

Word Alignment

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CS159 – Spring 2023

Some slides adapted from
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Computer Science Department
UCBerkeley

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Admin

Assignment 5

Assignment 6 out later today: due Sunday 11/13

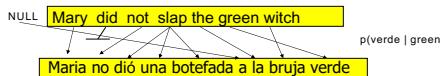
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Language translation



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Word models: IBM Model 1



Each foreign word is aligned to exactly one English word

This is the **ONLY** thing we model!

$$p(f_1 f_2 \dots f_{|f|}, a_1 a_2 \dots a_{|f|} | e_1 e_2 \dots e_{|f|}) = \prod_{i=1}^{|f|} p(f_i | e_{a_i})$$

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Training a word-level model

The old man is happy. He El viejo está feliz porque ha
has fished many times. pescado muchos veces.
His wife talks to him. Su mujer habla con él.
The sharks await. Los tiburones esperan.

...

...

$$p(f_1 f_2 \dots f_{|f|} | a_1 a_2 \dots a_{|f|} | e_1 e_2 \dots e_{|e|}) = \prod_{i=1}^{|f|} p(f_i | e_i)$$

$p(f_i | e_i)$: probability that e is translated as f

How do we learn these?

What data would be useful?

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Thought experiment

The old man is happy. He has fished many times.
El viejo está feliz porque ha pescado muchos veces.

His wife talks to him.
Su mujer habla con él.

The sharks await.
Los tiburones esperan.

$$p(f_i | e_i) = ?$$

$$p(el | the) = ?$$

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Thought experiment

The old man is happy. He has fished many times.
El viejo está feliz porque ha pescado muchos veces.

His wife talks to him.
Su mujer habla con él.

The sharks await.
Los tiburones esperan.

$$p(f_i | e_i) = \frac{\text{count}(f \text{ aligned-to } e)}{\text{count}(e)}$$

$$p(el | the) = 0.5$$

Any problems concerns?

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Thought experiment

The old man is happy. He has fished many times.
El viejo está feliz porque ha pescado muchos veces.

His wife talks to him.
Su mujer habla con él.

The sharks await.
Los tiburones esperan.

Getting data like this is expensive!

Even if we had it, what happens when we switch to a new domain/corpus

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Thought experiment #2

The old man is happy. He has fished many times.
 ↓ ↓ ↓ ↓ ↓
 El viejo está feliz porque ha pescado muchos veces.

Annotator 1

The old man is happy. He has fished many times.
 ↓ ↓ ↓ ↓ ↓
 El viejo está feliz porque ha pescado muchos veces.

Annotator 2

$p(f_i | e_{a_i}) = \frac{\text{count}(f \text{ aligned-to } e)}{\text{count}(e)}$ What do we do?

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Thought experiment #2

The old man is happy. He has fished many times.
 ↓ ↓ ↓ ↓ ↓
 El viejo está feliz porque ha pescado muchos veces.

80 annotators

The old man is happy. He has fished many times.
 ↓ ↓ ↓ ↓ ↓
 El viejo está feliz porque ha pescado muchos veces.

20 annotators

$p(f_i | e_{a_i}) = \frac{\text{count}(f \text{ aligned-to } e)}{\text{count}(e)}$ What do we do?

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Thought experiment #2

The old man is happy. He has fished many times.
 ↓ ↓ ↓ ↓ ↓
 El viejo está feliz porque ha pescado muchos veces.

80 annotators

The old man is happy. He has fished many times.
 ↓ ↓ ↓ ↓ ↓
 El viejo está feliz porque ha pescado muchos veces.

20 annotators

$p(f_i | e_{a_i}) = \frac{\text{count}(f \text{ aligned-to } e)}{\text{count}(e)}$ Use partial counts:
 - count(viejo ↔ man) 0.8
 - count(viejo ↔ old) 0.2

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Training without alignments

a b
 x y

c b
 z x

How should these be aligned?

There is some information!
 (Think of the alien translation task last time)

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Training without alignments

a b

x y

IBM model 1: Each foreign word is aligned to 1 English word (ignore NULL for now)

What are the possible alignments?

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Training without alignments

a b

x y

a b

x y

a b

x y

a b

x y

IBM model 1: Each foreign word is aligned to 1 English word

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Training without alignments

a b

x y

a b

x y

a b

x y

a b

x y

IBM model 1: Each foreign word is aligned to 1 English word

If I told you how likely each of these were, does that help us with calculating $p(f | e)$?

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Training without alignments

a b

x y

a b

x y

a b

x y

a b

x y

IBM model 1: Each foreign word is aligned to 1 English word

$$p(f_i | e_{a_i}) = \frac{\text{count}(f \text{ aligned-to } e)}{\text{count}(e)}$$

Use partial counts and sum:
- count(y ↔ a) 0.9+0.01
- count(x ↔ a) 0.01+0.01

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One the one hand

a b x y	a b X x y	a b / x y	a b / \ x y
0.01	0.9	0.08	0.01



If you had the likelihood of each alignment, you could calculate $p(f|e)$

$$p(f_i | e_{a_i}) = \frac{\text{count}(f \text{ aligned-to } e)}{\text{count}(e)}$$

One the other hand

a b x y	a b X x y	a b / x y	a b / \ x y
0.01	0.9	0.08	0.01

If you had $p(f|e)$ could you calculate the probability of the alignments?

$$p(F, a_1 a_2 \dots a_n | E) = \prod_{i=1}^n p(f_i | e_{a_i})$$

$$p(f_i | e_{a_i})$$

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One the other hand

a b x y	a b X x y	a b / x y	a b / \ x y
0.01	0.9	0.08	0.01

We want to calculate the probability of the alignment, e.g.

$$p(\text{alignment1}|F, E) = p(A_1|F, E)$$

We can calculate $p(A_1, F | E)$ using the word probabilities.

$$p(F, a_1 a_2 \dots a_n | E) = \prod_{i=1}^n p(f_i | e_{a_i})$$

One the other hand

a b x y	a b X x y	a b / x y	a b / \ x y
0.01	0.9	0.08	0.01

We want to calculate the probability of the alignment, e.g.

$$p(\text{alignment1}|F, E) = p(A_1|F, E)$$

We can calculate $p(A_1, F | E)$ using the word probabilities.

$$p(A, F | E) \quad ? \quad p(A|F, E)$$

How are these two probabilities related?

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Our friend the chain rule

$$p(A_1, F|E) = p(A_1|F, E) * p(F|E)$$

$$p(A_1|F, E) = \frac{p(A_1, F|E)}{p(F|E)}$$

What is $P(F|E)$?

Hint: how do we go from $p(A, F|E)$ to $P(F|E)$?

Our friend the chain rule

$$p(A_1, F|E) = p(A_1|F, E) * p(F|E)$$

$$p(A_1|F, E) = \frac{p(A_1, F|E)}{p(F|E)}$$

$$p(A_1|F, E) = \frac{p(A_1, F|E)}{\sum_A p(A, F|E)}$$

sum over the variable!

How likely is this alignment,
compared to all other alignments
under the model

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One the other hand

Alignment 1 Alignment 2 Alignment 3 Alignment 4

a b
x y

a b
x y

a b
x y

a b
x y

$$\boxed{p(x|a)^* p(y|b)} \quad \boxed{p(x|b)^* p(y|a)} \quad \boxed{p(x|b)^* p(y|b)} \quad \boxed{p(x|a)^* p(y|a)}$$

$$p(F, a1|E) \quad p(F, a2|E) \quad p(F, a3|E) \quad p(F, a4|E)$$

$$p(F, a_1 a_2 \dots a_{|\mathcal{A}|} | E) = \prod_{i=1}^{|\mathcal{A}|} p(f_i | e_{a_i})$$

One the other hand

Alignment 1 Alignment 2 Alignment 3 Alignment 4

a b
x y

a b
x y

a b
x y

a b
x y

$$\boxed{p(x|a)^* p(y|b)} \quad \boxed{p(x|b)^* p(y|a)} \quad \boxed{p(x|b)^* p(y|b)} \quad \boxed{p(x|a)^* p(y|a)}$$

$$p(F, a1|E) \quad p(F, a2|E) \quad p(F, a3|E) \quad p(F, a4|E)$$

Normalize

$$p(a_1|E, F) = \frac{p(x|a)^* p(y|b)}{\sum_{i=1}^4 p(F, a_i|E)}$$

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Have we gotten anywhere?



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Training without alignments

Initially assume all $p(f|e)$ are equally probable

Repeat:

- Enumerate all possible alignments
- Calculate how probable the alignments are under the current model (i.e. $p(f|e)$)
- Recalculate $p(f|e)$ using counts from all alignments, weighted by how probable they are

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EM algorithm

(something from nothing)

General approach for calculating “hidden variables”, i.e. variables without explicit labels in the data

Repeat:

E-step: Calculate the expected probabilities of the hidden variables based on the current model

M-step: Update the model based on the expected counts/probabilities

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EM alignment

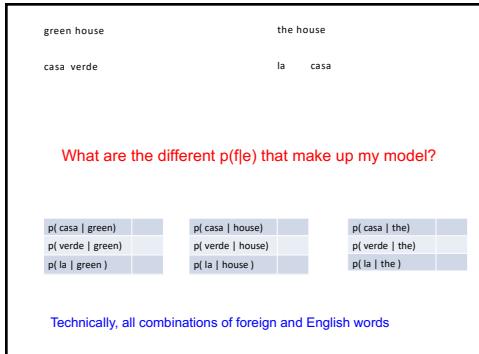
E-step

- Enumerate all possible alignments
- Calculate how probable the alignments are under the current model (i.e. $p(f|e)$)

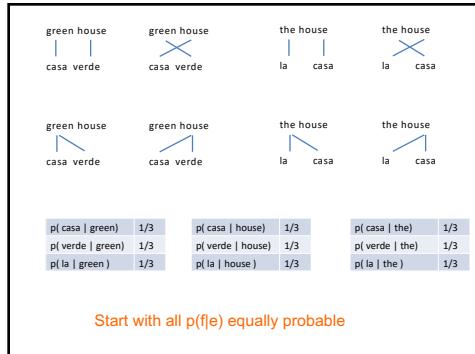
M-step

- Recalculate $p(f|e)$ using counts from all alignments, weighted by how probable they are

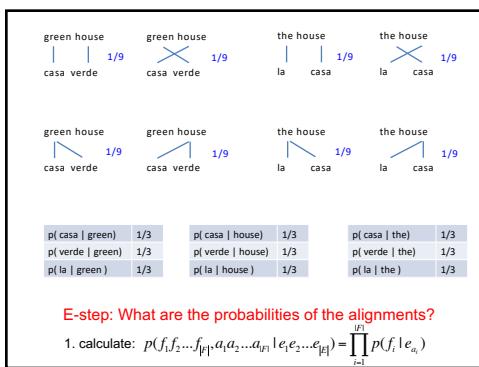
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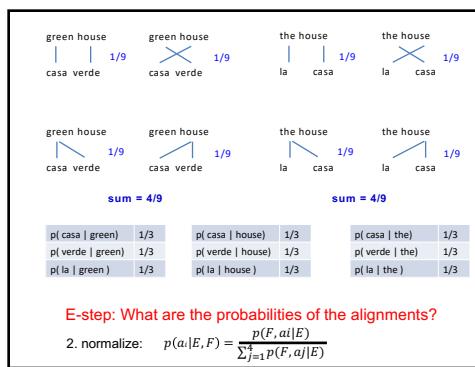
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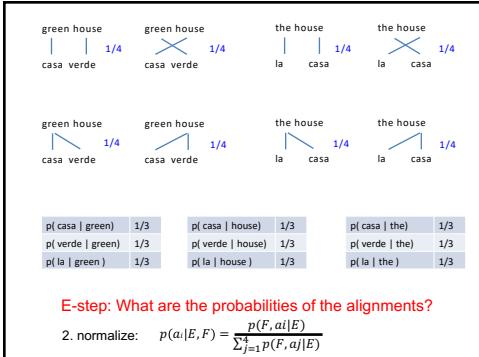
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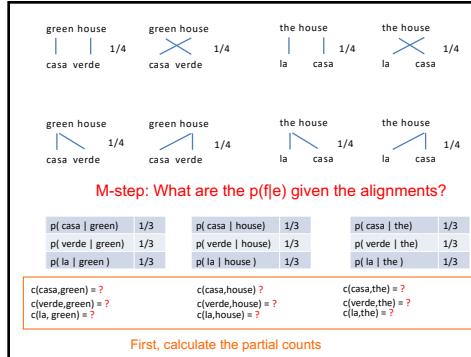
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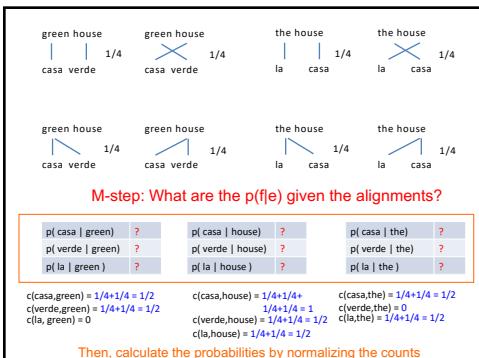
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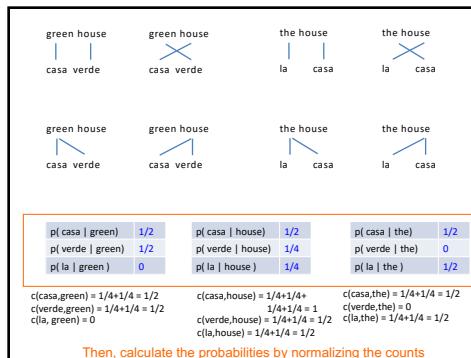
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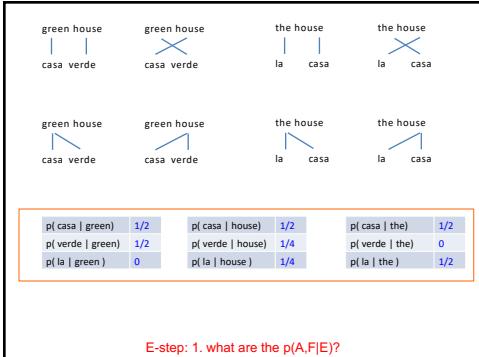
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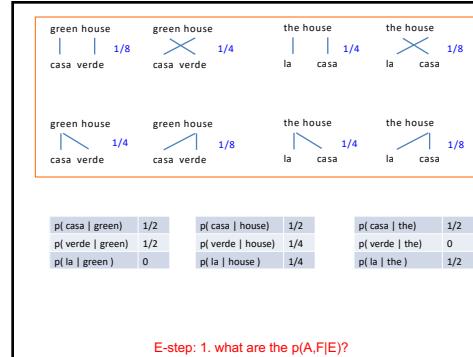
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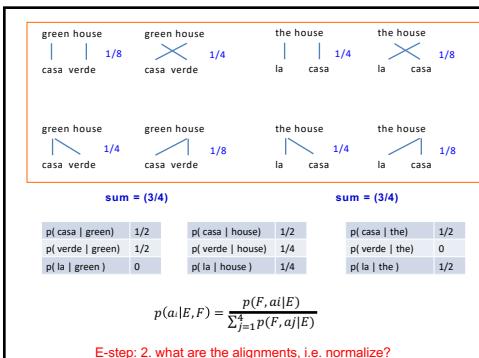
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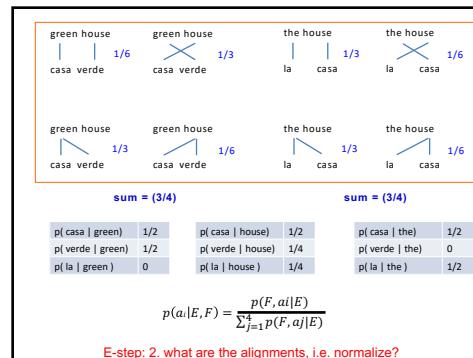
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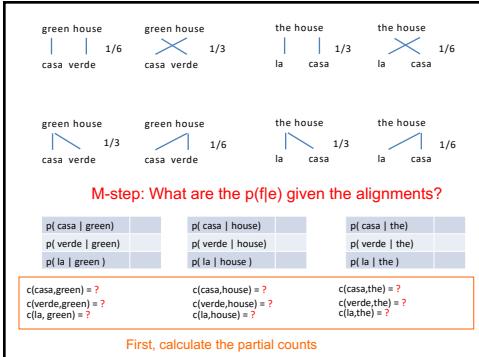
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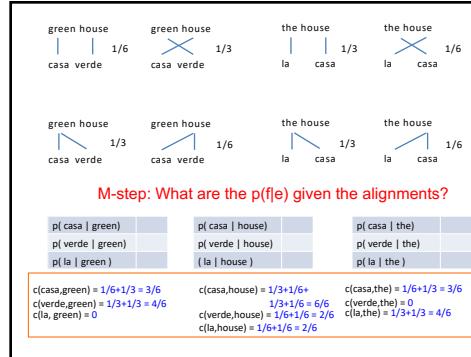
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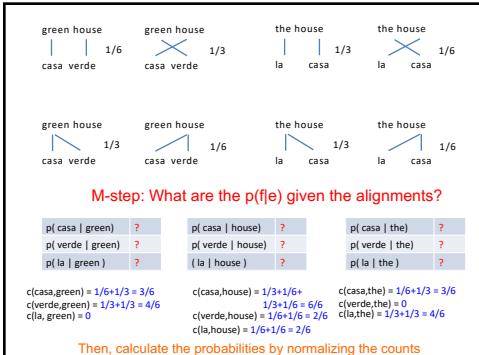
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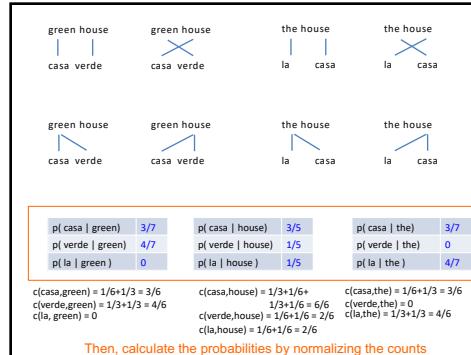
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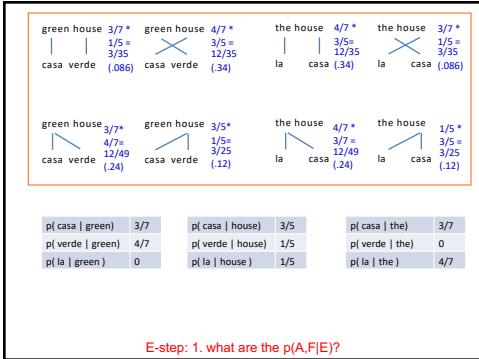
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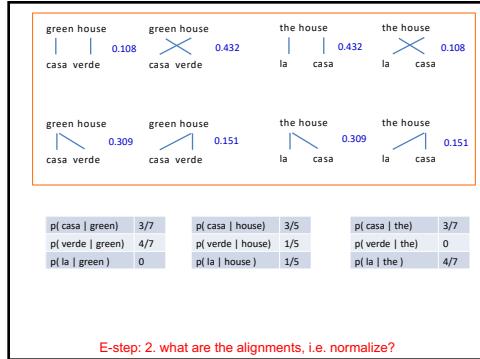


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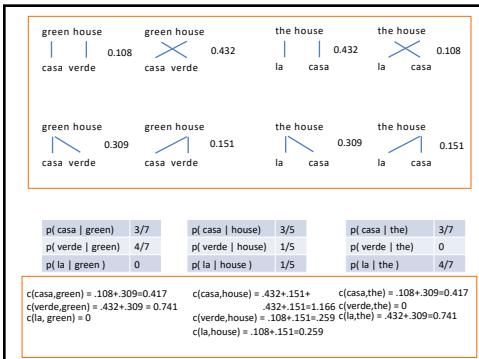
E-step: 1. what are the $p(A,F|E)$?

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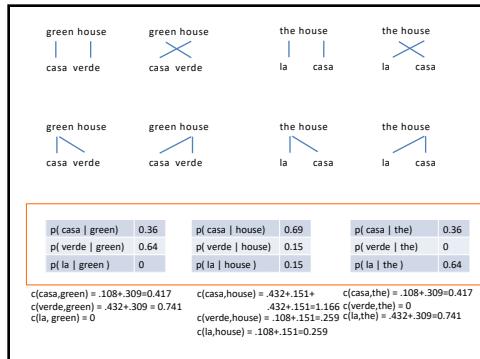


E-step: 2. what are the alignments, i.e. normalize?

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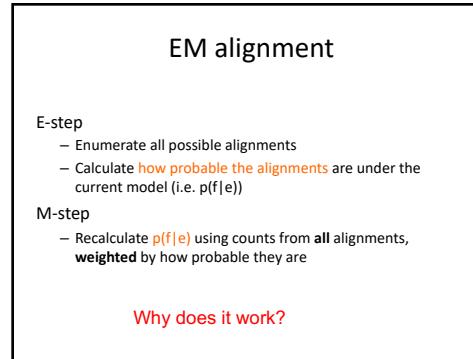


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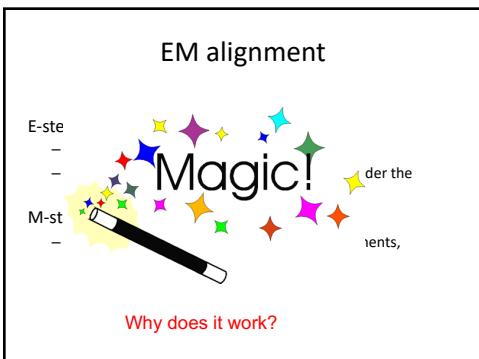
Iterate...

5 iterations			10 iterations			100 iterations		
$p(\text{casa} \mid \text{green})$	0.24		$p(\text{casa} \mid \text{green})$	0.1		$p(\text{casa} \mid \text{green})$	0.005	
$p(\text{verde} \mid \text{green})$	0.76		$p(\text{verde} \mid \text{green})$	0.9		$p(\text{verde} \mid \text{green})$	0.995	
$p(\text{la} \mid \text{green})$	0		$p(\text{la} \mid \text{green})$	0		$p(\text{la} \mid \text{green})$	0	
$p(\text{casa} \mid \text{house})$	0.84		$p(\text{casa} \mid \text{house})$	0.98		$p(\text{casa} \mid \text{house})$	~1.0	
$p(\text{verde} \mid \text{house})$	0.08		$p(\text{verde} \mid \text{house})$	0.01		$p(\text{verde} \mid \text{house})$	~0.0	
$p(\text{la} \mid \text{house})$	0.08		$p(\text{la} \mid \text{house})$	0.01		$p(\text{la} \mid \text{house})$	~0.0	
$p(\text{casa} \mid \text{the})$	0.24		$p(\text{casa} \mid \text{the})$	0.1		$p(\text{casa} \mid \text{the})$	0.005	
$p(\text{verde} \mid \text{the})$	0		$p(\text{verde} \mid \text{the})$	0		$p(\text{verde} \mid \text{the})$	0	
$p(\text{la} \mid \text{the})$	0.76		$p(\text{la} \mid \text{the})$	0.9		$p(\text{la} \mid \text{the})$	0.995	

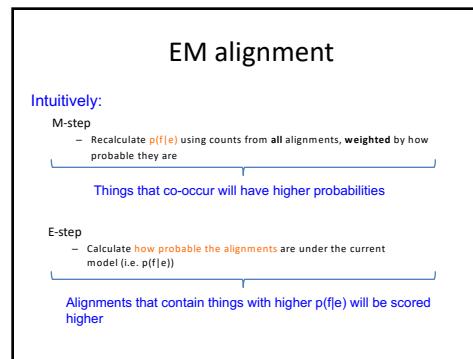
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An aside: estimating probabilities

What is the probability of "the" occurring in a sentence?

$$\frac{\text{number of sentences with "the"}}{\text{total number of sentences}}$$

Is this right?

Estimating probabilities

What is the probability of "the" occurring in a sentence?

$$\frac{\text{number of sentences with "the"}}{\text{total number of sentences}}$$

No. This is an **estimate** based on our data

This is called the **maximum likelihood estimation**.
Why?

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Maximum Likelihood Estimation (MLE)

Maximum likelihood estimation picks the values for the model parameters that maximize the likelihood of the training data

You flip a coin 100 times. 60 times you get heads.

What is the MLE for heads?

$$p(\text{head}) = 0.60$$

Maximum Likelihood Estimation (MLE)

Maximum likelihood estimation picks the values for the model parameters that maximize the likelihood of the training data

You flip a coin 100 times. 60 times you get heads.

What is the likelihood of the data under this model (each coin flip is a data point)?

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MLE example

You flip a coin 100 times. 60 times you get heads.

MLE for heads: $p(\text{head}) = 0.60$

What is the likelihood of the data under this model
(each coin flip is a data point)?

$$\text{likelihood}(\text{data}) = \prod_i p(x_i)$$

$$\log(0.60^{60} * 0.40^{40}) = -67.3$$

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MLE example

Can we do any better?

$$\text{likelihood}(\text{data}) = \prod_i p(x_i)$$

$$p(\text{heads}) = 0.5$$

$$\log(0.50^{60} * 0.50^{40}) = -69.3$$

$$p(\text{heads}) = 0.7$$

$$-\log(0.70^{60} * 0.30^{40}) = -69.5$$

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EM alignment: the math

The EM algorithm tries to find parameters of the model
($p(f|e)$) that *maximize the likelihood of the data*

In our case:

$$p(f_1 f_2 \dots f_{|f|} | e_1 e_2 \dots e_{|e|}) = \sum_{a_1} \sum_{a_2} \dots \sum_{a_{|f|}} p(f_i | e_a)$$

Each iteration, we increase (or keep the same) the likelihood of the data

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Implementation details

Any concerns/issues?
Anything underspecified?

Repeat:

E-step

- Enumerate all possible alignments
- Calculate how probable the alignments are under the current model (i.e. $p(f|e)$)

M-step

- Recalculate $p(f|e)$ using counts from all alignments, weighted by how probable they are

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Implementation details

When do we stop?

Repeat:

E-step

- Enumerate all possible alignments
- Calculate how probable the alignments are under the current model (i.e. $p(f|e)$)

M-step

- Recalculate $p(f|e)$ using counts from all alignments, weighted by how probable they are

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Implementation details

- Repeat for a fixed number of iterations
- Repeat until parameters don't change (much)
- Repeat until likelihood of data doesn't change much

Repeat:

E-step

- Enumerate all possible alignments
- Calculate how probable the alignments are under the current model (i.e. $p(f|e)$)

M-step

- Recalculate $p(f|e)$ using counts from all alignments, weighted by how probable they are

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Implementation details

For $|E|$ English words and $|F|$ foreign words, how many alignments are there?

Repeat:

E-step

Enumerate all possible alignments

- Calculate how probable the alignments are under the current model (i.e. $p(f|e)$)

M-step

- Recalculate $p(f|e)$ using counts from all alignments, weighted by how probable they are

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Implementation details

Each foreign word can be aligned to any of the English words (or NULL)



Repeat:

E-step

Enumerate all possible alignments

- Calculate how probable the alignments are under the current model (i.e. $p(f|e)$)

M-step

- Recalculate $p(f|e)$ using counts from all alignments, weighted by how probable they are

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Thought experiment

The old man is happy. He has fished many times.
 ↓
 El viejo está feliz porque ha pescado muchos veces.

His wife talks to him. The sharks await.
 ↓
 Su mujer habla con él. Los tiburones esperan.

$$p(f_i | e_{a_i}) = \frac{\text{count}(f \text{ aligned-to } e)}{\text{count}(e)}$$

$$p(\text{el} \leftrightarrow \text{the}) = 0.5$$

$$p(\text{Los} \leftrightarrow \text{the}) = 0.5$$

If we had the alignments

Input: corpus of English/Foreign sentence pairs along with alignment

for (E, F) in corpus:
 for aligned words (e, f) in pair (E,F):
 $\text{count}(e,f) += 1$
 $\text{count}(e) += 1$

for all (e,f) in count:
 $p(f|e) = \text{count}(e,f) / \text{count}(e)$

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If we had the alignments

Input: corpus of English/Foreign sentence pairs along with alignment

for (E, F) in corpus:
 for e in E:
 for f in F:
 if f aligned-to e:
 $\text{count}(e,f) += 1$
 $\text{count}(e) += 1$

for all (e,f) in count:
 $p(f|e) = \text{count}(e,f) / \text{count}(e)$

If we had the alignments

Input: corpus of English/Foreign sentence pairs along with alignment

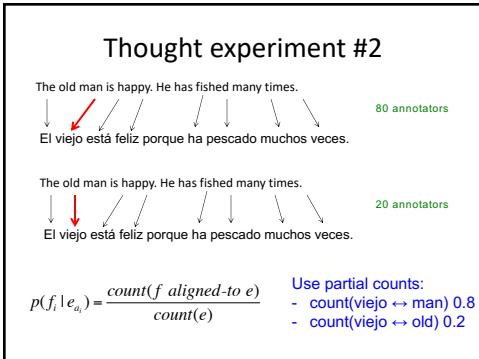
for (E, F) in corpus:
 for aligned words (e, f) in pair (E,F):
 $\text{count}(e,f) += 1$
 $\text{count}(e) += 1$

Are these equivalent?

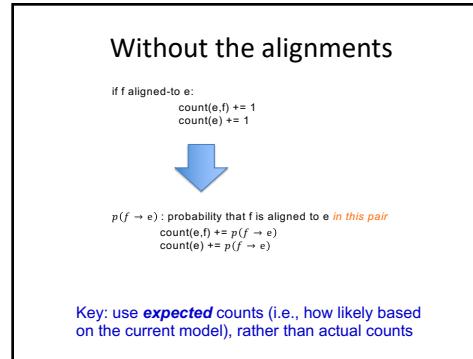
for all (e,f) in count:
 $p(f|e) = \text{count}(e,f) / \text{count}(e)$

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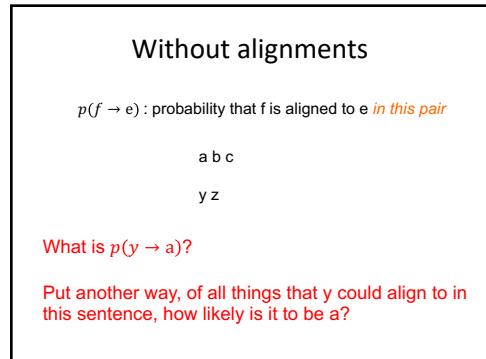
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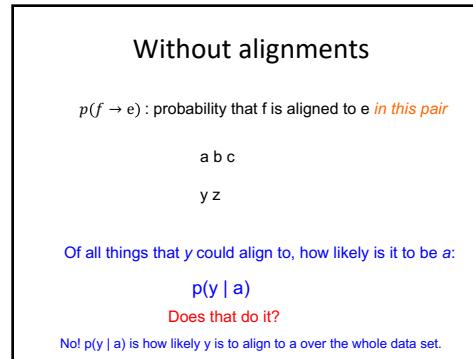
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Without alignments

$p(f \rightarrow e)$: probability that f is aligned to e *in this pair*



Of all things that y could align to, how likely is it to be a :

$$\frac{p(y | a)}{p(y | a) + p(y | b) + p(y | c)}$$

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Without the alignments

Input: corpus of English/Foreign sentence pairs (no alignment)

```
for (E, F) in corpus:
    for e in E:
        for f in F:
             $p(f \rightarrow e) = p(f|e) / \sum_{e \in E} p(f|e)$ 
            count(e,f) +=  $p(f \rightarrow e)$ 
            count(e) +=  $p(f \rightarrow e)$ 

    for all (e,f) in count:
         $p(f|e) = \text{count}(e,f) / \text{count}(e)$ 
```

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EM: without the alignments

Input: corpus of English/Foreign sentence pairs (no alignment)

```
for some number of iterations:
    for (E, F) in corpus:
        for e in E:
            for f in F:
                 $p(f \rightarrow e) = p(f|e) / \sum_{e \in E} p(f|e)$ 
                count(e,f) +=  $p(f \rightarrow e)$ 
                count(e) +=  $p(f \rightarrow e)$ 

        for all (e,f) in count:
             $p(f|e) = \text{count}(e,f) / \text{count}(e)$ 
```

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EM: without the alignments

Input: corpus of English/Foreign sentence pairs (no alignment)

```
for some number of iterations:
    for (E, F) in corpus:
        for e in E:
            for f in F:
                 $p(f \rightarrow e) = p(f|e) / \sum_{e \in E} p(f|e)$ 
                count(e,f) +=  $p(f \rightarrow e)$ 
                count(e) +=  $p(f \rightarrow e)$ 

        for all (e,f) in count:
             $p(f|e) = \text{count}(e,f) / \text{count}(e)$ 
```

77

EM: without the alignments

Input: corpus of English/Foreign sentence pairs (no alignment)

```
for some number of iterations:  
    for (E, F) in corpus:  
        for e in E:  
            for f in F:  
                 $p(f \rightarrow e) = p(f|e) / \sum_{e' \in E} p(f|e')$   
                count(e,f) +=  $p(f \rightarrow e)$   
                count(e) +=  $p(f \rightarrow e)$   
  
        for all (e,f) in count:  
             $p(f|e) = count(e,f) / count(e)$ 
```

Where are the E and M steps?

78

EM: without the alignments

Input: corpus of English/Foreign sentence pairs (no alignment)

```
for some number of iterations:  
    for (E, F) in corpus:  
        for e in E:  
            for f in F:  
                 $p(f \rightarrow e) = p(f|e) / \sum_{e' \in E} p(f|e')$   
                count(e,f) +=  $p(f \rightarrow e)$   
                count(e) +=  $p(f \rightarrow e)$ 
```

```
for all (e,f) in count:  
     $p(f|e) = count(e,f) / count(e)$ 
```

Calculate how probable the alignments are under the current model (i.e. $p(f|e)$)

79

EM: without the alignments

Input: corpus of English/Foreign sentence pairs (no alignment)

```
for some number of iterations:  
    for (E, F) in corpus:  
        for e in E:  
            for f in F:  
                 $p(f \rightarrow e) = p(f|e) / \sum_{e' \in E} p(f|e')$   
                count(e,f) +=  $p(f \rightarrow e)$   
                count(e) +=  $p(f \rightarrow e)$   
  
        for all (e,f) in count:  
             $p(f|e) = count(e,f) / count(e)$ 
```

Recalculate $p(f|e)$ using counts from all alignments, weighted by how probable they are

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NULL

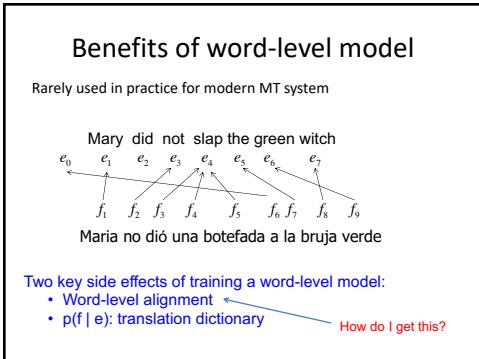
Sometimes foreign words don't have a direct correspondence to an English word

Adding a NULL word allows for $p(f | \text{NULL})$, i.e. words that appear, but are not associated explicitly with an English word

Implementation: add "NULL" (or some unique string representing NULL) to each of the English sentences, often at the beginning of the sentence

$p(\text{casa} \text{NULL})$	1/3
$p(\text{verde} \text{NULL})$	1/3
$p(\text{la} \text{NULL})$	1/3

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Word alignment

100 iterations

$p(\text{casa} \text{green})$	0.005
$p(\text{verde} \text{green})$	0.995
$p(\text{la} \text{green})$	0

green house
casa verde

How should these be aligned?

$p(\text{casa} \text{house})$	~1.0
$p(\text{verde} \text{house})$	~0.0
$p(\text{la} \text{house})$	~0.0

the house
la casa

$p(\text{casa} \text{the})$	0.005
$p(\text{verde} \text{the})$	0
$p(\text{la} \text{the})$	0.995

83

Word alignment

100 iterations

$p(\text{casa} \text{green})$	0.005
$p(\text{verde} \text{green})$	0.995
$p(\text{la} \text{green})$	0

green house
casa verde

Why?

$p(\text{casa} \text{house})$	~1.0
$p(\text{verde} \text{house})$	~0.0
$p(\text{la} \text{house})$	~0.0

the house
la casa

$p(\text{casa} \text{the})$	0.005
$p(\text{verde} \text{the})$	0
$p(\text{la} \text{the})$	0.995

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Word-level alignment

$$\text{alignment}(E, F) = \arg_A \max p(A, F | E)$$

Which for IBM model 1 is:

$$\text{alignment}(E, F) = \arg_A \max \prod_{i=1}^{|F|} p(f_i | e_{a_i})$$

Given a model (i.e. trained $p(f|e)$), how do we find this?
 Align each foreign word (f in F) to the English word (e in E) with highest $p(f|e)$

$$a_i = \arg_{j:1 \leq j \leq |E|} \max p(f_i | e_j)$$

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Word-alignment Evaluation

The old man is happy. He has fished many times.
↓ ↓ ↓ ↓
El viejo está feliz porque ha pescado muchos veces.

How good of an alignment is this?
How can we quantify this?

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Word-alignment Evaluation

System:
The old man is happy. He has fished many times.
↓ ↓ ↓ ↓
El viejo está feliz porque ha pescado muchos veces.

Human
The old man is happy. He has fished many times.
↓ ↓ ↓ ↓
El viejo está feliz porque ha pescado muchos veces.

How can we quantify this?

87

Word-alignment Evaluation

System:
The old man is happy. He has fished many times.
↓ ↓ ↓ ↓
El viejo está feliz porque ha pescado muchos veces.

Human
The old man is happy. He has fished many times.
↓ ↓ ↓ ↓
El viejo está feliz porque ha pescado muchos veces.

Precision and recall!

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Word-alignment Evaluation

System:
The old man is happy. He has fished many times.
↓ ↓ ↓ ↓
El viejo está feliz porque ha pescado muchos veces.

Human
The old man is happy. He has fished many times.
↓ ↓ ↓ ↓
El viejo está feliz porque ha pescado muchos veces.

Precision: $\frac{6}{7}$

Recall: $\frac{6}{10}$

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Appendix A

```

Input: corpus of English/Foreign sentence pairs (no alignment)

for some number of iterations:
    for (E, F) in corpus:
        for e in E:
            for f in F:
                 $p(f \rightarrow e) = p(f|e) / \sum_{e' \in E} p(f|e')$ 
                count(e,f) +=  $p(f \rightarrow e)$ 
                count(e) +=  $p(f \rightarrow e)$ 

        for all (e,f) in count:
             $p(f|e) = \text{count}(e,f) / \text{count}(e)$ 

```

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Appendix A

```

for (E, F) in corpus:
    for e in E:
        for f in F:
             $p(f \rightarrow e) = \frac{p(f|e)}{\sum_{e' \in E} p(f|e')}$ 
            count(e,f) +=  $p(f \rightarrow e)$ 
            count(e) +=  $p(f \rightarrow e)$ 

Pair 1: E: green house
          F: casa verde

Pair 2: E: the house
          F: la casa

```

Step 1: calculate $p(f \rightarrow e)$ for all pairs of words in the two sentences (assume $p(f|e)$ is a constant for all f,e)

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Appendix A

```

for (E, F) in corpus:
    for e in E:
        for f in F:
             $p(f \rightarrow e) = \frac{p(f|e)}{\sum_{e' \in E} p(f|e')}$ 
            count(e,f) +=  $p(f \rightarrow e)$ 
            count(e) +=  $p(f \rightarrow e)$ 

Pair 1: E: green house
          F: casa verde

Pair 2: E: the house
          F: la casa

```

Step 2: aggregate the counts

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Appendix A

```

Pair 1: E: green house
          F: casa verde

Pair 2: E: the house
          F: la casa

for all (e,f) in count:
     $p(f|e) = \text{count}(e,f) / \text{count}(e)$ 

Step 3: recalculate  $p(e|f)$ 

```

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Appendix A

Input: corpus of English/Foreign sentence pairs (no alignment)

for some number of iterations:

```
for e in E:
    for f in F:
        p(f → e) = p(f|e) / Σe in E p(f|e)           count(e,f)
        += p(f → e)
        count(e) += p(f → e)

    for all (e,f) in count:
        p(f|e) = count(e,f) / count(e)
```

94

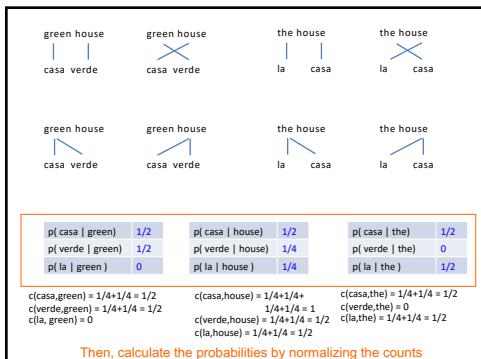
Worksheet

Pair 1:	Pair 2:
p(casa → green) =	p(la → the) =
p(casa → house) =	p(la → house) =
p(verde → green) =	p(casa → the) =
p(verde → house) =	p(casa → house) =

count(green, casa) =	count(the, casa) =
count(green, verde) =	count(the, la) =
count(house, casa) =	count(green) =
count(house, verde) =	count(house) =
count(house, la) =	count(the) =

p(casa green) =	p(casa the) =
p(verde green) =	p(la the) =
p(casa house) =	
p(verde house) =	
p(la house) =	

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