

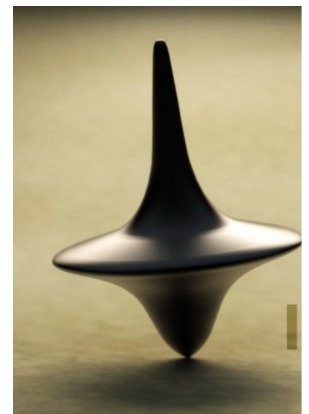
Lecture 14: Recursion

CS 51P

October 24, 2022



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he/him/his



Class News

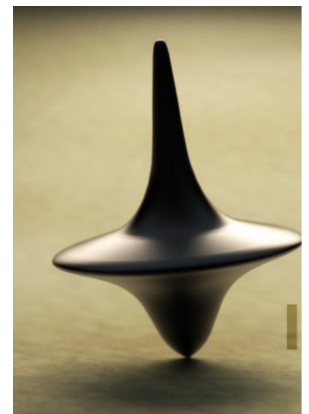
- Image manipulations lab deadline extended to Tue 10/25

Learning Goals

- Recursion

What is recursion?

- Wikipedia: "Recursion occurs when a thing is defined in terms of itself."
- A technique for tackling large or complicated problems by taking 1 "bite" of the problem at a time
 - Divide and conquer

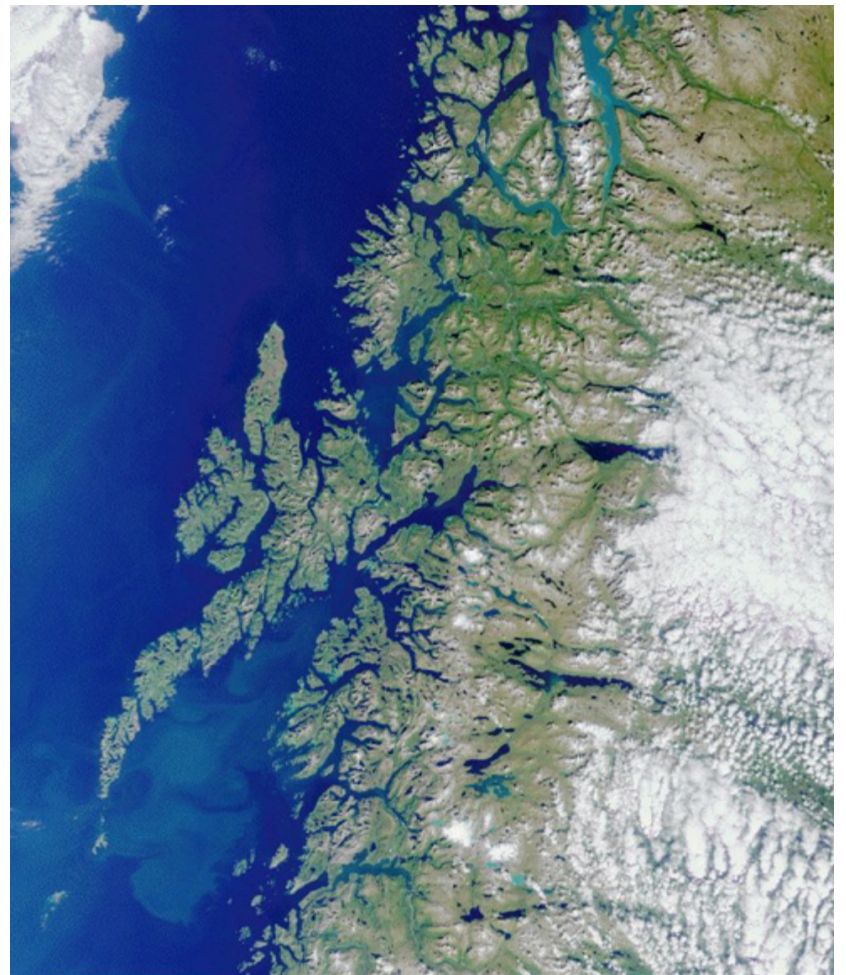
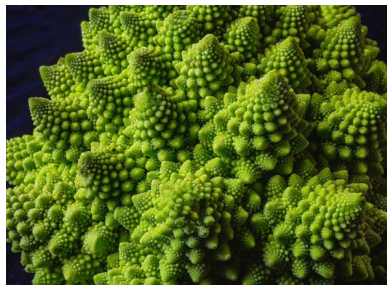


What is recursion?

- A powerful substitute for iteration (loops)
 - Start by seeing the difference between iteration vs recursion
 - Some problems can only be solved using recursion
- Results in elegant, shorter code when used well
- Often applied to sorting and searching problems

What is recursion?

- Can be used to express patterns seen in nature
- Object containing smaller copies of itself



How many students are in class?

- If I want to find out how many people are in class today, but I don't want to walk around and count each person.
- I am recruiting you to help, but I also want to minimize each student's amount of work.



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- **We can solve this problem recursively!**

How many students are in class?

- Let's focus on solving the problem for a single column of students.



How many students are in class?

- Let's focus on solving the problem for a single column of students.
- I will ask the first person in the front row: "How many people are sitting directly behind you in your column?"



How many students are in class?

- Student's algorithm:
 - If there is no one behind me, answer 0.
 - If someone is sitting behind me:
 - Ask that person: "How many people are sitting directly behind you in your column?"
 - When they respond with a value N , respond $(N + 1)$ to the person who asked me.



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- Can generalize to the entire classroom!

2 main components of recursion

- 1) Base case
 - The simplest version of your problem that all other cases reduce to
 - An occurrence that can be answered directly

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2 main components of recursion

- 1) **Base case**
 - The simplest version of your problem that all other cases reduce to
 - An occurrence that can be answered directly
 - What's the base case for the demo?
- 2) **Recursive case**
 - The step where you break down more complex versions of the task into smaller occurrences
 - Cannot be answered directly
 - What is the recursive case for the demo?

Recursion overview

- Reduce problem into repeated, smaller tasks of the same form
- Recursion has 2 main parts: **base case** and **recursive case**
- Solution is built up as you come back up the call stack
- When solving recursively, look for self-similarity and think about what info is stored in each stack frame
- Take the “recursive leap of faith” and trust the smaller tasks will solve the problem for you!

Factorial example

- The number **n factorial**, **n!** in math notation, is
 - **$n \times (n - 1) \times \dots \times 3 \times 2 \times 1$**

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 - $5! = 5 \times 4 \times 3 \times 2 \times 1 = 120$
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 - $0! = 1$ (by definition)
- Let's implement the factorial function!

Factorial function

- $5! = 5 \times 4 \times 3 \times 2 \times 1$

Math view of factorials

- $n! = 1$ if $n = 0$
- $n! = n \times (n - 1)!$ Otherwise

- Convert to code:

Recursion in action

- Stack frame – one gets created each time a function is called
- Stack is where information is stored in computer's memory
- Every time we call `factorial()`, we get a new copy of the local variable `n`
- Stack frames go away once they return

Recursion review

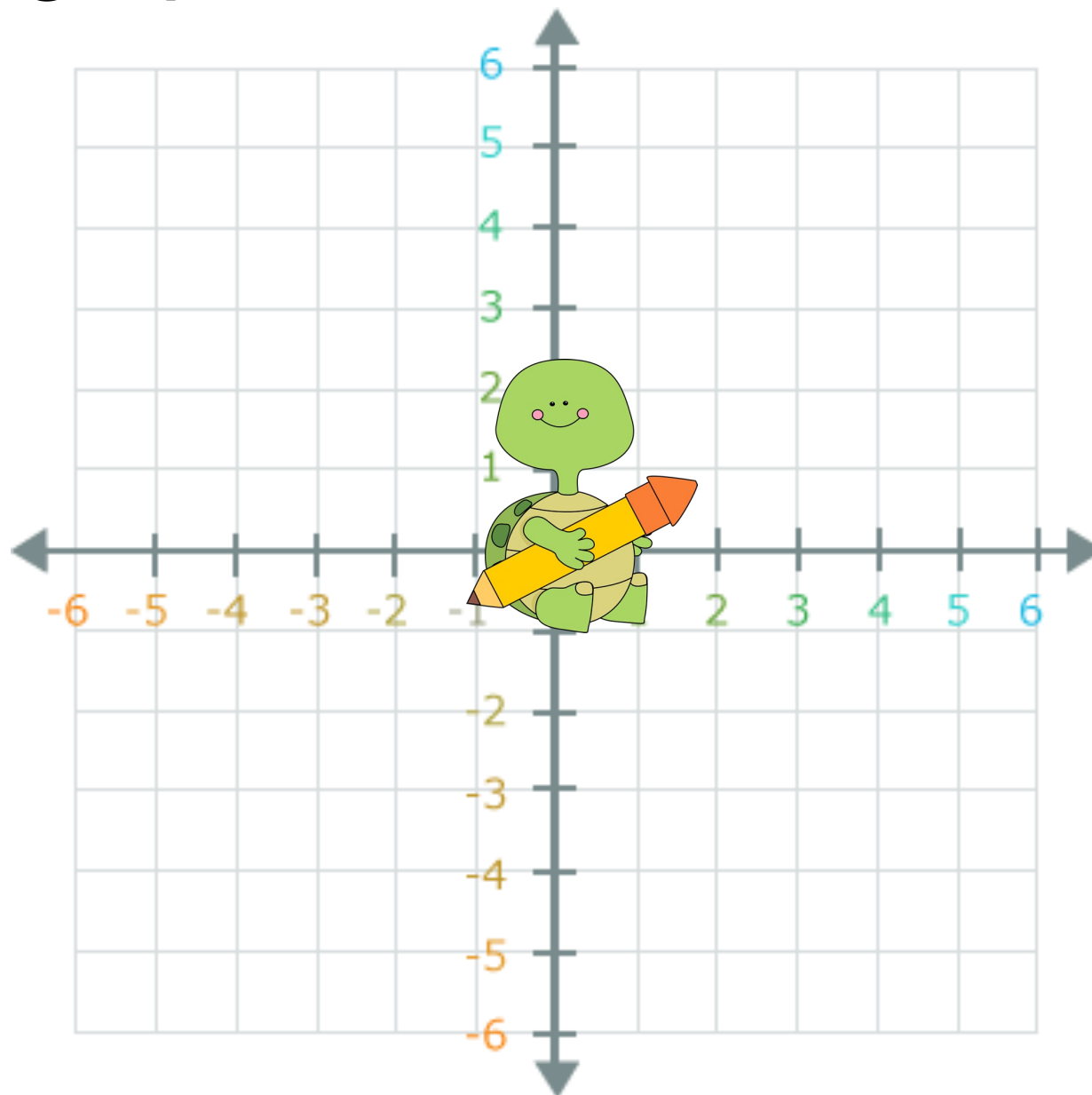
- Reduce problem into repeated, smaller tasks of the same form
- Recursion has 2 parts: **base case** and **recursive case**
 - Each part may have multiple cases
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Exercise: isPalindrome

- Write a recursive function to check if a string is a palindrome
- Palindrome is word, number, phrase or other sequence of symbols that reads the same backwards and forwards.

C
ANNA
CIVIC
RACECAR
STEP ON NO PETS
STRESSED DESSERTS

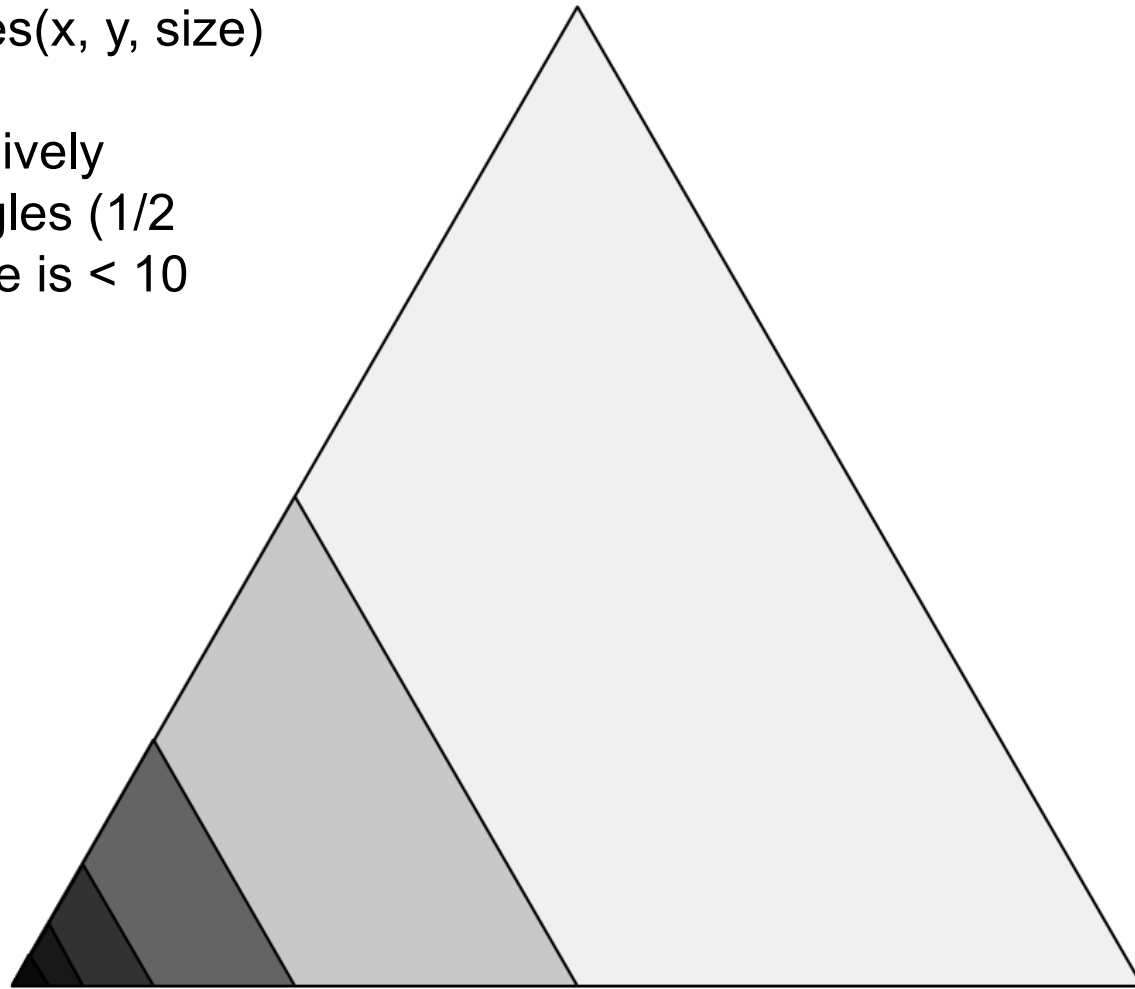
Turtle graphics



Example - Recursive Graphics

`draw_triangles(x, y, size)`

Draws recursively
smaller triangles (1/2
size) until size is < 10



Counting Triangles

