In-Class Worksheet Discrete Math & Functional Programming— CSCI 054— Spring 2025 Instructor: Osborn

Given an implication $p \Rightarrow q$, we can define the following related concepts:

• converse: $q \Rightarrow p$ • inverse: $\neg p \Rightarrow \neg q$

• contrapositive: $\neg q \Rightarrow \neg p$

Which, if any, are logically equivalent to the original implication?

If 2 is an even number, then 3 is an odd number

If x is an even number, then x + 1 is an odd number

Define the predicates:

- rested(n) = "n got at least 8 hours of sleep in the past 24 hours"
- bornMA(n) = "n was born in Massachusetts"

Which, if any, of the following propositions is True? Justify your answer.

- \exists n in this room : rested(n)
- \forall n in this room : (rested(n) \Rightarrow bornMA(n))
- \exists n currently enrolled at Pomona College : (rested(n) \land bornMA(n))
- \forall currently enrolled at Pomona College : (rested(n) \lor bornMA(n))

Is the following a theorem? Explain.

 $[\forall x \in S : P(x)] \lor [\forall x \in S : \neg P(x)]$