Algorithms, Red-Black Trees - Sunday, October 11, 2020

1. What is the minimum number of nodes in a tree based on “k”?

2. Draw a worst-case (as unbalanced as possible) Red-Black tree that has exactly 3 black nodes on every root-NULL path. (Draw red nodes as open circles and black nodes as double lined circles.)

3. Insert a “9” into the tree below. You do not have to show all of your work (step through the provided code; I’ve given two copies of the code to help with groups). You should redraw the tree in the space to the right. This will require several rotations.
FUNCTION RBTreeInsert(tree, new_node)
    # Search for position of new_node
    parent = NONE
    current_node = tree.root
    WHILE current_node != NONE
        parent = current_node
        IF new_node.key < current_node.key
            current_node = current_node.left
        ELSE
            current_node = current_node.right
        new_node.parent = parent
    # Insert as root or left/right child
    IF parent == NONE
        tree.root = new_node
    ELSE IF new_node.key < parent.key
        parent.left = new_node
    ELSE
        parent.right = new_node
    # Initialize the new_node
    new_node.left = NONE
    new_node.right = NONE
    new_node.color = RED
    RBTreeFixColors(tree, new_node)

FUNCTION RBTreeFixColors(tree, node)
    WHILE node.parent.color == RED
        # Look for aunt/uncle node
        IF node.parent == node.parent.parent.left
            aunt = node.parent.parent.right
        IF aunt.color == RED
            node.parent.color = BLACK
            aunt.color = BLACK
            node.parent.parent.color = RED
            node = node.parent.parent
        ELSE
            IF node == node.parent.right
                node = node.parent
                LeftRotate(tree, node)
            node.parent.color = BLACK
            node.parent.parent.color = RED
            RightRotate(tree, node)
        ELSE
            IF node == node.parent.left
                node = node.parent
                RightRotate(tree, node)
            node.parent.color = BLACK
            node.parent.parent.color = RED
            LeftRotate(tree, node)
    tree.root.color = BLACK
FUNCTION RBTTreeInsert(tree, new_node)
    # Search for position of new_node
    parent = NONE
    current_node = tree.root
    WHILE current_node != NONE
        parent = current_node
        IF new_node.key < current_node.key
            current_node = current_node.left
        ELSE
            current_node = current_node.right
        new_node.parent = parent
    # Insert as root or left/right child
    IF parent == NONE
        tree.root = new_node
    ELSE IF new_node.key < parent.key
        parent.left = new_node
    ELSE
        parent.right = new_node
    # Initialize the new_node
    new_node.left = NONE
    new_node.right = NONE
    new_node.color = RED

RBTTreeFixColors(tree, new_node)