

Longest increasing subsequence

Given a sequence of numbers $X = x_1, x_2, ..., x_n$ find the longest increasing subsequence

 $(i_1,\,i_2,\,\ldots,\,i_m),\,i.e.,\,a$ subsequence where numbers in the sequence increase.

52863697

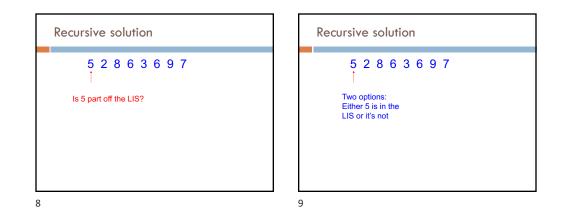
Longest increasing subsequence

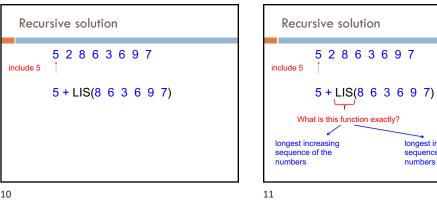
Given a sequence of numbers $X = x_1, \, x_2, \, \ldots, \, x_n$ find the longest increasing subsequence

 $(i_1,\,i_2,\,\ldots,\,i_m),\,i.e.,\,a$ subsequence where numbers in the sequence increase.

5 <u>2</u> 8 6 <u>3</u> <u>6</u> <u>9</u> 7

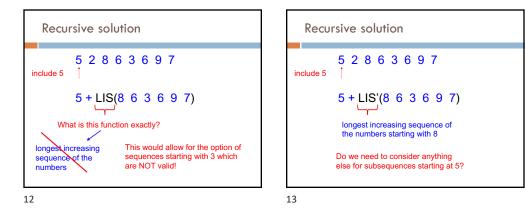
3

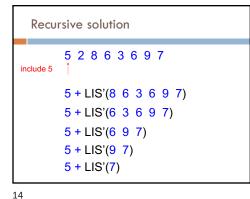


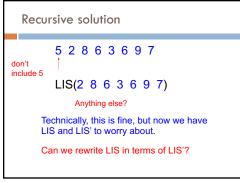


longest increasing sequence of the

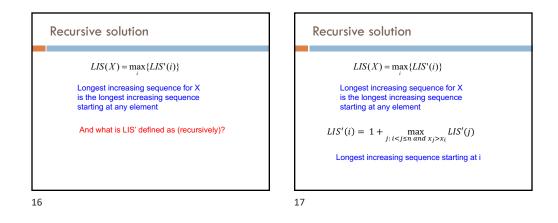
numbers starting with 8

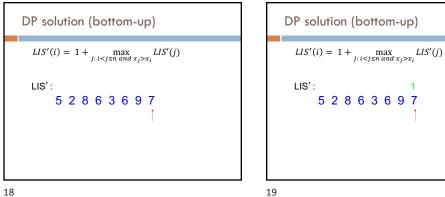


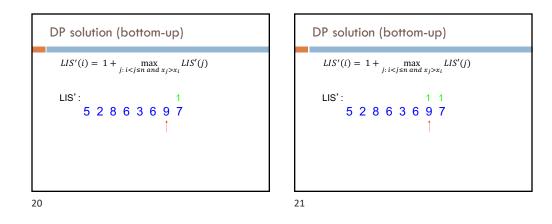


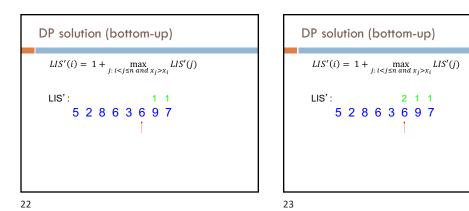


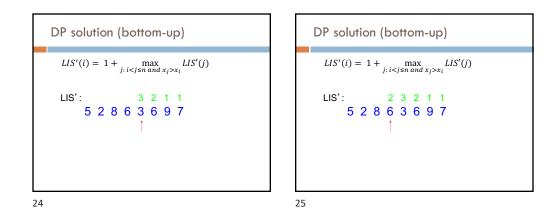




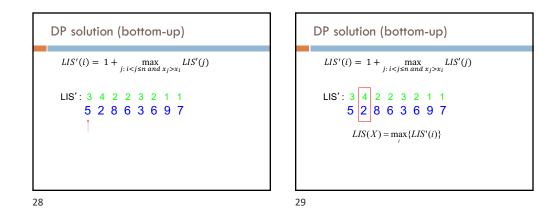


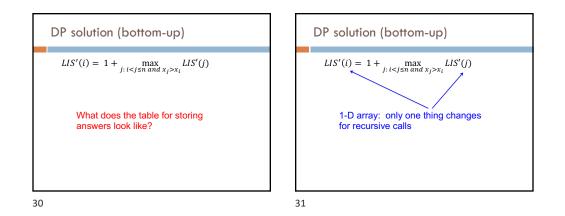


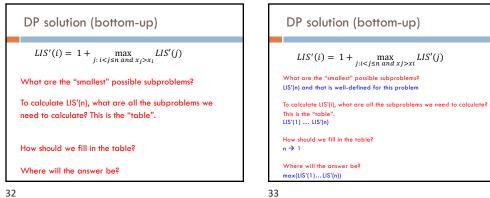




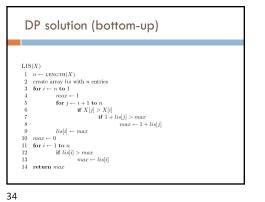
DP solution (bottom-up)	DP solution (bottom-up)
$LIS'(i) = 1 + \max_{j: \ i < j \le n \ and \ x_j > x_i} LIS'(j)$	$LIS'(i) = 1 + \max_{j: i < j \le n \text{ and } x_j > x_i} LIS'(j)$
LIS': 2 2 3 2 1 1 5 2 8 6 3 6 9 7 1	LIS': 4 2 2 3 2 1 1 5 2 8 6 3 6 9 7 1

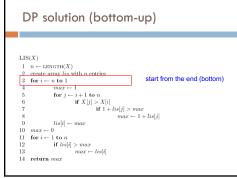




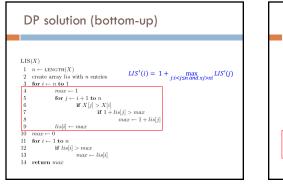


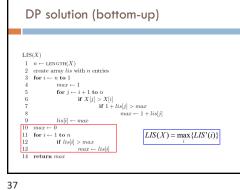


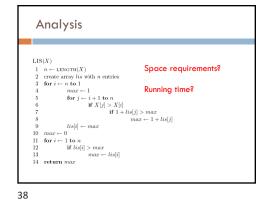


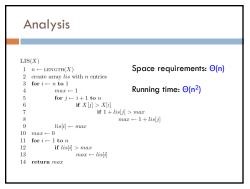




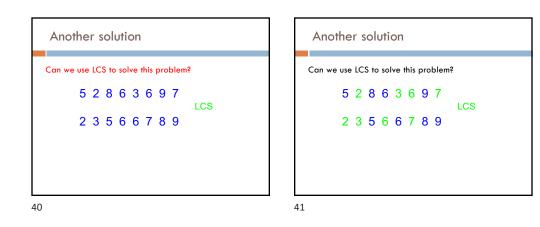


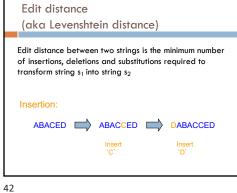












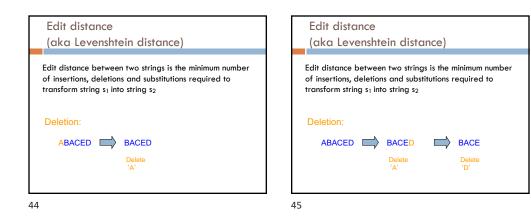


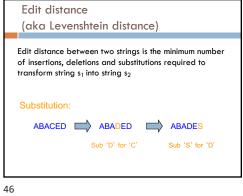
(aka Levenshtein distance)

Edit distance between two strings is the minimum number of insertions, deletions and substitutions required to transform string s1 into string s2

Deletion:

ABACED

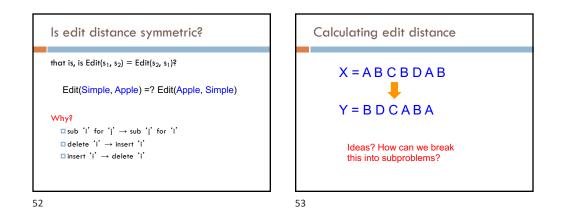


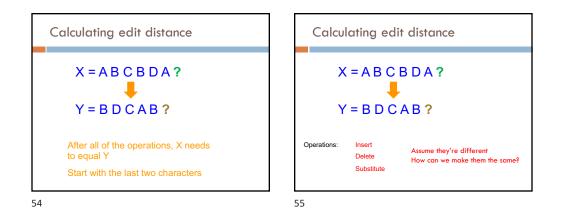


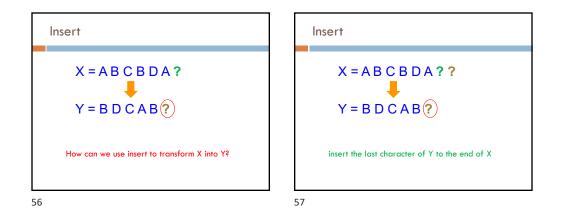
Edit distance examples
Edit(Kitten, Mitten) = 1
Operations: Sub 'M' for 'K' Mitten
47

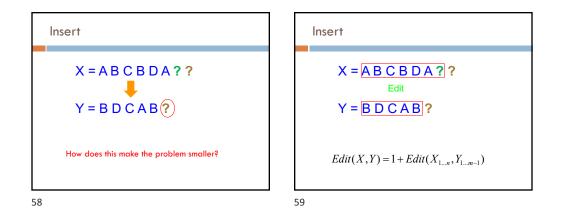
Edit distance examples	Edit distance examples
Edit(Happy, Hilly) = 3	Edit(Banana, Car) = 5
Operations:	Operations:
Sub 'a' for 'i' Hippy	Delete 'B' anana
Sub 'l' for 'p' Hilpy	Delete 'a' nana
Sub 'l' for 'p' Hilly	Delete 'n' naa
	Sub 'C' for 'n' Caa
	Sub 'a' for 'r' Car

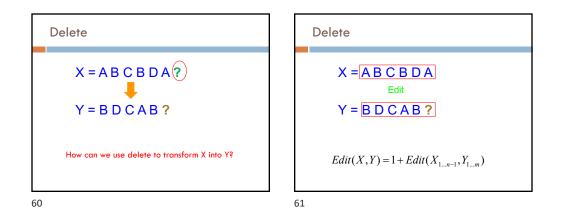


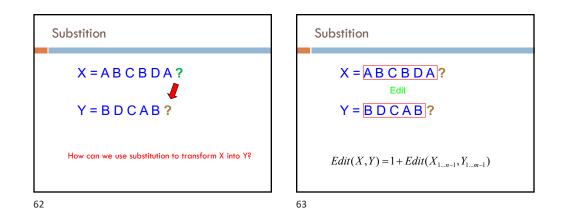


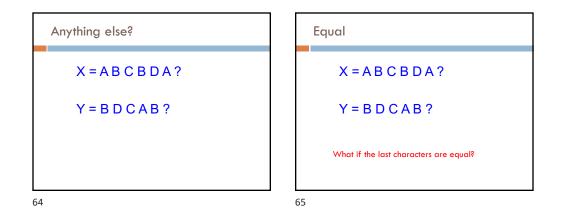


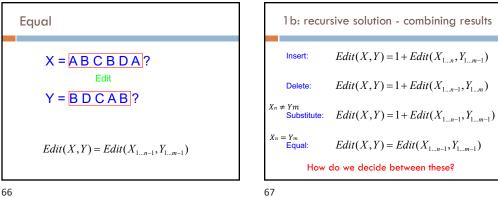










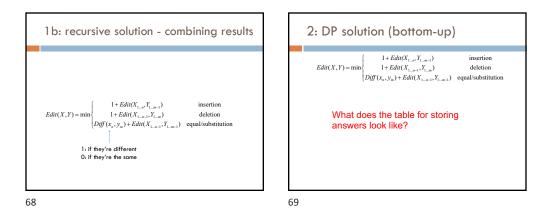


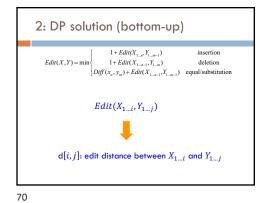
16

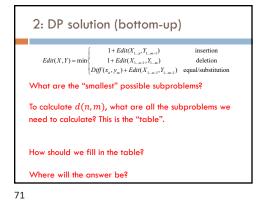
 $Edit(X,Y) = 1 + Edit(X_{1...n}, Y_{1...m-1})$

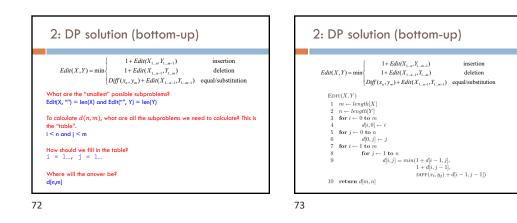
 $Edit(X, Y) = 1 + Edit(X_{1...n-1}, Y_{1...m})$

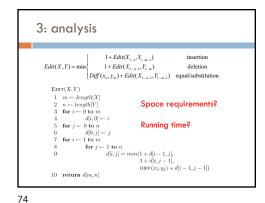
 $Edit(X, Y) = Edit(X_{1...n-1}, Y_{1...m-1})$

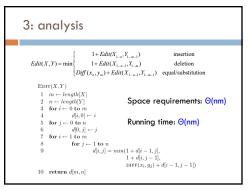




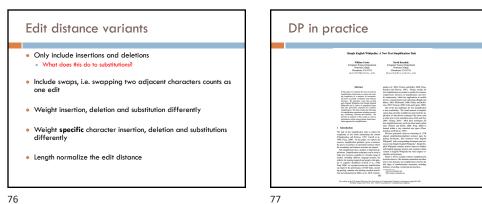


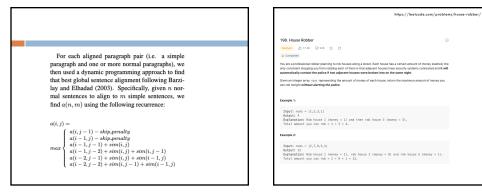
















10/8/24