











Greedy vs. divide and conquer	
Greedy	I
To solve the general problem:	
Pick a locally optimal solution and repeat	
6	











A greedy	solution?	
$\Rightarrow x$	$x \wedge z \Longrightarrow w$	$w \wedge y \wedge z \Longrightarrow x$
$x \Rightarrow y$	$x \wedge y \Longrightarrow w$	$\overline{w} \vee \overline{x} \vee \overline{y}$
	w 0	
	x 1	
	y 1	
	z 0	





















Correctness of greedy solution

Two parts:

- If our algorithm returns an assignment, is it a valid assignment?
- If our algorithm does not return an assignment, does an assignment exist?

21



22



































Variable length code





































A greedy algorithm? Given file frequencies, can we come up with a prefixfree encoding (i.e. build a prefix tree) that minimizes the number of bits? $HUFFMAN(F) = 1 \quad Q \leftarrow MAREHEAP(F) \\ 2 \quad for \ i - 1 \ to \ |Q| - 1 \\ 3 \quad allocate a new node z \\ 4 \quad left[z] \leftarrow x \leftarrow EXTRACTMIN(Q) \\ 5 \quad right[z] \leftarrow y \leftarrow EXTRACTMIN(Q) \\ 6 \quad f[z] \leftarrow f[x] + f[y] \\ 7 \quad INBERT(Q,z) \\ 8 \quad return EXTRACTMIN(Q)$





























All the greedy algorithms we've looked at so far give the optimal answer

Some of the most common greedy algorithms generate good, but non-optimal solutions

- set cover
- clustering
- hill-climbing
- relaxation

69

Knapsack problems: Greedy or not?

 $\begin{array}{l} \textbf{0-1 Knapsack} - A \text{ thief robbing a store finds n items} \\ \text{worth } v_1, v_2, ..., v_n \text{ dollars and weight } w_1, w_2, ..., w_n \\ \text{pounds, where } v_i \text{ and } w_i \text{ are integers. The thief can carry } \\ \text{at most } W \text{ pounds in the knapsack. Which items should } \\ \text{the thief take if he wants to maximize value.} \end{array}$

Fractional knapsack problem – Same as above, but the thief happens to be at the bulk section of the store and can carry fractional portions of the items. For example, the thief could take 20% of item i for a weight of $0.2w_i$ and a value of $0.2v_i$.

70











Course feedback

lectures are wayyy too fast, barely enough time to process things so it feels pointless to take notes; current course content is comprehensive and makes sense but it feels disorganized, like different content stitched together sort of so...

Having more examples, or going through the slides a bit slower



Course feedback

The homeworks are a lot of work and the mentors are super helpful but someone's even they don't have the solutions and that wastes hours of our time. I think homeworks can have more straight forward problems that show we understand things rather than problems that we always have to scavenge the internet and bug mentors for understandings.

76



Checkpoint 1

77