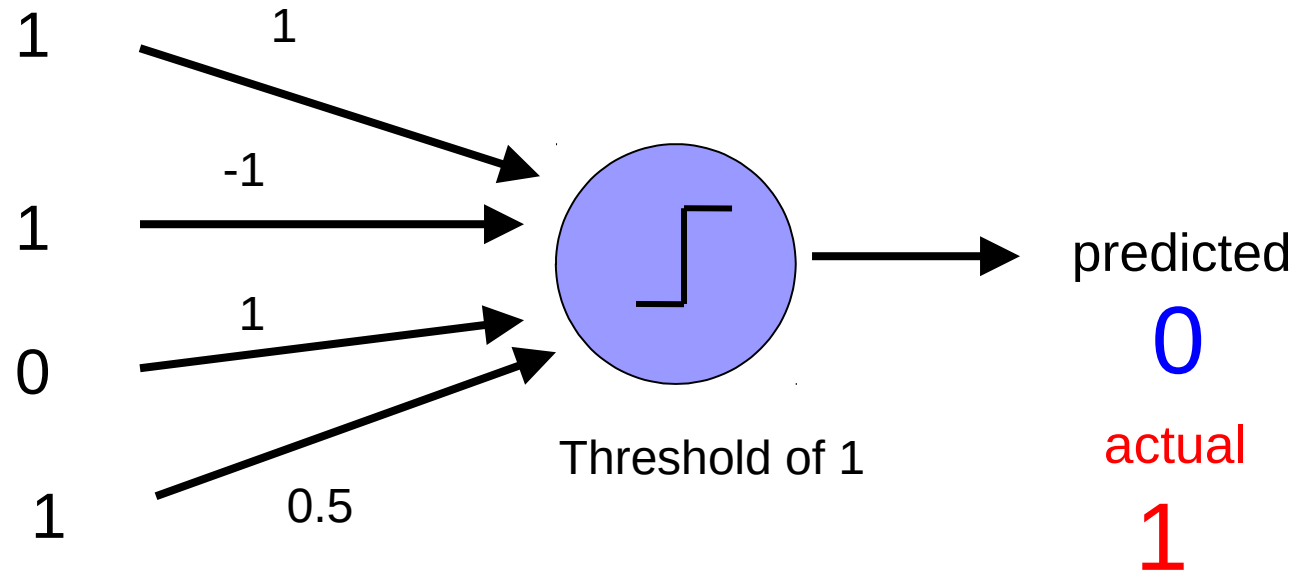


$$w_i = w_i + \Delta w_i$$

$$\Delta w_i = \lambda * (\text{actual} - \text{predicted}) * x_i$$

What does this do?

Perceptron learning

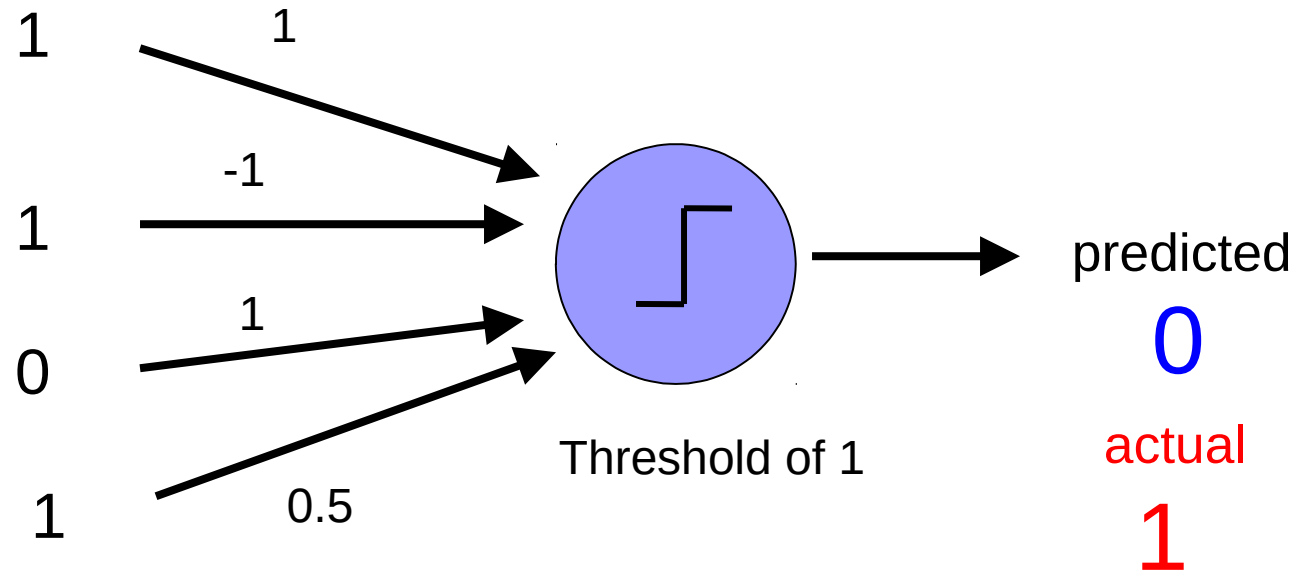


$$w_i = w_i + \Delta w_i$$

$$\Delta w_i = \lambda * (\text{actual} - \text{predicted}) * x_i$$

“learning rate”: value between 0 and 1 (e.g 0.1)
adjusts how abrupt the changes are to the model

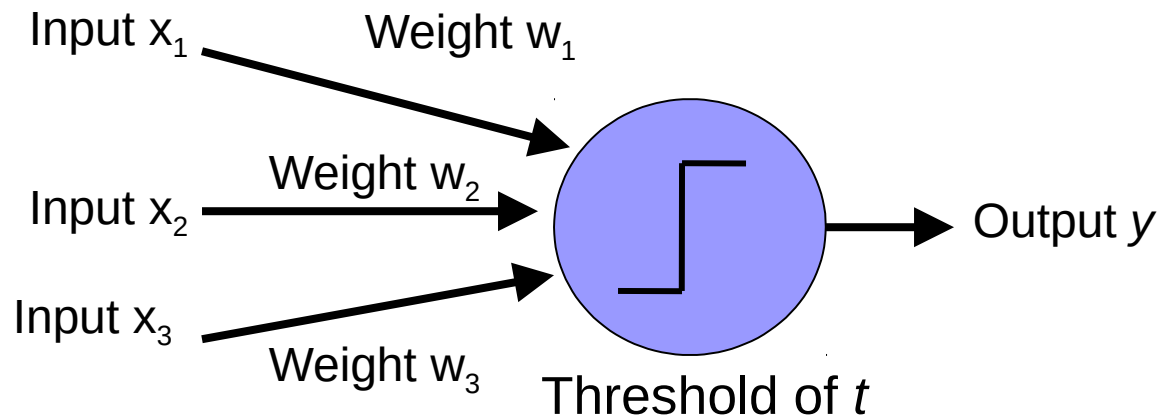
Perceptron learning



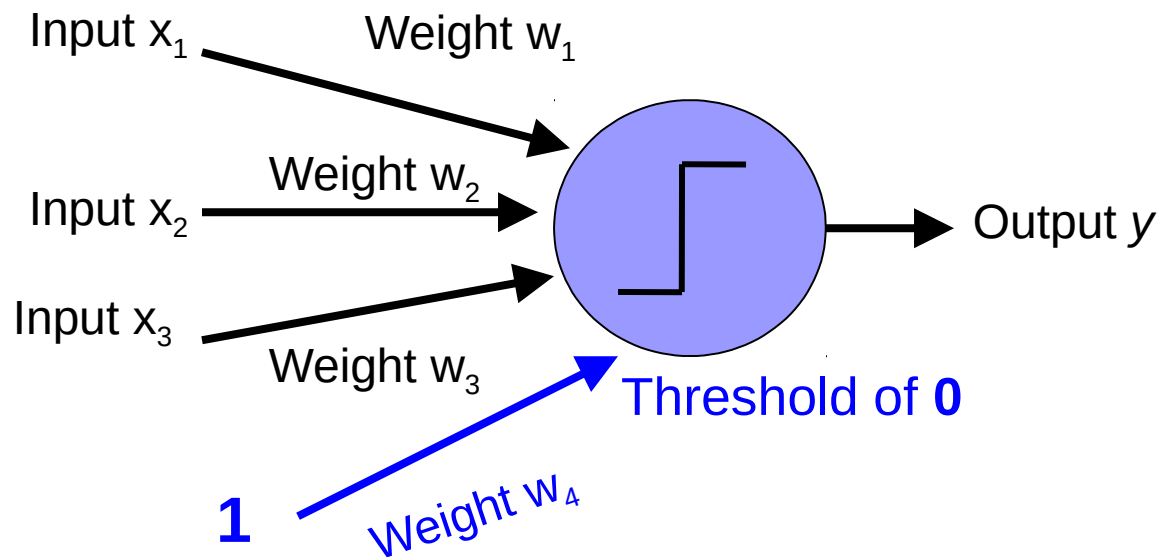
$$w_i = w_i + \Delta w_i$$

$$\Delta w_i = \lambda * (\text{actual} - \text{predicted}) * x_i$$

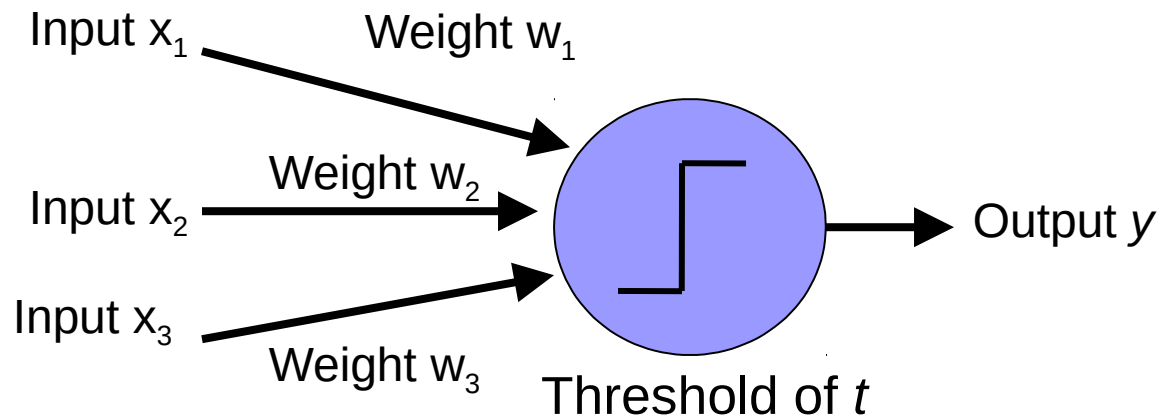
What about the threshold?



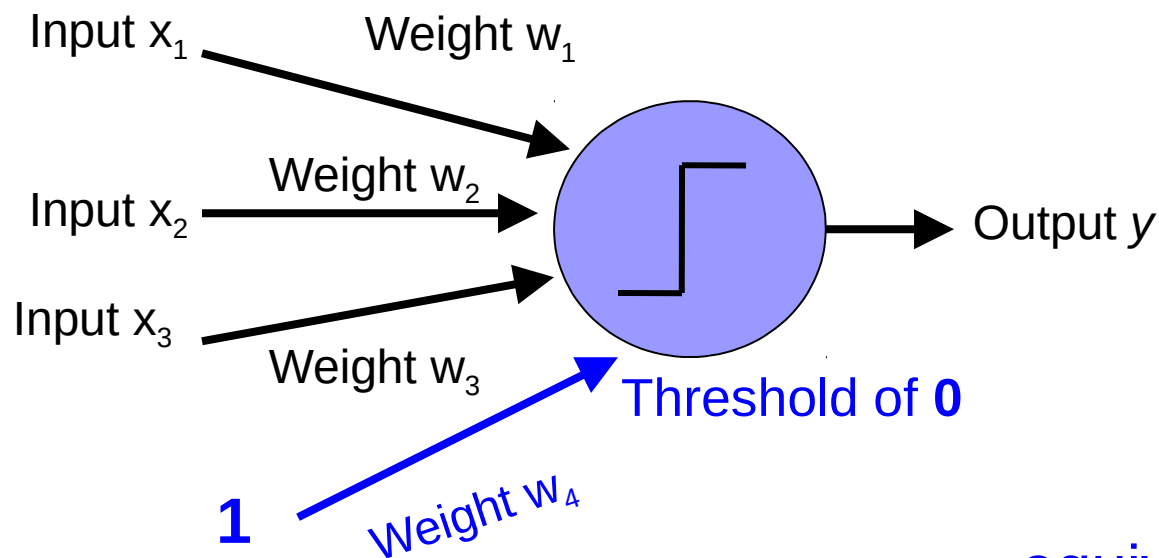
$$1 \text{ if } \sum_{i=1}^3 w_i x_i \geq t$$



$$1 \text{ if } w_4 + \sum_{i=1}^3 w_i x_i \geq 0$$



$$1 \text{ if } \sum_{i=1}^3 w_i x_i \geq t$$



$$1 \text{ if } w_4 + \sum_{i=1}^3 w_i x_i \geq 0$$

equivalent when $w_4 = -t$

Perceptron learning algorithm

initialize weights of the model randomly

repeat until you get all examples right:

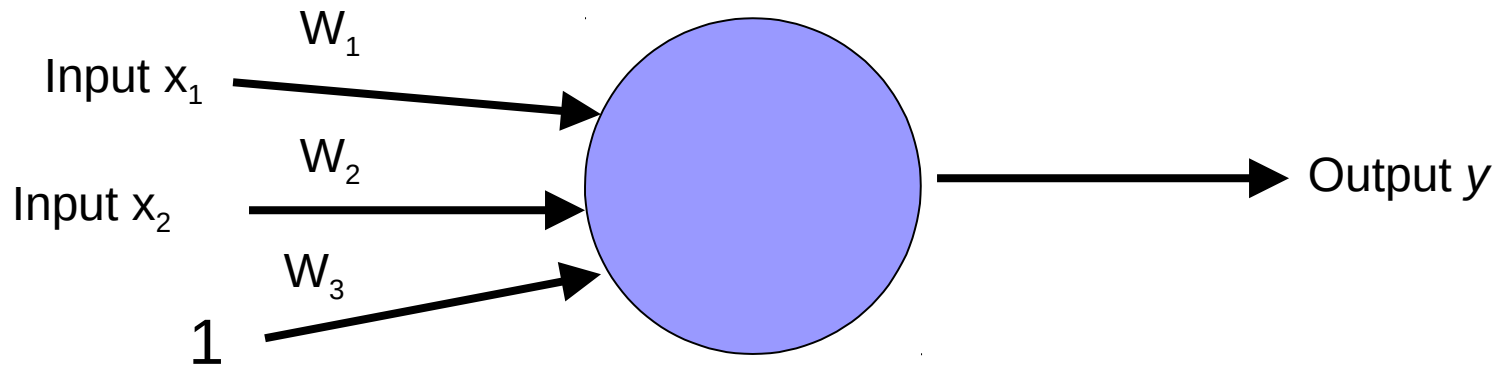
- for each “training” example (*in a random order*):
 - calculate current prediction on the example
 - if *wrong*:

$$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$$

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

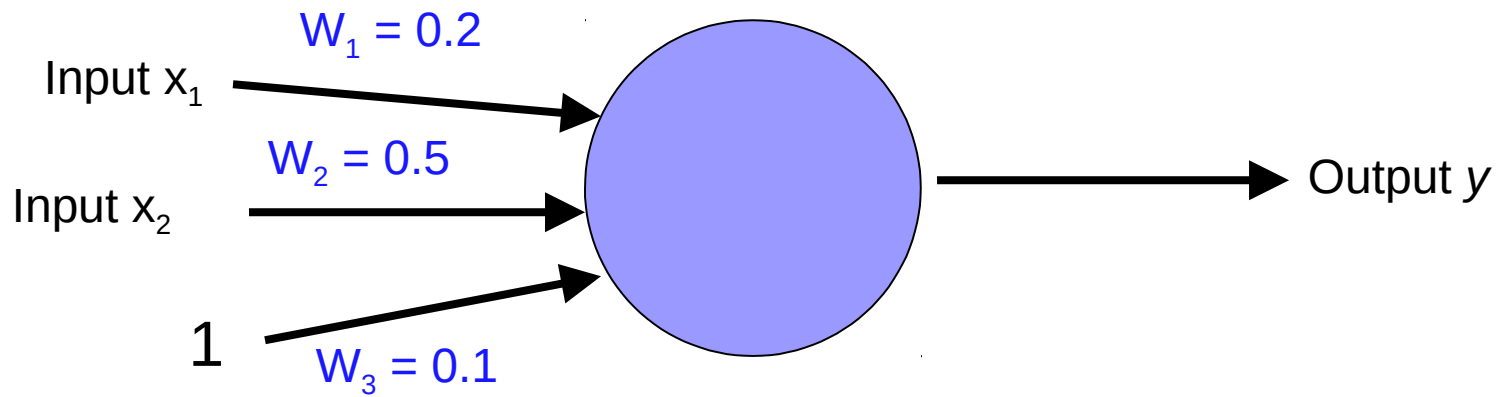
$$\lambda = 0.1$$

initialize with random weights



x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$$\lambda = 0.1$$

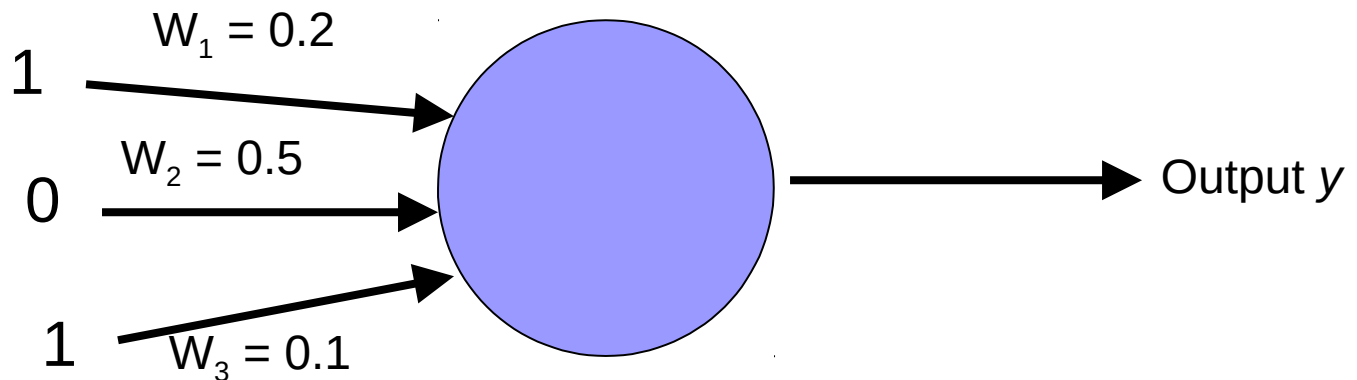


x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$$\lambda = 0.1$$

if wrong:

$$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$$



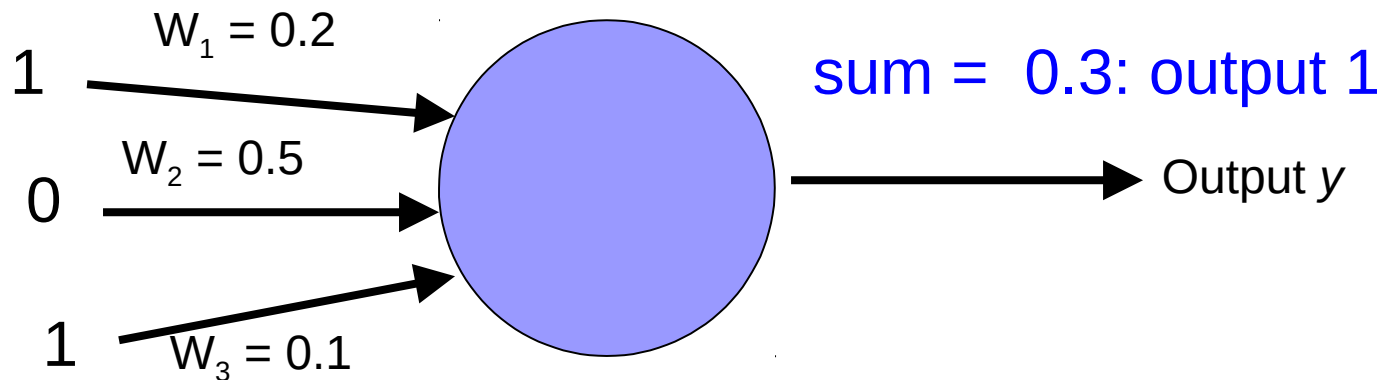
Right or wrong?

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$$\lambda = 0.1$$

if wrong:

$$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$$



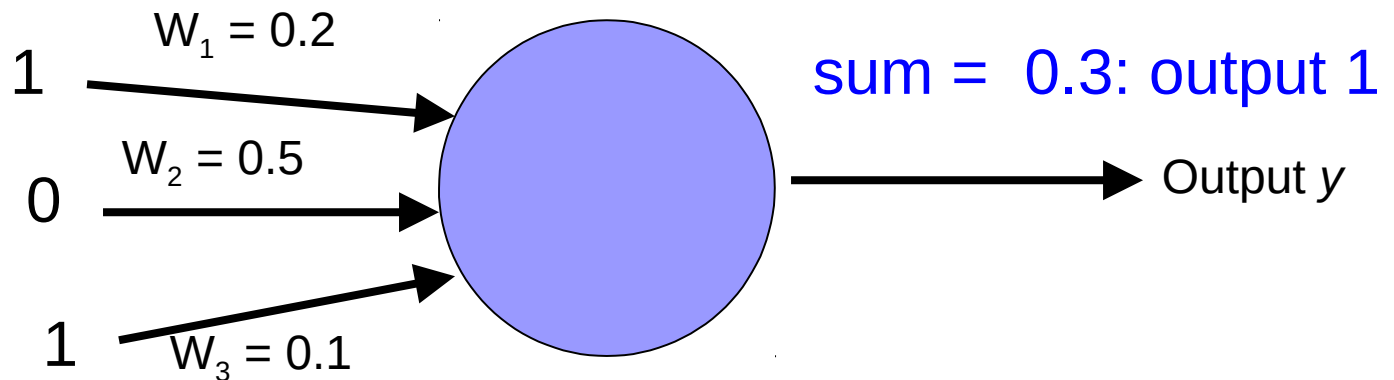
Wrong

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$$\lambda = 0.1$$

if wrong:

$$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$$



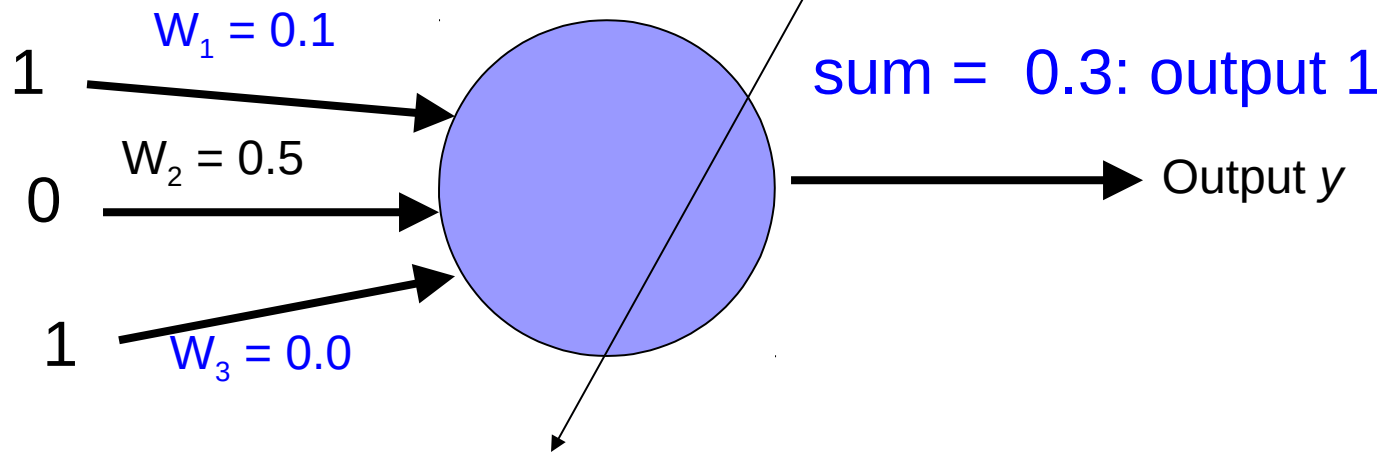
new weights?

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$\lambda = 0.1$

if wrong:

$$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$$



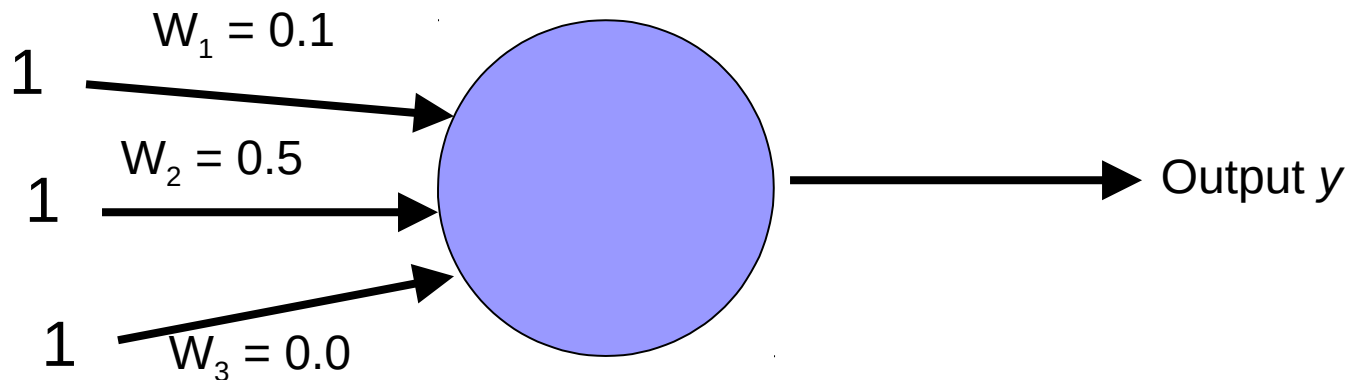
decrease $(0-1=-1)$ all non-zero x_i by 0.1

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$$\lambda = 0.1$$

if wrong:

$$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$$



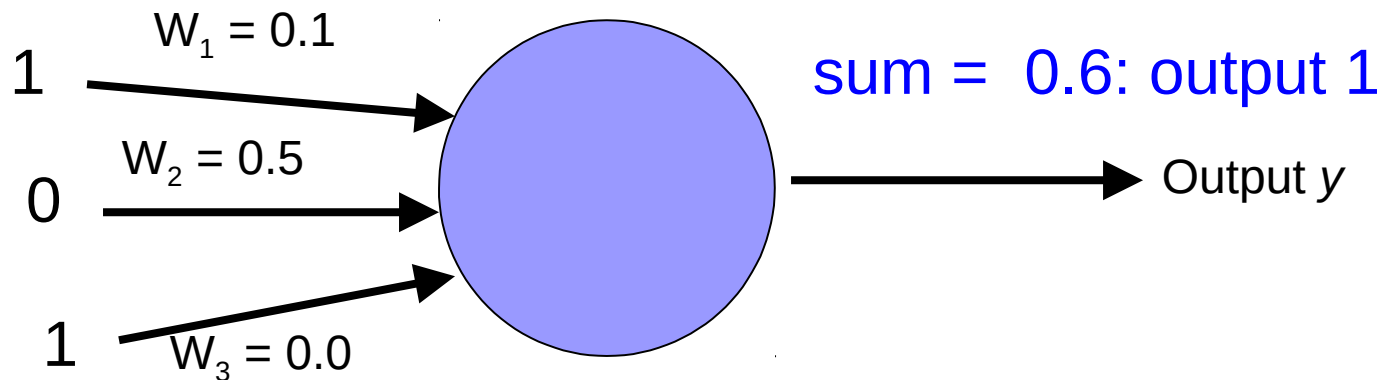
Right or wrong?

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$$\lambda = 0.1$$

if wrong:

$$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$$



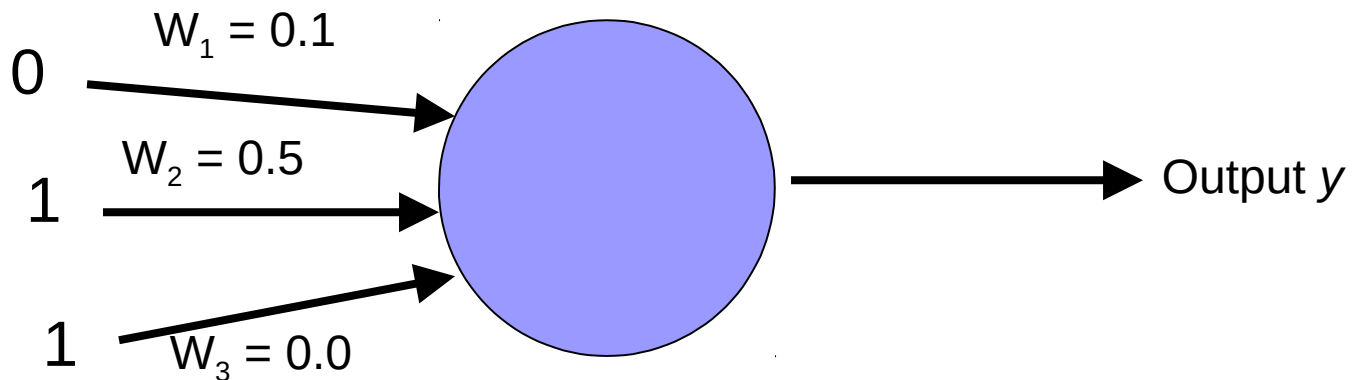
Right. No update!

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$$\lambda = 0.1$$

if wrong:

$$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$$



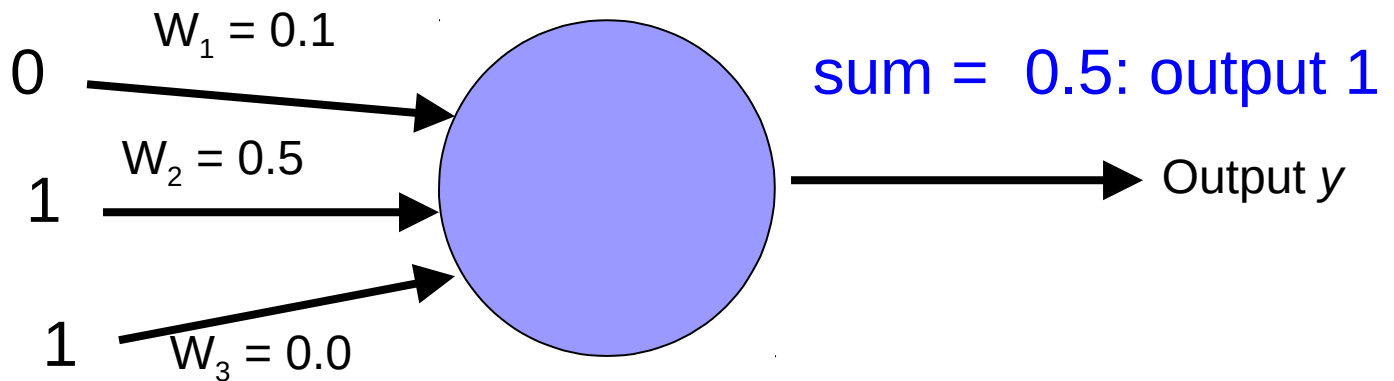
Right or wrong?

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$$\lambda = 0.1$$

if wrong:

$$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$$



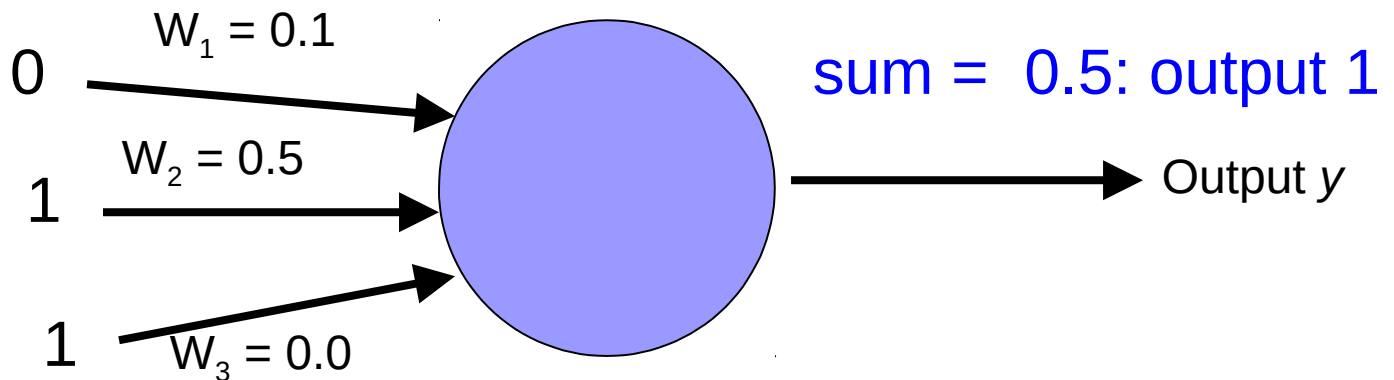
Wrong

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$$\lambda = 0.1$$

if wrong:

$$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$$



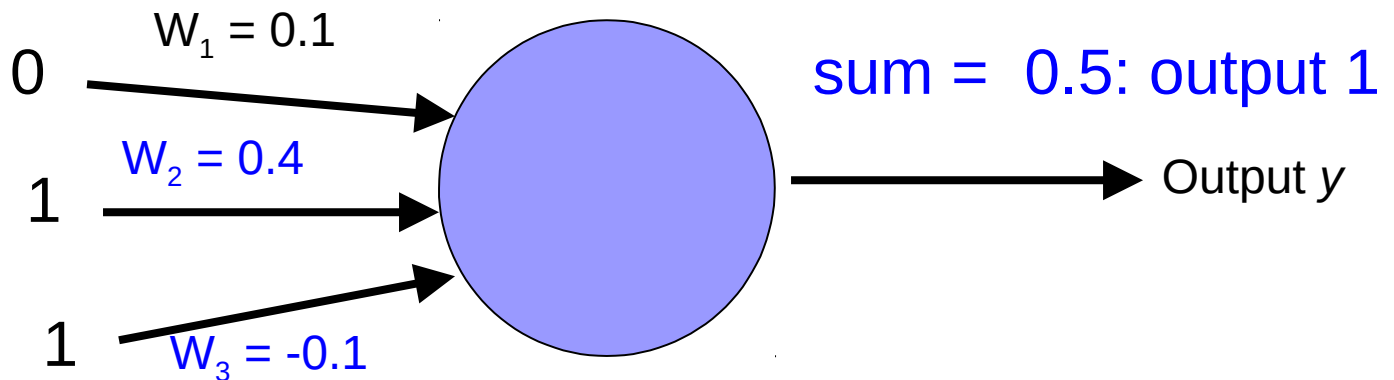
new weights?

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$$\lambda = 0.1$$

if wrong:

$$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$$



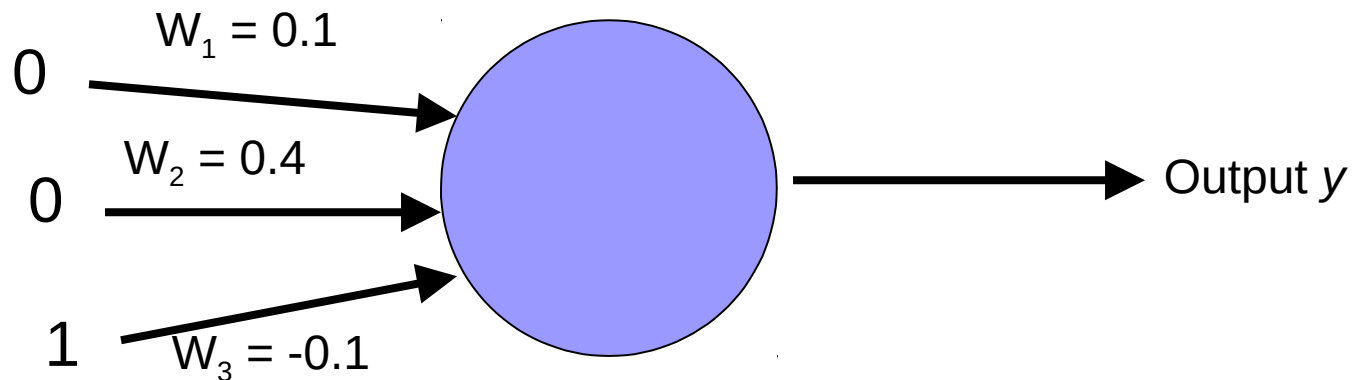
decrease $(0-1=-1)$ all non-zero x_i by 0.1

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$$\lambda = 0.1$$

if wrong:

$$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$$



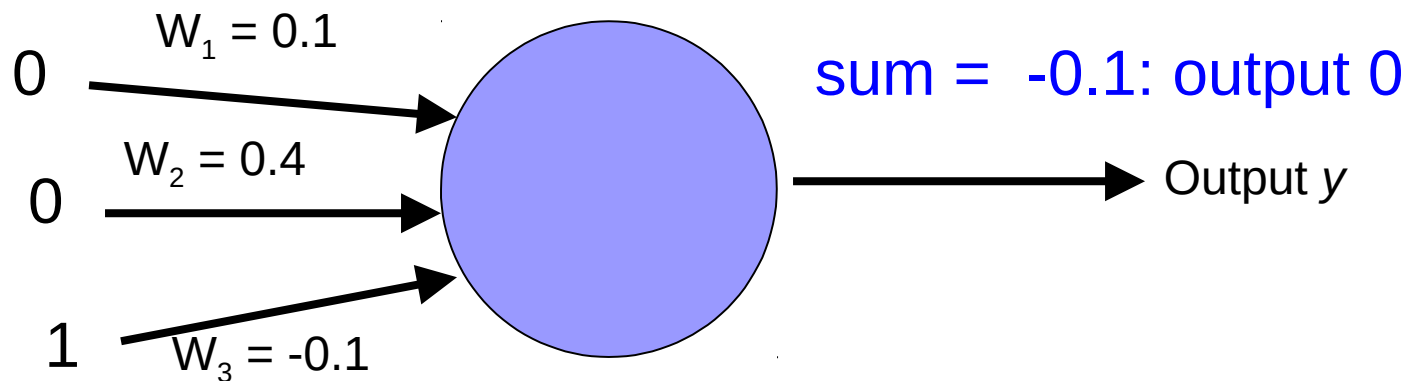
Right or wrong?

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$$\lambda = 0.1$$

if wrong:

$$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$$



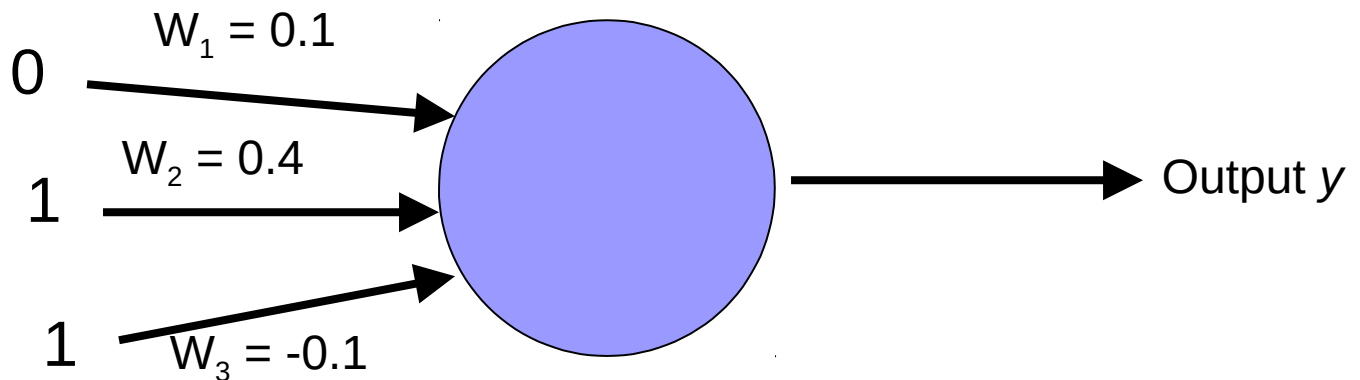
Right. No update!

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$$\lambda = 0.1$$

if wrong:

$$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$$



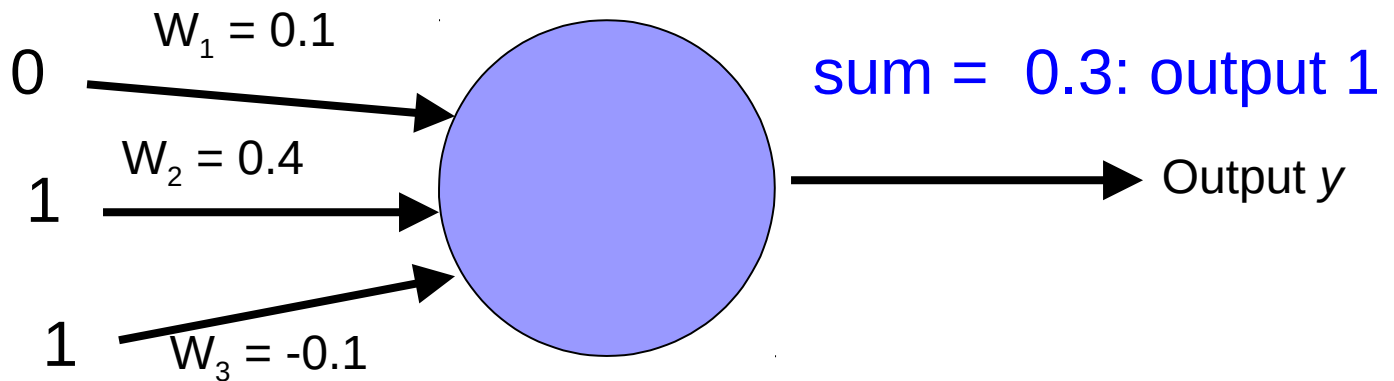
Right or wrong?

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$$\lambda = 0.1$$

if wrong:

$$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$$



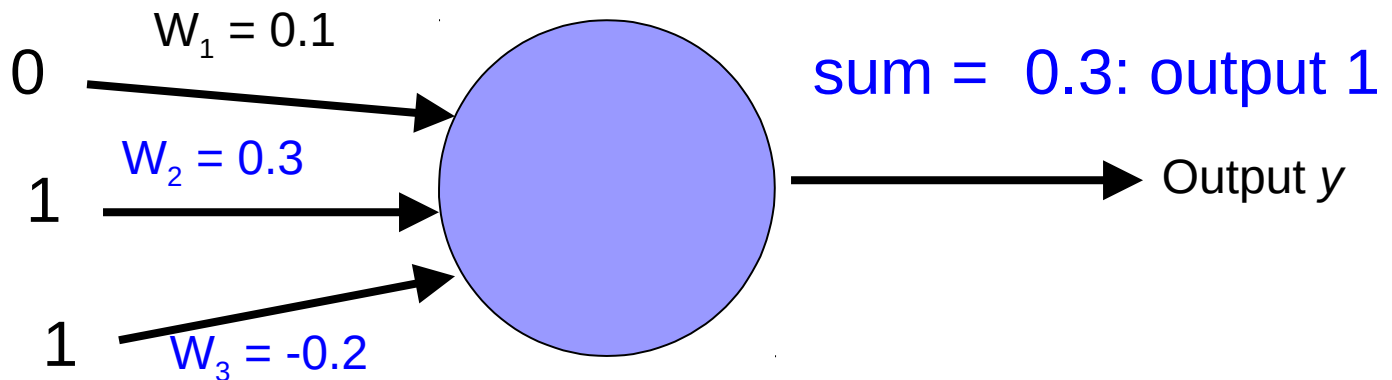
Wrong

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$$\lambda = 0.1$$

if wrong:

$$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$$



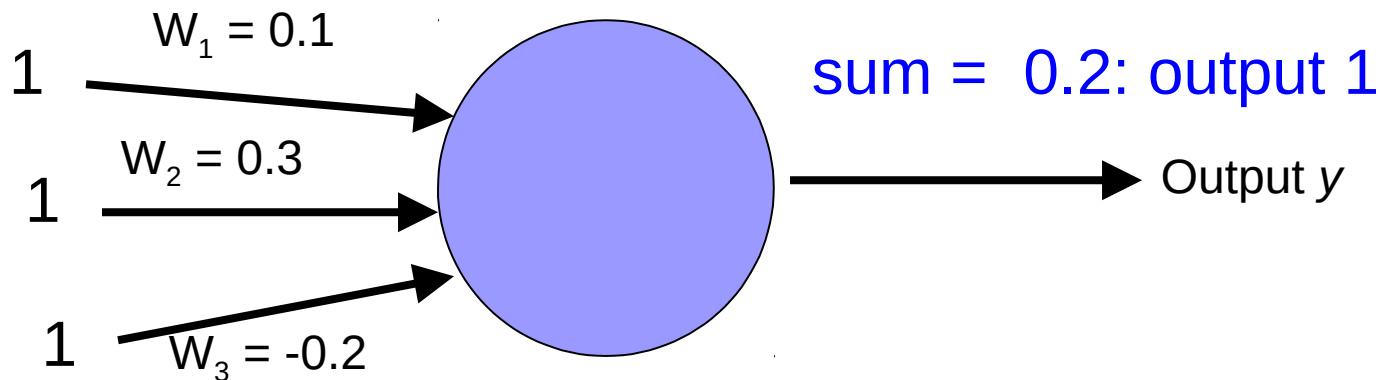
decrease $(0-1=-1)$ all non-zero x_i by 0.1

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$$\lambda = 0.1$$

if wrong:

$$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$$



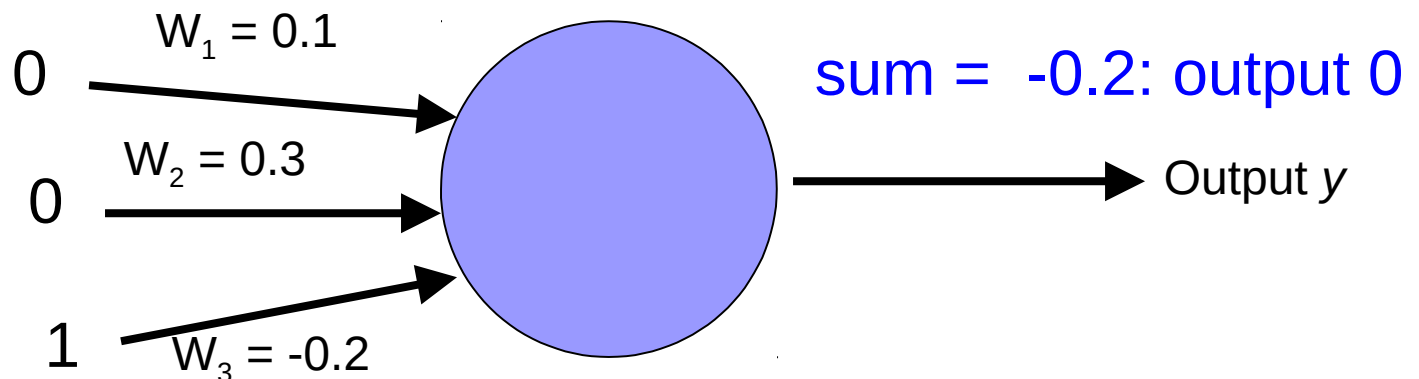
Right. No update!

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$$\lambda = 0.1$$

if wrong:

$$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$$



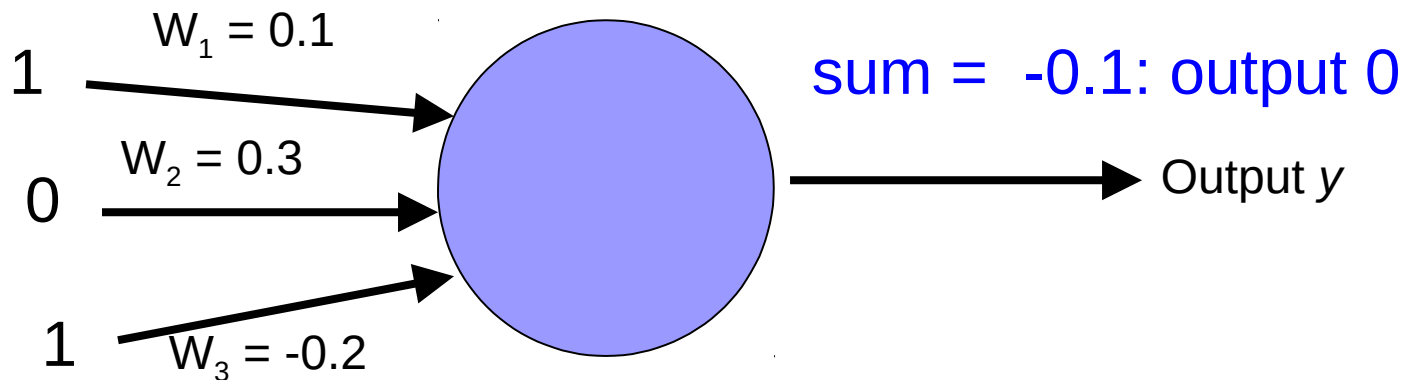
Right. No update!

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$$\lambda = 0.1$$

if wrong:

$$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$$



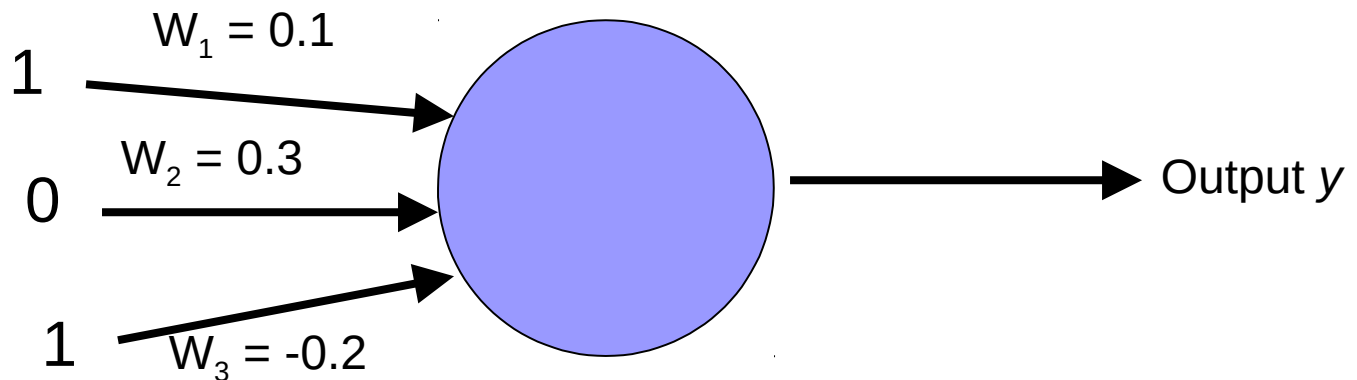
Right. No update!

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$$\lambda = 0.1$$

if wrong:

$$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$$



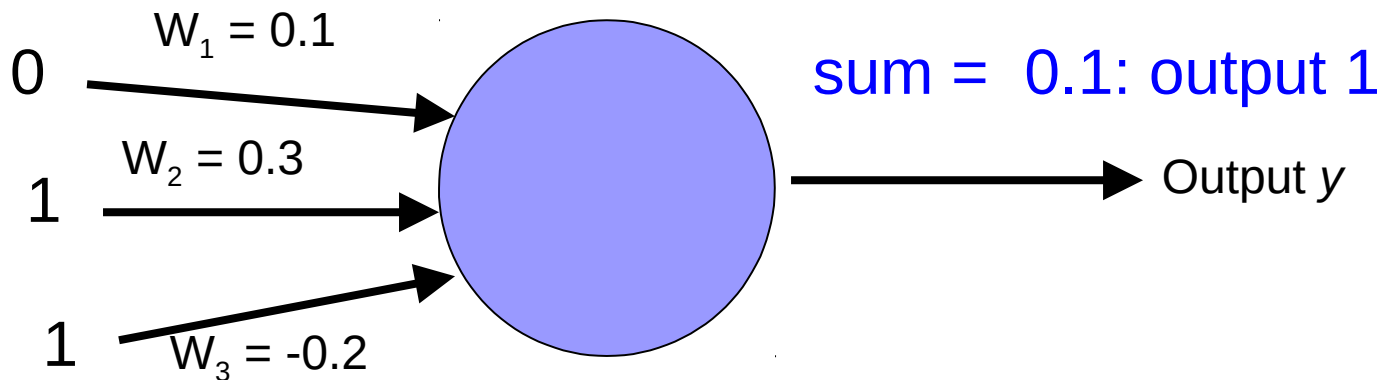
Are they all right?

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$$\lambda = 0.1$$

if wrong:

$$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$$



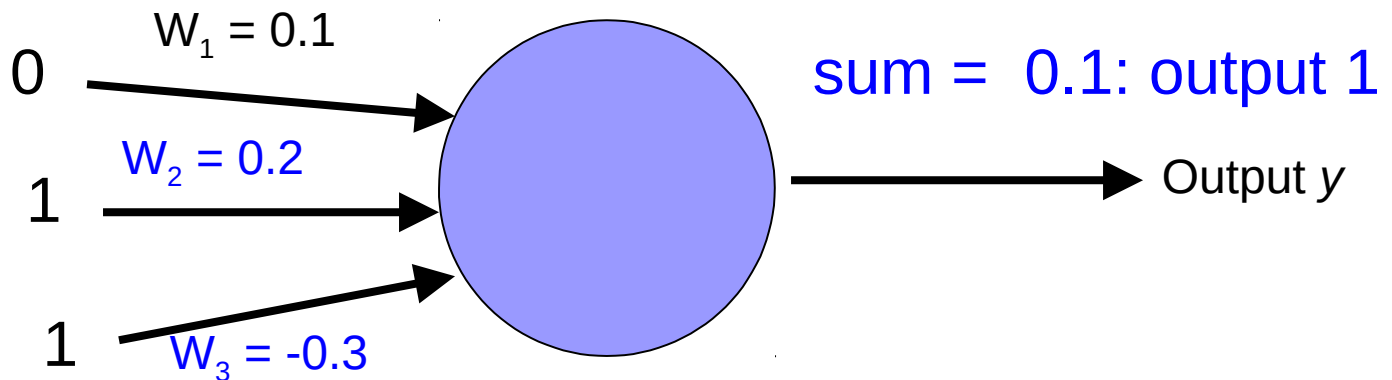
Wrong

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$$\lambda = 0.1$$

if wrong:

$$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$$



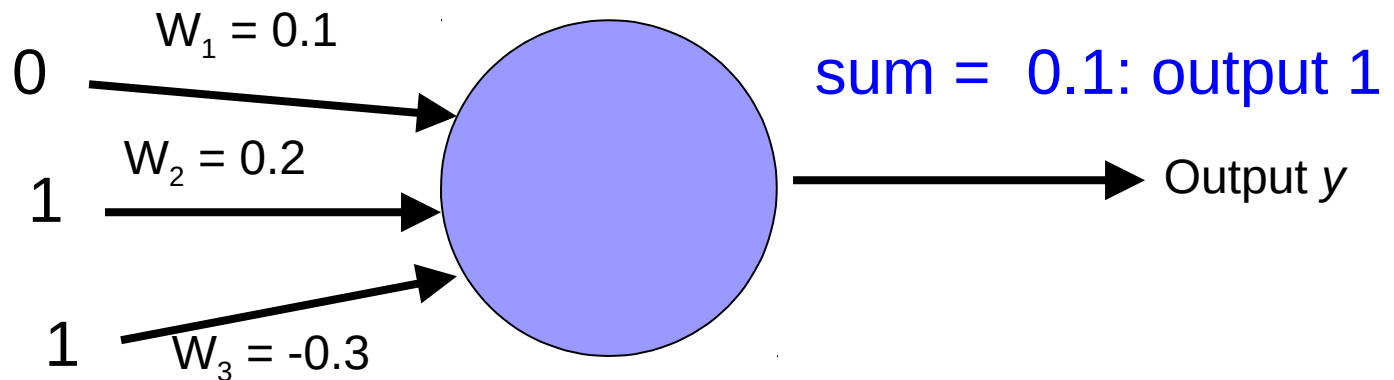
decrease $(0-1=-1)$ all non-zero x_i by 0.1

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$$\lambda = 0.1$$

if wrong:

$$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$$



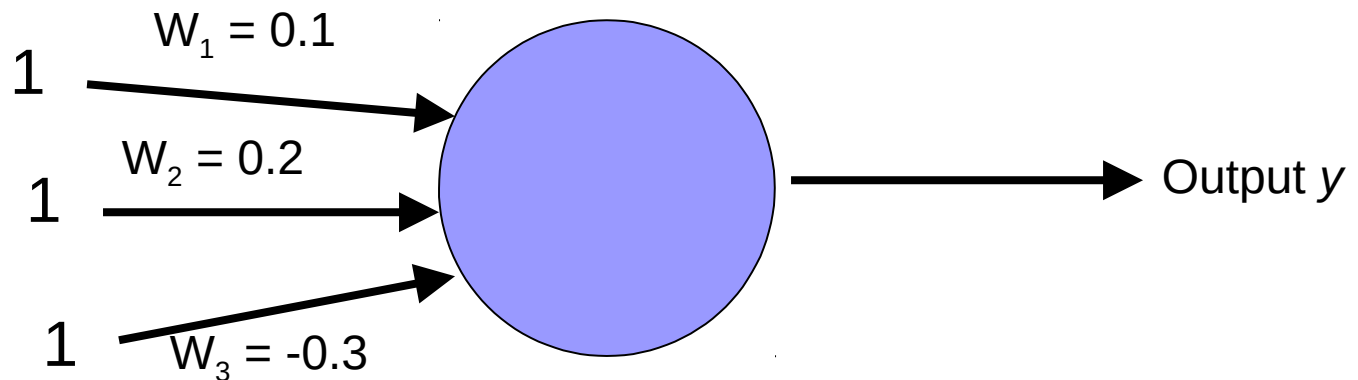
Are they all right?

x_1	x_2	x_1 and x_2
0	0	0
0	1	0
1	0	0
1	1	1

$$\lambda = 0.1$$

if wrong:

$$w_i = w_i + \lambda * (\text{actual} - \text{predicted}) * x_i$$



We've learned AND!



Perceptron learning

A few missing details, but not much more than this

Keeps adjusting weights as long as it makes mistakes

If the training data is **linearly separable** the perceptron learning algorithm is guaranteed to converge to the “correct” solution (where it gets all examples right)



Optional parameters

See:

http://www.cs.pomona.edu/~dkauchak/classes/cs51a/examples/optional_parameters.txt