

Admin

Class Thursday: asynchronous

Assignment 10 due Sunday

Midterm 3 next week on Thursday (11/21)

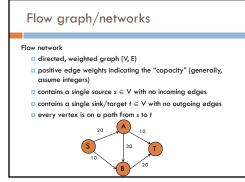
Assignment 11 (last one!) due Tuesday before Thanksgiving (11/26)

Class on 11/26?

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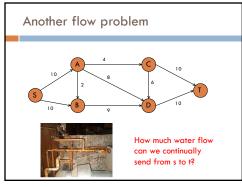


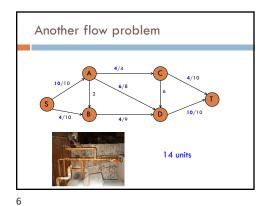
Flow constraints

in-flow = out-flow for every vertex (except s, t)

flow along an edge cannot exceed the edge capacity

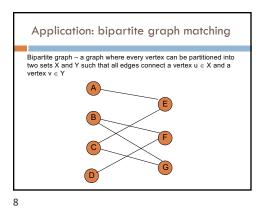
flows are positive

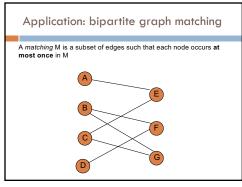


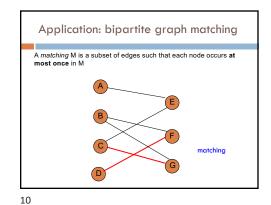


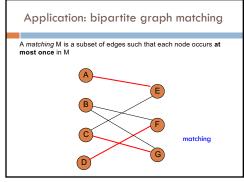
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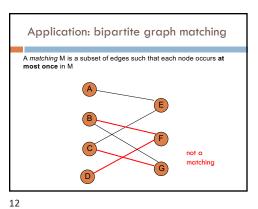
Given a flow network: what is the maximum flow we can send from s to t that meet the flow constraints?

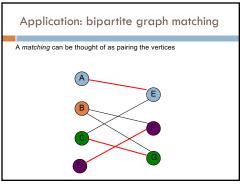












Application: bipartite graph matching

Bipartite matching problem: find the largest matching in a bipartite graph

Where might this problem come up?

- CS department has n courses and m faculty
- Every instructor can teach some of the courses
- What course should each person teach?
- Anytime we want to match n things with m, but not all things can metch

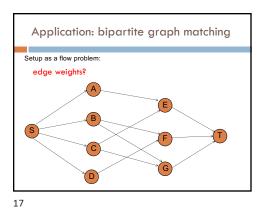
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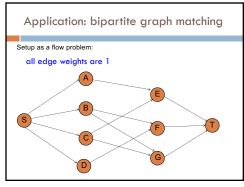
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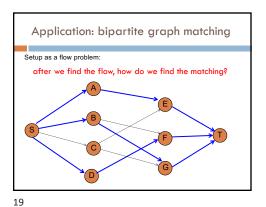
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Application: bipartite graph matching

Setup as a flow problem:





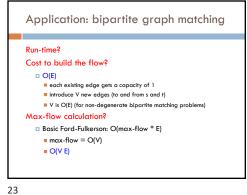


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Application: bipartite graph matching Setup as a flow problem: match those nodes with flow between them 20

Application: bipartite graph matching Run-time? Cost to build the flow? each existing edge gets a capacity of 1 ■ introduce V new edges (to and from s and t) ■ V is O(E) (for non-degenerate bipartite matching problems) Max-flow calculation? ■ Basic Ford-Fulkerson: O(max-flow * E) ■ Edmunds-Karp: O(V E²) □ Preflow-push: O(V³) What is the max flow?

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Application: bipartite graph matching Bipartite matching problem: find the largest matching in a bipartite - CS department has n courses and m faculty - Every instructor can teach some of the courses - What course should each person - Each faculty can teach at most 3 courses a semester? Change the s edge weights (representing faculty) to 3

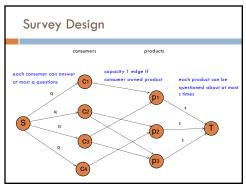
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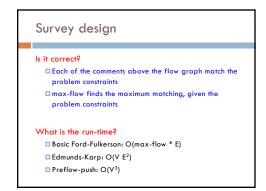
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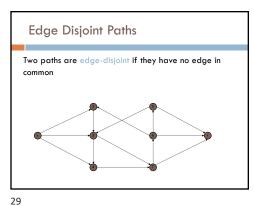
Application: bipartite graph matching Change the s edge weights (representing faculty) to 3 All others are capacity 1

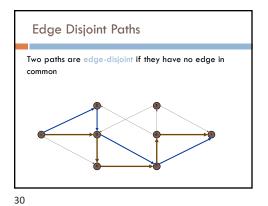
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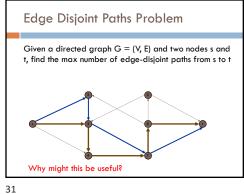
Survey Design Design a survey with the following requirements: □ Design survey asking *n* consumers about *m* products □ Can only survey consumer about a product if they own it $\hfill\square$ Question consumers about at most q products □ Each product should be surveyed at most s times ■ Maximize the number of surveys/questions asked How can we do this?





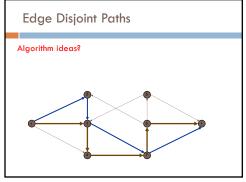


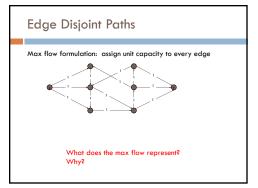




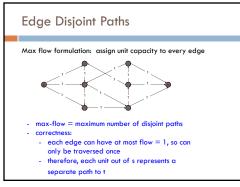
Edge Disjoint Paths Problem Given a directed graph G = (V, E) and two nodes s and t, find the max number of edge-disjoint paths from s to t Why might this be useful? a edges are unique resources (e.g. communications, transportation, etc.) □ how many concurrent (non-conflicting) paths do we have from s to t

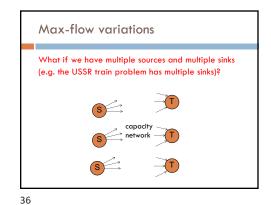
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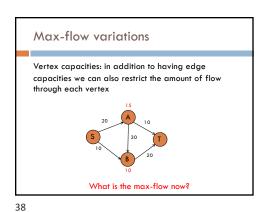


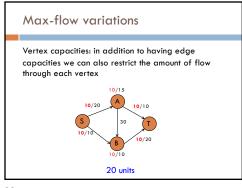


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Create a new source and sink and connect up with infinite capacities...





Max-flow variations

Vertex capacities: in addition to having edge capacities we can also restrict the amount of flow through each vertex

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How can we solve this problem?

